

1) a) $(f \circ g)(2) = -5$ b) $(g \circ f)(2) = 88$ c) No

2) Undefined, Is $g(2)$ in the domain of f ? No

3) $(f \circ g)(-9)$ is undefined. $(g \circ f)(4) = 15$

Domain of $f(x)$: $[0, \infty)$, Domain of $g(x)$: All reals.

Domain of $f(g(x)) = [-5.5, \infty)$ Domain of $g(f(x)) = [0, \infty)$

FINDING A COMPOSITE FUNCTION

1) a) $F(g(x)) = (x-3)(x-1) = x^2 - 4x + 3$ $g(f(x)) = (x+3)(x-1) = x^2 + 2x - 3$

b) $F(g(3)) = 0$, $g(f(-2)) = -3$

2) $f(g(x)) = \sqrt{x-5}$ $[5, \infty)$

3) a) $f(g(x)) = \frac{1}{\frac{3}{x-2} + 1} = \frac{1}{\frac{3+x-2}{x-2}} = \frac{x-2}{x+1}$, Domain $\{x | x \neq -1, x \neq 2\}$

b) $G(f(x)) = \frac{-3x-3}{2x+1}$ Domain $\{x | x \neq -0.5, x \neq -1\}$

4) a) Both = x b) They create an identity function.

c) They are reflections over $y=x$.

5) a) Both = x b) Yes c) Yes d) (b,a) e) The segment is perpendicular to $y=x$.

FINDING THE COMPONENTS OF A COMPOSITE FUNCTION

1) $g(x) = 2x-5$ $f(x) = x^8$

2) $f(x) = 1/x$ $g(x) = x^2+1$

3) $f(g(x)) = 2(3x+a)^2 - 4(3x+a)$ if $(0, -2)$ is a point then

$2(3 \cdot 0 + a)^2 - 4(3 \cdot 0 + a) = -2 \Rightarrow 2a^2 - 4a + 2 = 0 \Rightarrow 2(a^2 - 2a + 1) = 2(x-1)^2$

$x=1$

FINDING THE INVERSE OF A FUNCTION

4) $f^{-1}(x) = (x-2) \cdot 3$

2.6 APPLICATIONS OF FUNCTIONS:

$$1) V(r) = \frac{32}{81} \pi t^9$$

$$2) a) C(N) = 15,000 + 8,000(100t - 5t^2)$$

$$C(N) = -40,000t^2 + 800,000t + 15,000, 0 \leq t \leq 10$$

$$b) \$2,055,000$$

$$3) H(x) = P(x) * I(x) = (P * I)(x)$$

$$4) T(x) = V(x) + P(x) = (V + P)(x)$$

$$5) N(x) = I(x) - T(x) = (I - T)(x)$$

$$6) R(x) = L(x) / P(x) = (L / P)(x)$$