### 2.5 TRANSFORMATIONS ON GRAPHS

Types of transformations:

- (1) Translations - a "slide"
- (2) Reflections - a "flip" about a line
- (3) Rotations - a "turn" about a point
- (4) Dilations - compressions or stretches

The first 3 transformations do not affect the "shape" of a graph.

Before we start, try these:
For all the transformation below $f(x)=x^{2}$. Put $f(x)=x^{2}$ in Y1 of your calculator and each transformation on $Y 2$. Compare the graphs and describe each transformation.

1) $f(x)+5$ ___ Vertical translation/slide up
2) $f(x-3) \quad$ _Horizontal translation/slide up
3) $f(-x)$
___Reflection/flip over y-axis $\qquad$
4) $-f(x)$ $\qquad$ Reflection/flip over $x$-axis $\qquad$
5) $3 \cdot f(x)$
___ Vertical stretch $\qquad$
6) $f(2 x)$
___Horizontal compression $\qquad$

FOR PROBLEMS 7-12
When executing a transformation you may be manipulating $x$ before you execute the function, manipulating the result you get from the function, or manipulating both.

When the transformation manipulates $x$, as in $f(x+2)$, the point you plot is created as follows:

- The $x$ you plot is the $x$ you start with.
- The y you plot is the y you get when you evaluate the function for the MANIPULATED $X$.

For $f(x)=3 x+11, f(7)=32$. Plotted as $(7,32)$
Given this $f(x), \underline{f(x+2)}$ evaluated at $x=7$ would be plotted as follows:

$$
\begin{equation*}
(1, f(x+2)) \text { or }(1,3(7+2)+11) \text { or } \tag{1,38}
\end{equation*}
$$

When the transformation manipulates $f(x)$, as in $5^{*} f(x)$, the point you plot is created as follow:

- The $x$ you plot is the $x$ you start with.
- The y you plot is the result you get when you evaluate the function for the starting $x$ and then manipulate the functions result.

For $f(x)=3 x+11, f(7)=32$. Plotted as $(7,32)$

Given this $f(x), 5^{\star} f(x)$ evaluated at $x=7$ would be plotted as follows:
$\left(1,5^{\star} f(x)\right)$ or $\left(1,5^{\star}(3(7)+11)\right)$ or $(1,160)$

Complete the table to help you redraw each of the graphs befow according to the given transformation.
7) $f(x-2)$


Describe the transformation: __horizontal translation right 2_
8) $f(x+3)$


Describe the transformation: $\qquad$ horizontal translation left 3__

Complete the table to help you redraw each of the graphs below according to the given transformation.
9) $f(-x)$

|  | Old <br> $y$ | Old <br> pt |  | New Y | New <br> Pt |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $x$ | $f(x)$ | $(x, y)$ | $-x$ | $f(-x)$ | $(x, y)$ |
| -3 | 0 | $(-3,0)$ | 3 | 2.1 | $(-3,2.1)$ |
| -1 | 3 | $(-1,3)$ | 1 | 1 | $(-1,1)$ |
| 1 | 1 | $(1,1)$ | -1 | 3 | $(1,3)$ |
| 4 | 3 | $(4,3)$ | -4 | 0 | $(4,0)$ |
| 6 | 3 | $(6,3)$ | -6 | 0 | $(6,0)$ |

Transformation: $\qquad$ Rotate over the $y$-axis $\qquad$
10) $-f(x)$

|  | Old <br> $y$ | Old <br> pt | New Y | New <br> Pt |
| :---: | :--- | :--- | :--- | :--- |
| $X$ | $f(x)$ | $(x, y)$ | $-f(x)$ | $(x, y)$ |
| -3 | 0 | $(-3,0)$ | 0 | $(-3,0)$ |
| -1 | 3 | $(-1,3)$ | -3 | $(-1,-3)$ |
| 1 | 1 | $(1,1)$ | -1 | $(1,-1)$ |
| 4 | 3 | $(4,3)$ | -3 | $(4,-3)$ |
| 6 | 3 | $(6,3)$ | -3 | $(6,-3)$ |



Transformation: $\qquad$ rotate over the $x$-axis $\qquad$

$$
\text { 11) } 2 \cdot f(x)
$$

|  | Old <br> $y$ | Old <br> pt | New Y | New <br> Pt |
| :--- | :--- | :--- | :--- | :--- |
| $X$ | $f(x)$ | $(x, y)$ | $2 f(x)$ | $(x, y)$ |
| -3 | 0 | $(-3,0)$ | 0 | $(-3,0)$ |
| -1 | 3 | $(-1,3)$ | 6 | $(-1,6)$ |
| 1 | 1 | $(1,1)$ | 2 | $(1,2)$ |
| 4 | 3 | $(4,3)$ | 6 | $(4,6)$ |
| 6 | 3 | $(6,3)$ | 6 | $(6,6)$ |



Transformation: $\qquad$ Vertical stretch $\qquad$
12) $f(2 x)$


Transformation: $\qquad$ Horiontal compression $\qquad$

