

Keynesian Cross

Or The Aggregate Expenditure Model

Or Circular Flow Gone Wild

Do Activity 19

The model of chapter 27 was an important step in understanding macroeconomics.

However, it is inadequate to explain all the activities of the economy.

It has been superseded.

However, some of the concepts it gives us are foundational and referred part of our preferred model.

What we need to understand from chapter 27 and 28:

Mr. Benjamin's Base Case Flow Version of the Keynesian Cross

$$DI = S + C \quad (\text{or } S = DI - C)$$

$I = S$  as a starting point

The % of income consumed changes with income level  
OR the % of income saved changes with income level

There exists a breakeven income level  
above which people save  
below which people borrow to consume

The amount consumed is determined by Income

The shape and level of the consumption (and savings) schedules are determined by:

- Wealth
- Expectations
- Interest rates
- Debt
- Taxation

The model:

- The consumption schedule and axis
- APS, APC, MPS, MPC ( $MPS + MPC = 1$ )
- Changes in consumption versus changes in the amount consumed

Investment is determined by interest rates

- Expected rate of return
- Real interest rate

The amount invested is determined by real interest rates

The shape and level of the investment demand curve is determined by:

- Costs: Acquisition, maintenance, and operating
- Taxes
- Technology change
- Stock of capital
- Expectations

Investment is unstable:

- Durability and discretion in maintenance vs. acquisition allows firms can manage timing
- Innovation is unpredictable.
- Profits are a by-product of complex circumstance
- Expectations are variable

The model:

- The investment demand curve and axis

Multiplier model:

- Mechanism
- Multiplier =  $1 / (1 - mpc)$

Recessionary/Inflationary Gap

- Limitations of the model

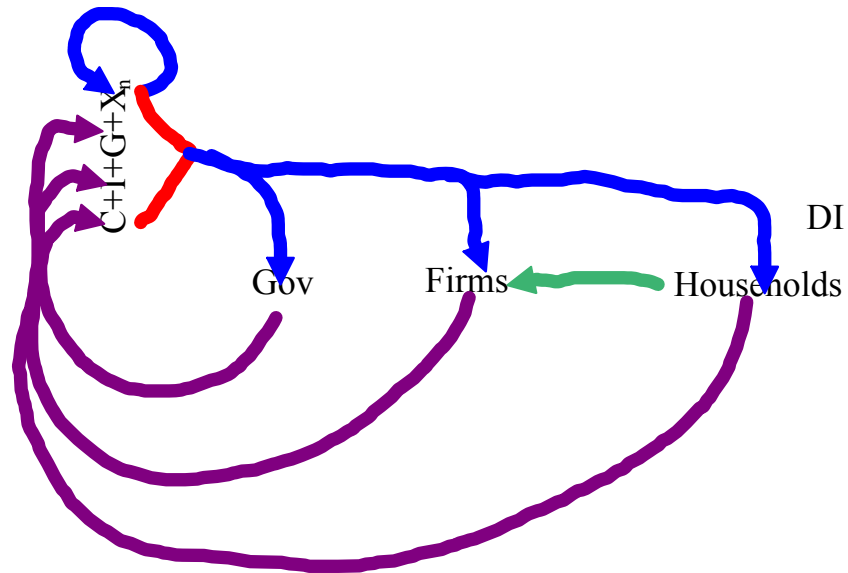
IN = OUT but amount of both can increase

Chapter 27 and 28

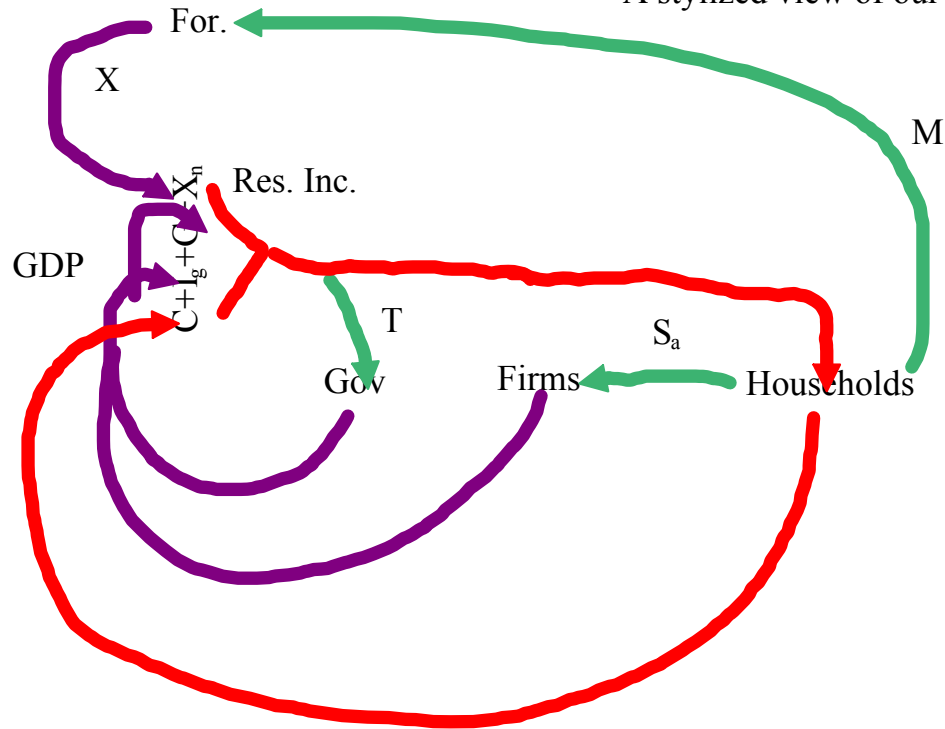
Building models to understand C,I,G, X

Understanding the mechanisms by which aggregate spending  
equilibrates with aggregate income.

Further exploring the leakages along the cycle from  
 $C+I+G+X_n \Rightarrow$  Resource Payments  $\Rightarrow$  DI



A stylized view of our macro-economic model.



The main artery is GDP providing resource income which should turn into C.

Everything else is a leakage or an injection.

*Household don't spend, they save? Leakage from C*

*Government taxes income? Leakage from C*

*Households buy foreign goods? Leakage from C*

*Government spends? An added injection*

*Firms decide to invest? An added injection.*

*Foreigners import our stuff? An added injection*

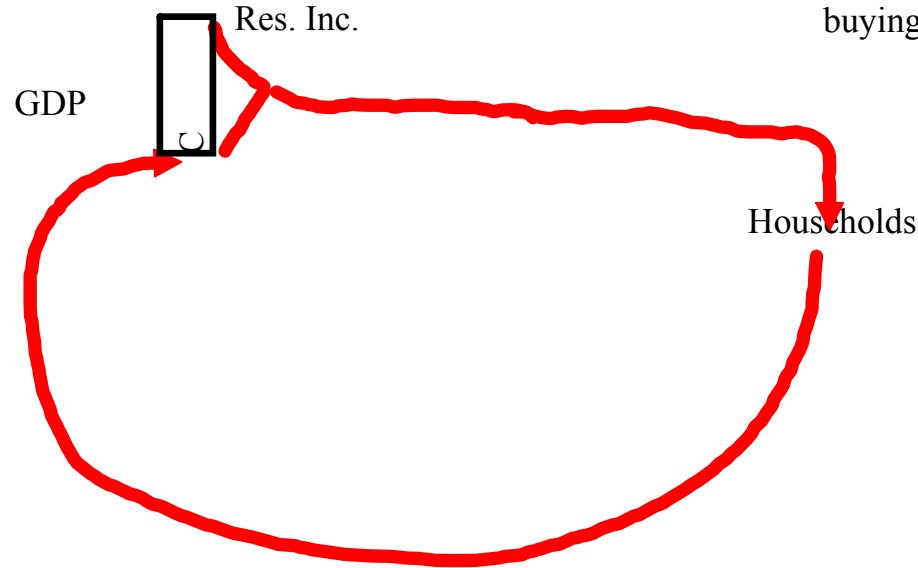
GENERAL RULE: INJECTIONS OR LEAKAGE  
HAVE A MULTIPLIED GDP IMPACT.

Coming next



Kill the government, forget Foreigners, and firms

Assume everyone is a farmer eating what they make, at most buying from their neighbors.



$$\text{Res. Inc.} = C = \text{GDP}$$

No injectors or leakers.

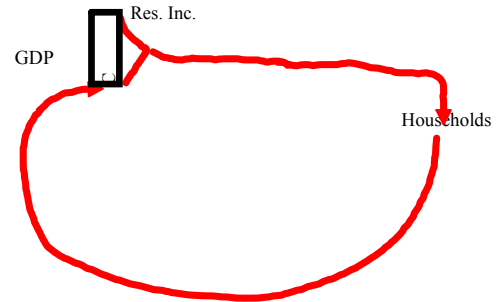
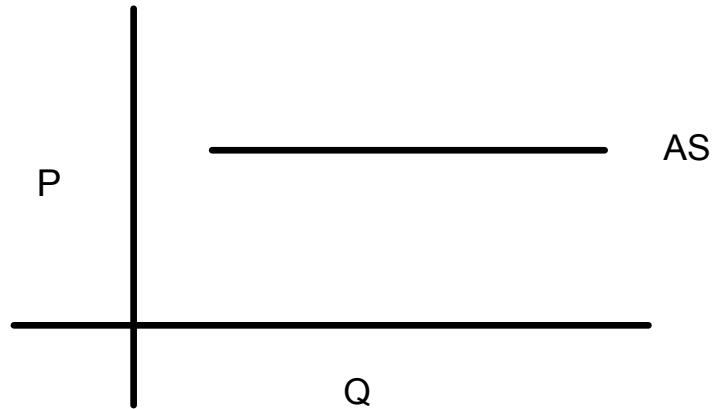
START HERE:

IF CONSUMERS WANT MORE, THEY BUY  
MORE IT TURNS INTO INCOME, IT KEEPS GOING.

Problem: No equilibrating mechanism, limiting factor

If people want more  
& firms figure it out  
=> they make more.

Economy is any size you want.



BUT,  
People don't spend every thing.

What are the implications of that?

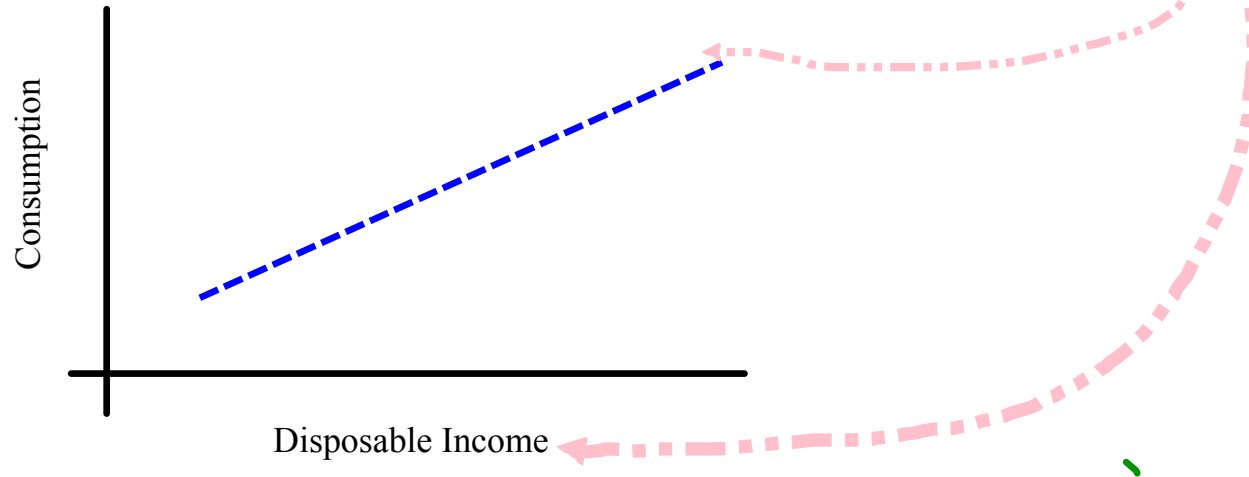
Top story C

We are satisfying wants and needs of consumers.  
Their buying and saving is the heart of the story.

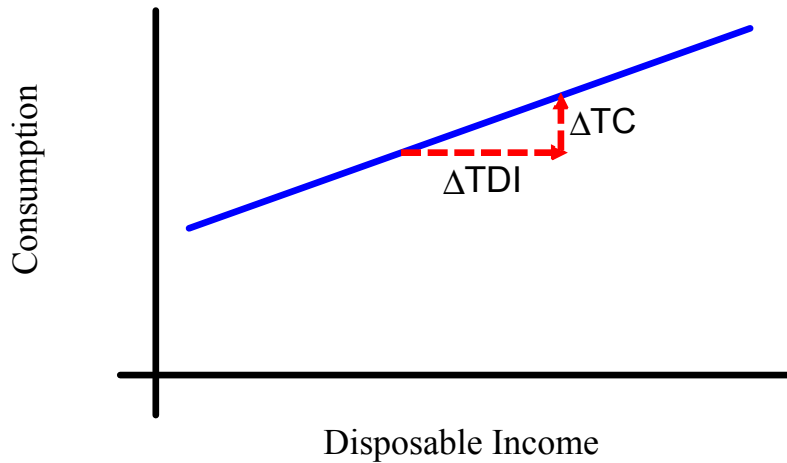
**The Model of C - the consumption schedule**

- 1) People spend PRINCIPALLY based on their understanding of  $DI\{C(DI)\}$
- 2) The ONLY alternative to spending is saving  
 $DI = C + S$  or  $(C = DI - S)$
- 3) As DI goes up consumption goes up.
- 4) Various factors determine how spending responds to DI (slope and height schedule)

{TBD}



KNOW THIS



1) The marginal propensity to consume is the slope of the consumption schedule

$$MPC = \frac{\Delta \text{ total dollars of Consumption}}{\Delta \text{ total disposable income}}$$

If  $DI^{\wedge} \$1 \Rightarrow C^{\wedge} .75$  then  $MPC = .75$

2) The households take every new dollar and spend some and save some.

MPS = Marginal propensity to save

$$MPS = \frac{\Delta \text{ total dollars saved}}{\Delta \text{ total disposable income}}$$

If  $DI^{\wedge} \$1 \Rightarrow C^{\wedge} .75$  then  $MPC = .75$   
&  $MPS = .25$

3) If every dollar is partially spent and partially saved:

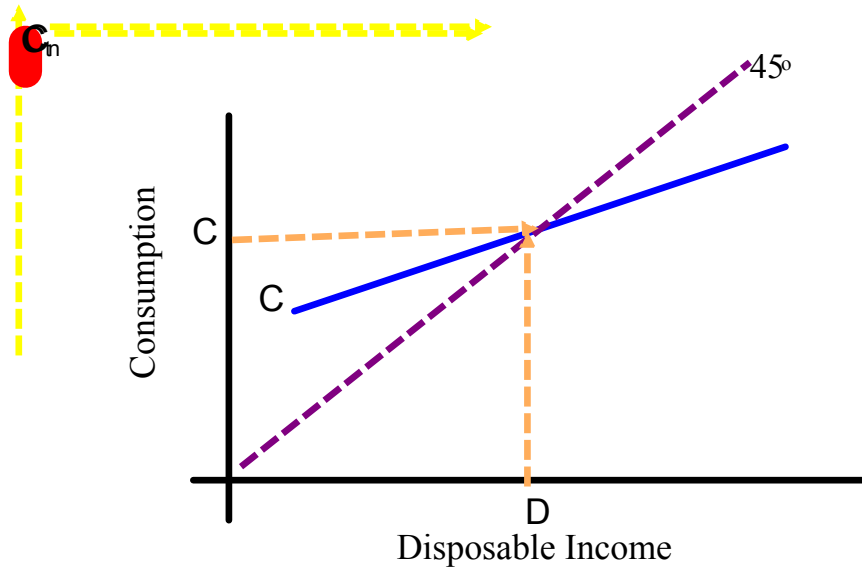
$$1 = MPC + MPS$$

$$MPC = 1 - MPS$$

$$MPS = 1 - MPC$$

4) Simplifying assumption: MPC is constant





The line has two key features, concepts:

1) MPC (slope)

2) 45° tells us breakeven income level  
The level at which you have exactly what you need to live.

- Above this DI people save some
- Below this DI people dis-save, borrow

The graph tells us

- The quantity consumed
- The quantity saved
- (see next slide)

What changes the way people spend?

Wealth - Perceived.

$W \wedge \Rightarrow C$  schedule ?

Expectations

Exp. Better  $\Rightarrow C$  schedule ?

Interest rates

$i$  (real)  $\vee \Rightarrow C$  schedule ?

Debt

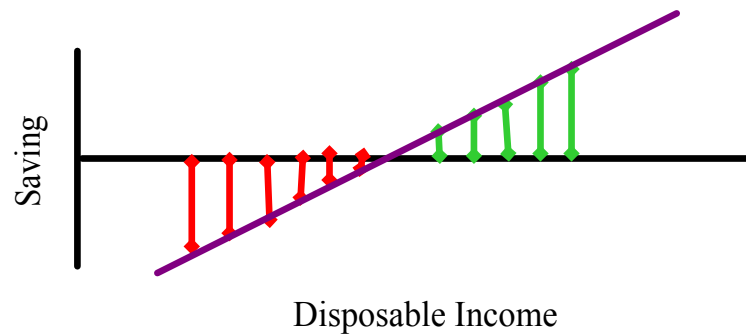
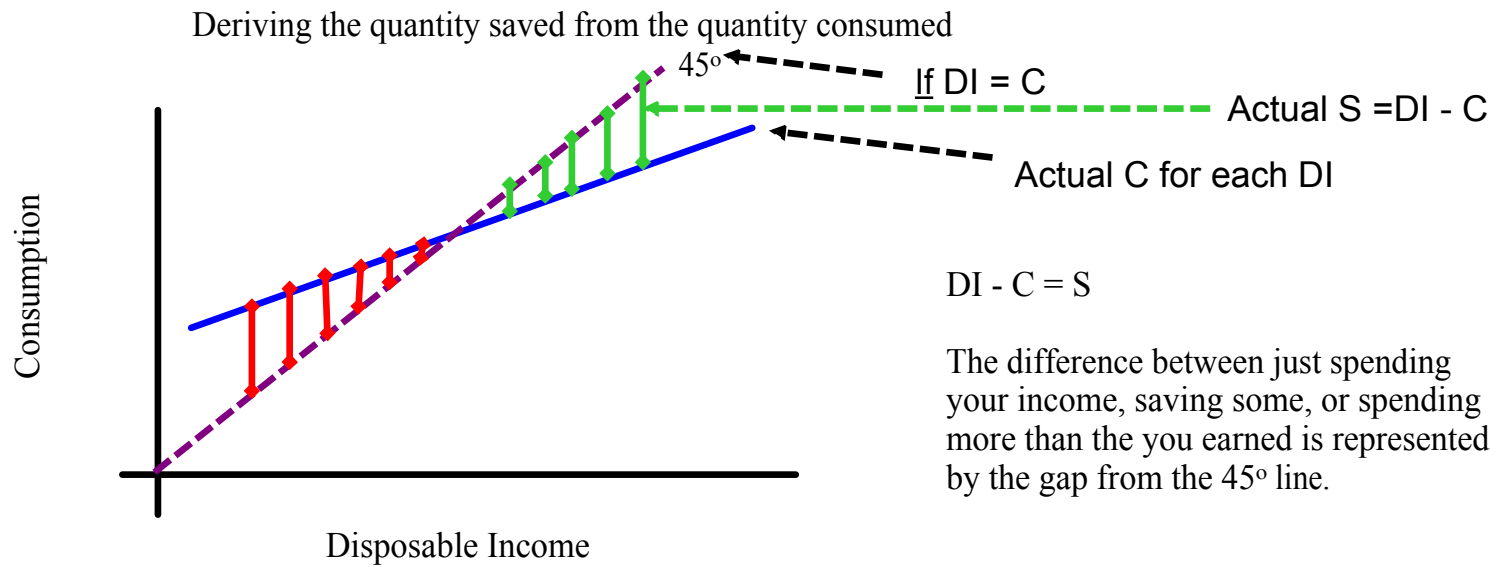
debt  $\wedge \Rightarrow C$  schedule ?\*

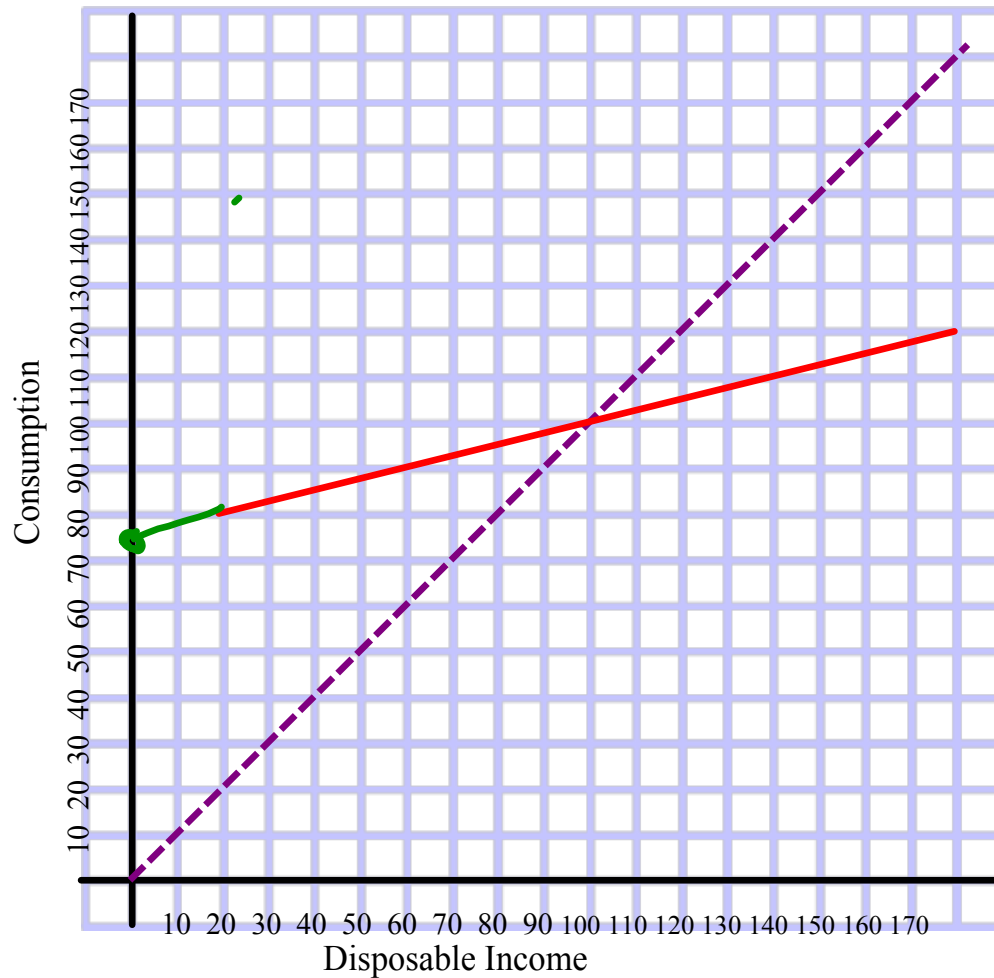
Taxation

taxes  $\wedge \Rightarrow C$  schedule ?

"increase in consumption"  
- the curve shifted up

"increase in quantity consumed"  
- Increase in DI moves us  
along the curve





What is the MPC?

What is the MPS?

At what disposable income do people spending exactly all their income?

What is the average propensity to consume when income is \$140?

What is the average propensity to save when income is \$20?

At what income level <sup>of income</sup> are consumers saving \$30?

At what income level are consumers borrowing \$30?

If income went from \$50 to \$70 what would happen?

If income went from \$130 to \$140 what would happen?

Key idea: Difference between average and marginal. LOOKING AT AGGREGATE

Other:

$$APC = \frac{\text{total consumption}}{\text{income}}$$

$$APS = \frac{\text{total savings}}{\text{income}}$$

If

MPC is constant and positive  
and  
at lowest income levels people dis-save or save nothing

MPC = .75

DI < \$10,000 people dis-save

then

Average propensity to consume  
Starts at 1 or above  
and  
Declines towards MPC as INCOME INCREASES

APC when DI < \$10,000?  
APC when DI > \$10,000?

Two statements:

As income increases the % of income consumed: ?

As income increases the % of income saved: ?

So, what can we do now:

Tell me how much DI moves and tell me MPC and I can tell you

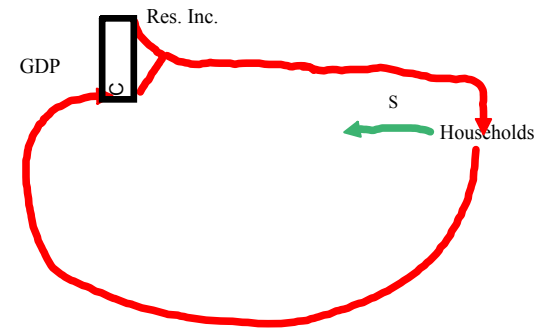
How much C changes

How much S changes

Tell me about a change in Wealth, Expectations, Interest rates, Debt, or Taxation  
and I can tell you what happens to C and S

AND TELL ME WHAT HAPPENS TO C AND I CAN TELL YOU WHAT HAPPENS  
TO GDP RIGHT?

NOT, more to discuss



## The multiplier effect

### Assumptions:

Each expenditure turns into income to the households providing resources.

Each household saves some and spends some.

The marginal propensity to consumer for all citizens is .75.  
The government prints \$1,000 and buys guns from Daria's Demolition

Spending

Savings

Daria provides all the resources to her company....

Daria takes home \$1,000 of new income

She does what with his \$1,000?

Everything Daria wants can be bought from Taylor's Teashop

Taylor provides all the resources to her company....

Taylor takes home \_\_\_\_\_ of new income

She does what?

Everything Taylor wants can be bought from Karen's K-mart

As Karen provides all the resources to her company....

Karen takes home \_\_\_\_\_ of new income

She does what?

Everything Karen wants can be bought from Brittany's Bargain's

As Brittany provides all the resources to her company....

Brittany takes home \_\_\_\_\_ of new income

She does what?

Brittany provides David with \_\_\_\_\_ of income with which David makes new purchases of \_\_\_\_\_

etc.....



A new amount of money spent generates an improvement of GDP as follows:

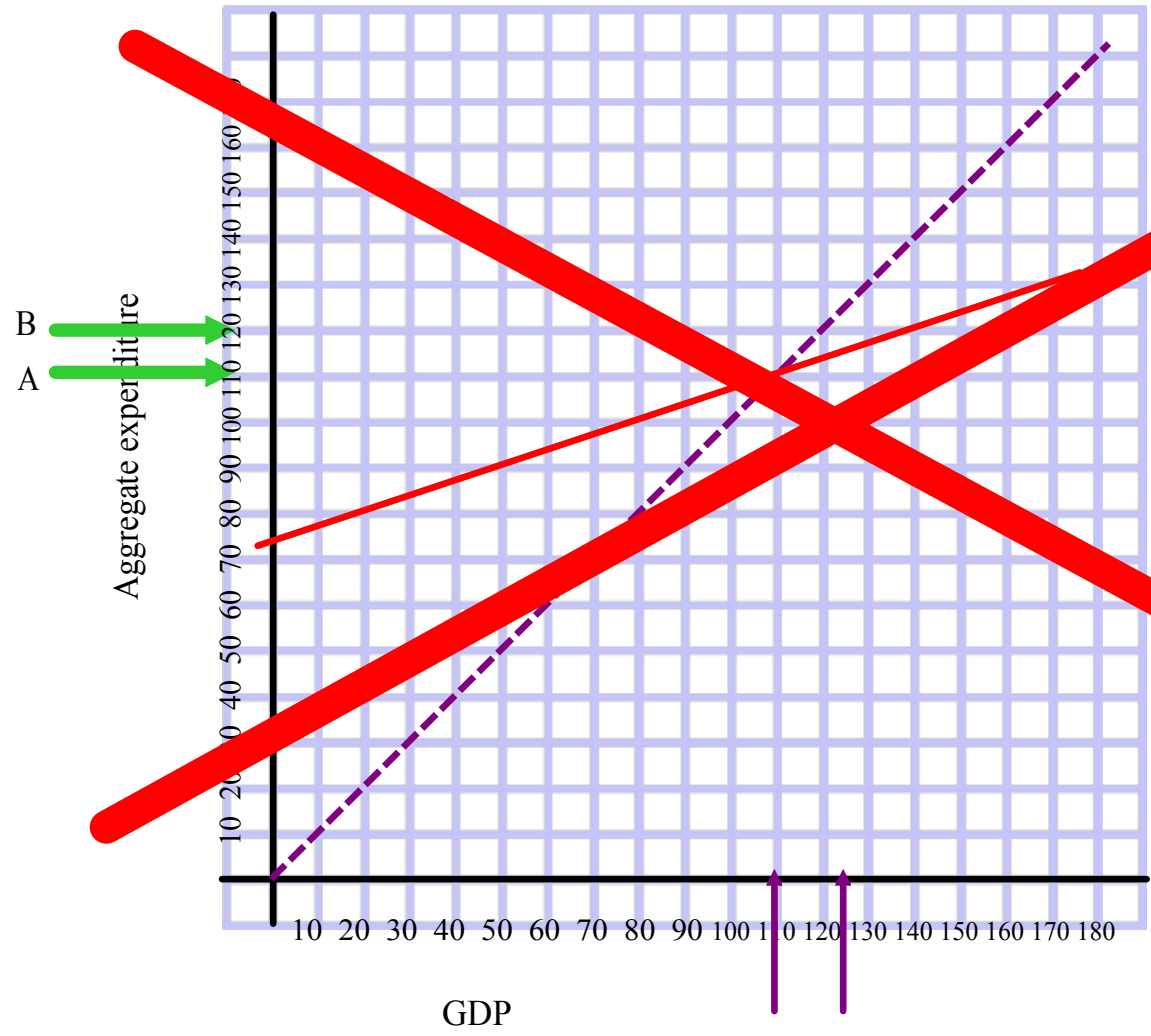
$$\text{Initial money spent} * \frac{1}{(1-\text{MPC})} = \text{Total GDP Increase}$$

$$= \frac{1}{\text{MPS}}$$

\$1,000 of new spending, MPS = .2.

What is the total impact on GDP?

What is the impact of the initial spending? What is the additional due to the multiplier effect?



If consumption increases from A to B, what is the impact on total income?

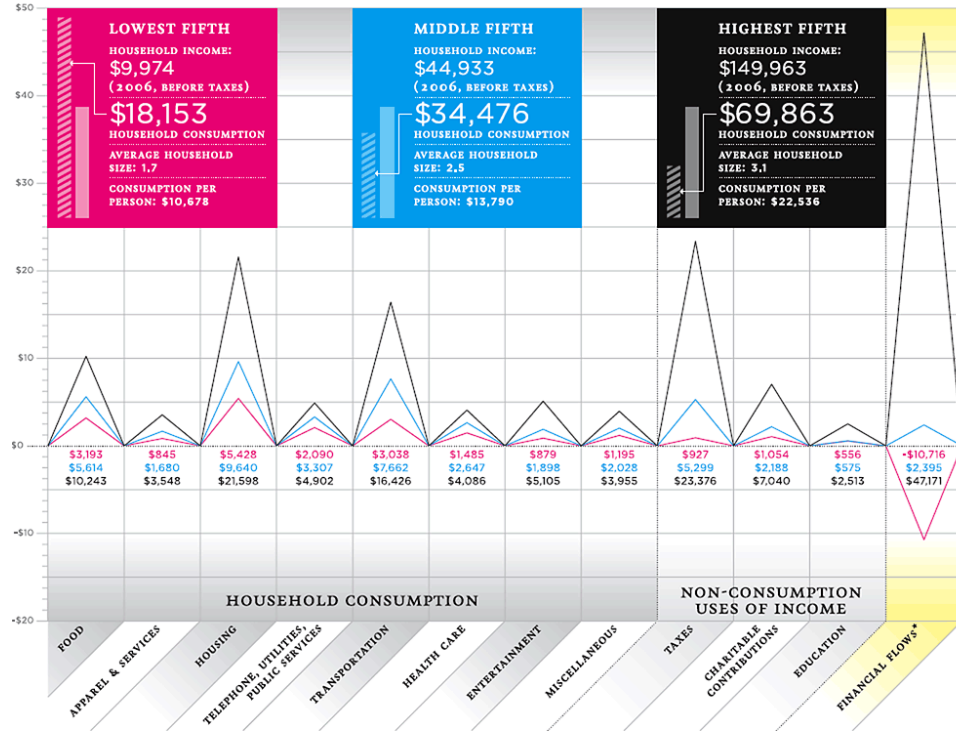
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HOUSEHOLD SPENDING  
IN THOUSANDS

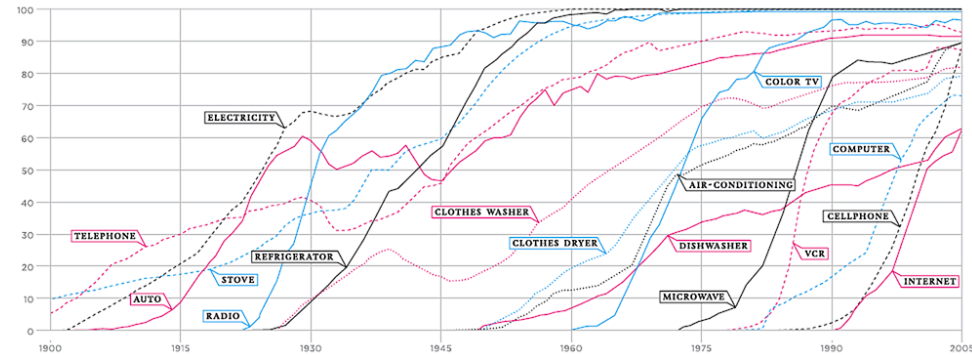
## HOW AMERICANS SPEND THEIR MONEY



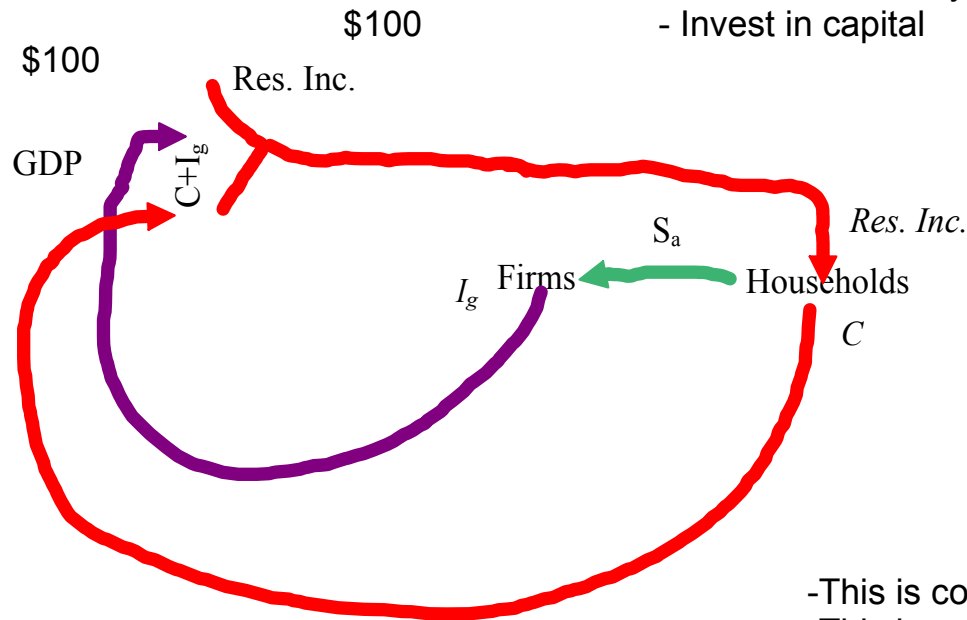
\* (FINANCIAL OUTFLOWS INCLUDE PAYMENTS LIKE PRIVATE PENSION CONTRIBUTIONS AND MORTGAGE PRINCIPAL; INFLOWS INCLUDE DRAWING DOWN OF SAVINGS, SALES OF PRINCIPAL HOLDINGS LIKE HOUSES OR SECURITIES, AND INSURANCE POLICIES REDEEMED.)

PERCENT OF  
U.S. HOUSEHOLDS

## CONSUMPTION SPREADS FASTER TODAY



But we know savings go to firms:  
 - Invest in inventory  
 - Invest in capital



For households:

$$\text{Res. Inc.} = \text{DI} = C + S_a$$

Assume Firms:

$$S_a = I_g$$

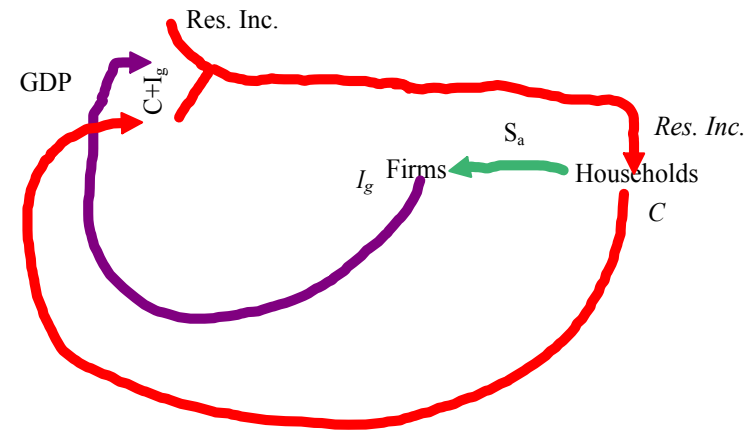
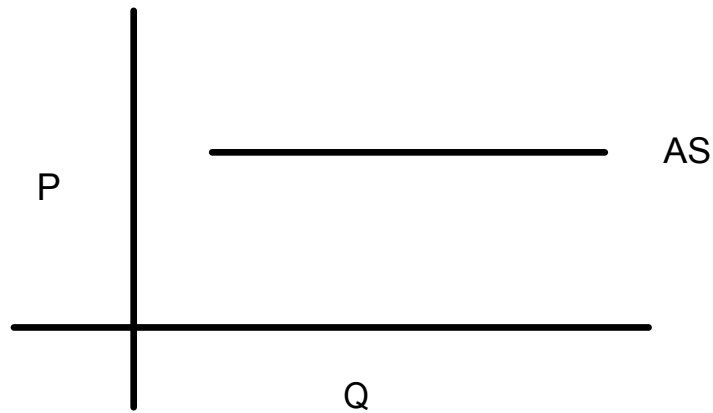
- This is consistent with our capital markets model.
- This is a point of contention.

WHEN WE ARE IN A STABLE STATE  
 S=I

Problem: No equilibrating mechanism, limiting factor

If people want more  
& firms figure it out  
=> they make more.

Economy is any size you want.



OK, but who decides where we are?

To have stuff people must work, so we know  
the answer is not an infinite amount.

Before we get answer, is it all up to  
consumers or can firms increase level of  
GDP?

No. If firms produce more to try boost C:  
 - The extra production increases DI  
 =>  $DI^{\wedge} \Rightarrow C^{\wedge}$  BUT because of S,  $C^{\wedge} < DI^{\wedge}$  and so is **less than the value of new goods**.  
 => Some of the new production stays on shelf  
     UNINTENDED INVESTMENT ( $I^{\wedge}$ ) happens => cut production  
 =>  $DI \vee \Rightarrow C \vee \Rightarrow$  unintended investment ( $I \vee$  some) => Not enough? Cut production =>  
     Until we get back to original C.

There are three stories we can tell:

- What happens if firms cut production?  $DI \vee \Rightarrow C \vee$ ,  $\{C \vee < DI \vee, C \vee$  **less than prod. cut** $\} \Rightarrow$   
     Unintended disinvestment ( $I \vee$ ) => increased production =>  $DI^{\wedge} \Rightarrow C^{\wedge} \Rightarrow$  until
- What happens when households want more C?  
      $C^{\wedge} \Rightarrow$  Unintended disinvestment ( $I \vee$ ) => increased production =>  $DI^{\wedge} \Rightarrow C^{\wedge} \Rightarrow$  until
- What happens when households want less C?  
      $C \vee \Rightarrow$  Unintended investment ( $I^{\wedge}$ ) => decreased production =>  $DI \vee \Rightarrow C \vee \Rightarrow$  until

Bottom line:

Investment must = Savings.

Business can only invest as much as people  
 set aside through saving.

So, any change in their injection, I

will be matched by a change household leakage, S

HOUSEHOLDS ARE IN CHARGE

Keynes: Firms can not determine

- 1) Size of economy
- 2) Total investment

But, savings is affected by interest rates:

Keynes cross does not give interest rate mechanism we can think about the following

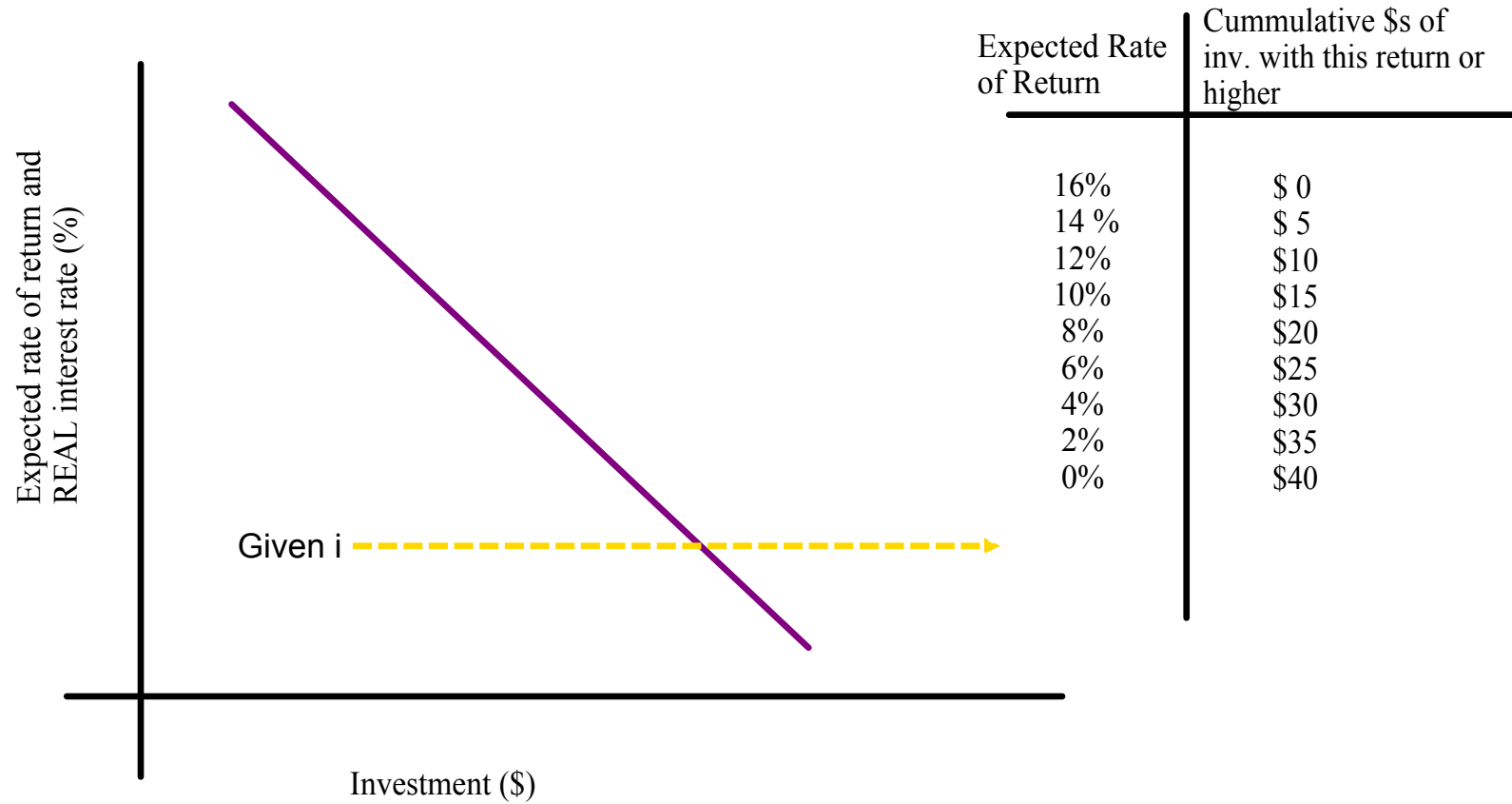
Firm demand  $\hat{Y} \Rightarrow i \hat{Y} \Rightarrow S \hat{Y}$ , possibly

Government sets  $i \downarrow \Rightarrow$  Quantity demand  $\hat{Y}$ , but  $S \downarrow$ , shortage  $\Rightarrow$  gets back

Government sets  $i \uparrow \Rightarrow$  Quantity demand  $\downarrow$ , but  $S \uparrow$ , surplus  $\Rightarrow$  gets back

A MORE NEEDED TOPIC

### Investment Demand - Revisited Side Bar



A CHANGE SHIFTS THE EXPENDITURE CURVE AS A WHOLE



So I is a function of the real interest rate.

$$E(\text{Ret}) = \frac{E(\text{Rev}) - \text{Costs}}{\text{Outlay/Inv.}}$$

But what will shift the curve

Acquisition, maintenance, and operating costs

Costs  $\downarrow \Rightarrow ?$

Business taxes

Taxes  $\wedge \Rightarrow ?$

Technological Change

$\Rightarrow ?$

Stock of capital

Comparison of one state to another

Expectations

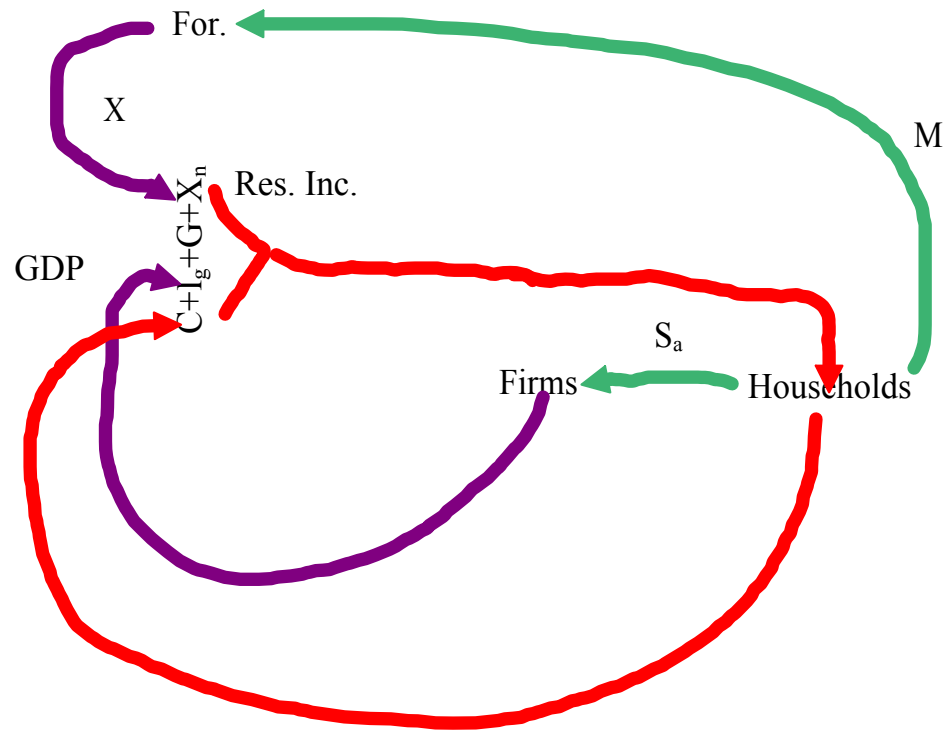
Investment is unstable:

Costs of buying high quality capital purchased and/or maintaining capital weighed against acquisition allows firms can manage timing

Innovation is unpredictable.

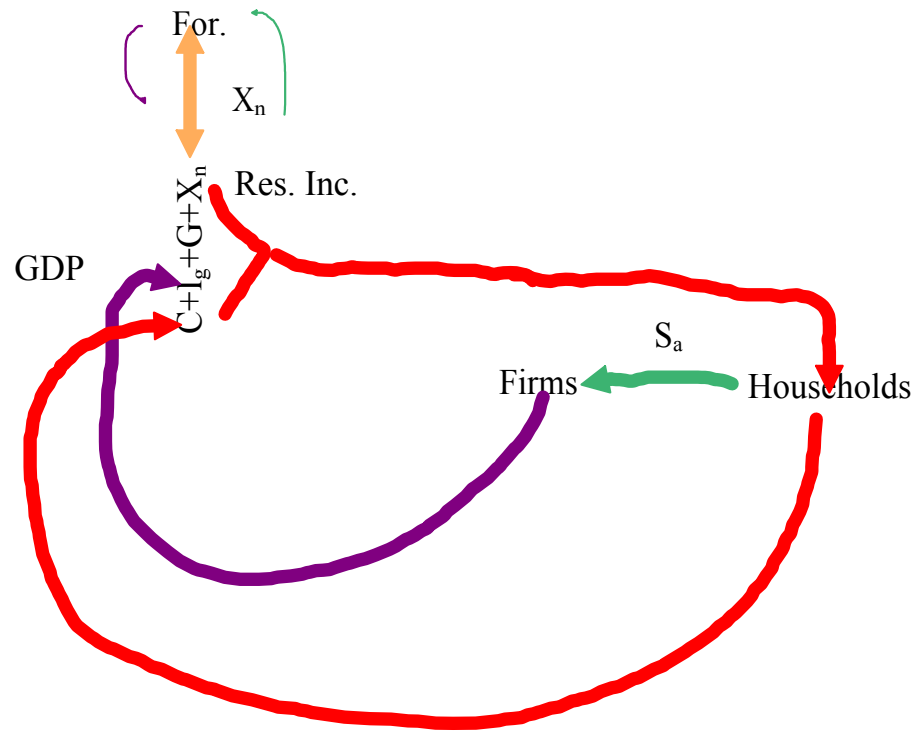
Profits are a by-product of complex circumstance

Expectations are variable



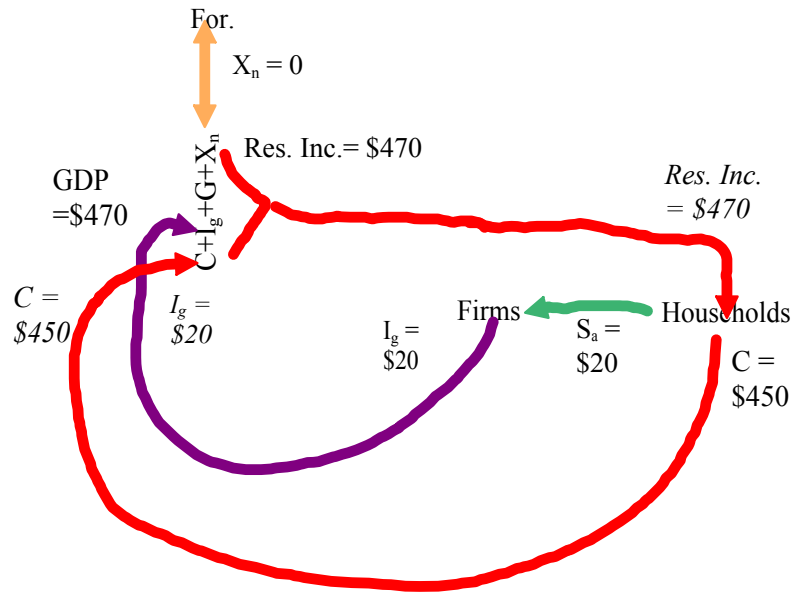
Looking at  $X_n$

This is the more realistic picture but  
let's simplify:



If  $X_n$  reflects higher  $X$  than  $M$  then this is an injection to the economy.

Hit the spending with the multiplier and it grows equilibrium GDP.

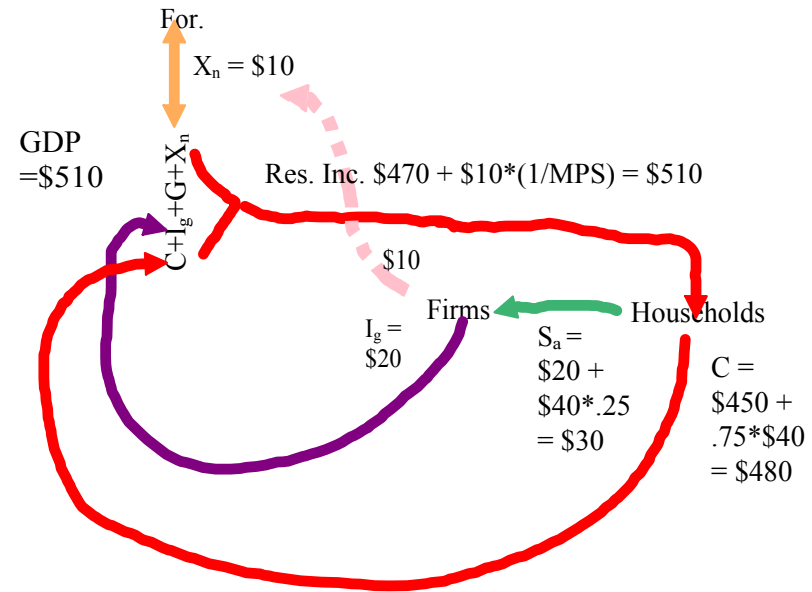


If this is equilibrium with no foreign flows, then...

Note: You either have to assume that

- $X$  always =  $M$  at equilibrium
- Firms finance exports. (closer to reality)

A MORE NEEDED TOPIC



If we are selling more goods than we import, then that is an injection subject to the multiplier.

$\$10$ , after multiple rounds, will grow equilibrium to  $\$510$ .

Important idea:

$X_n$  is assumed to be this thoroughly exogenous injection or leakage.

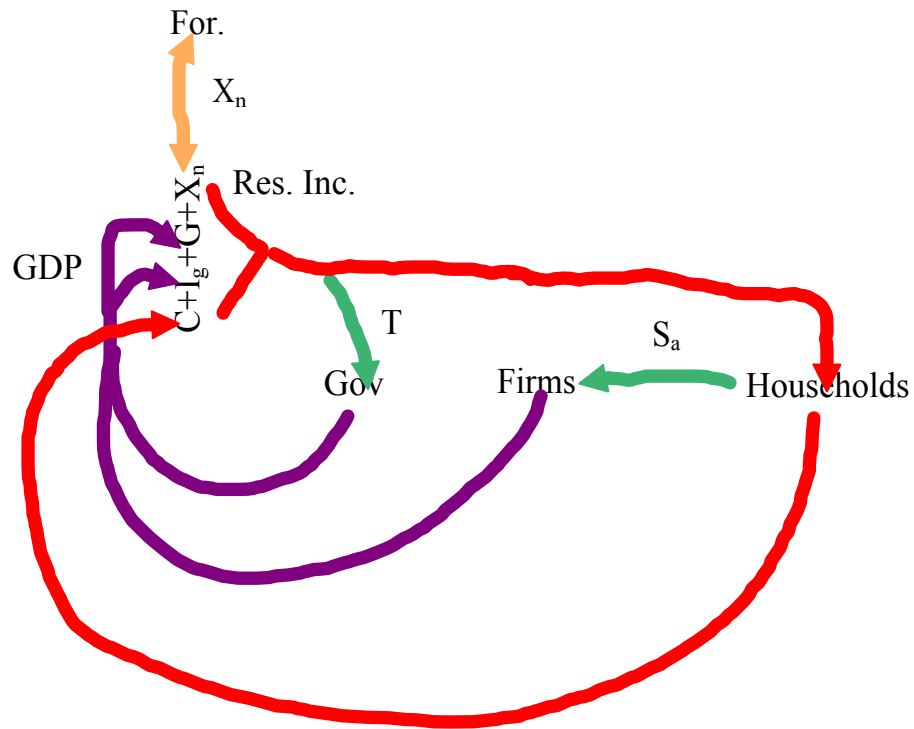
Hmmm....

No, our GDP effects C, which effects M

Also, our M effects GDP in other countries, which effects X

Exchange rate are not exogenous (GDP effects them), they effect M and X

But this is a good basic first thought



Add government.

It would be neat to think of it in the same net way as the foreign spending.

But a problem.

The government has two possible actions.

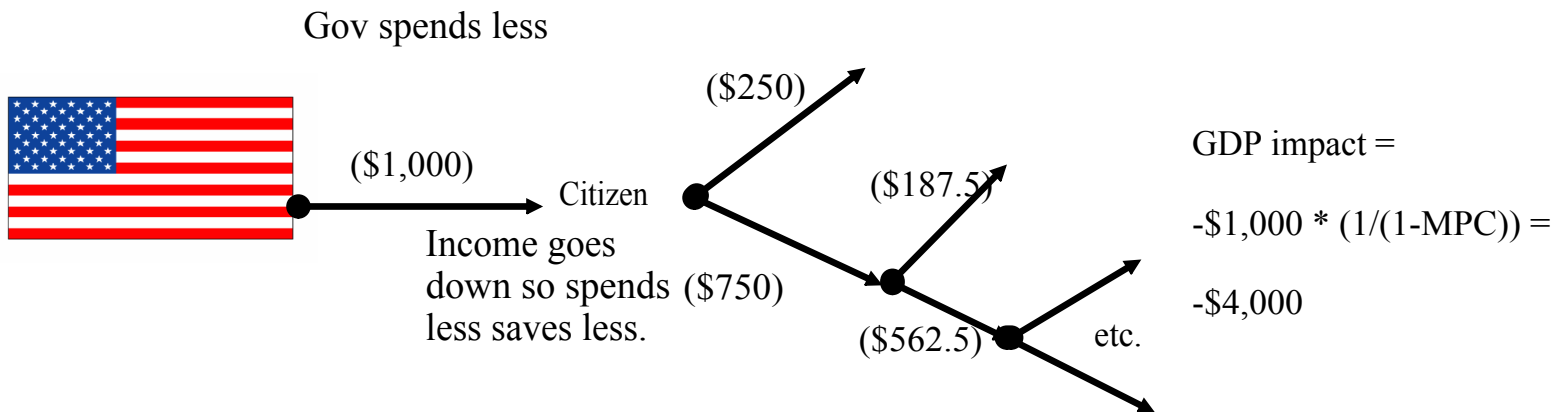
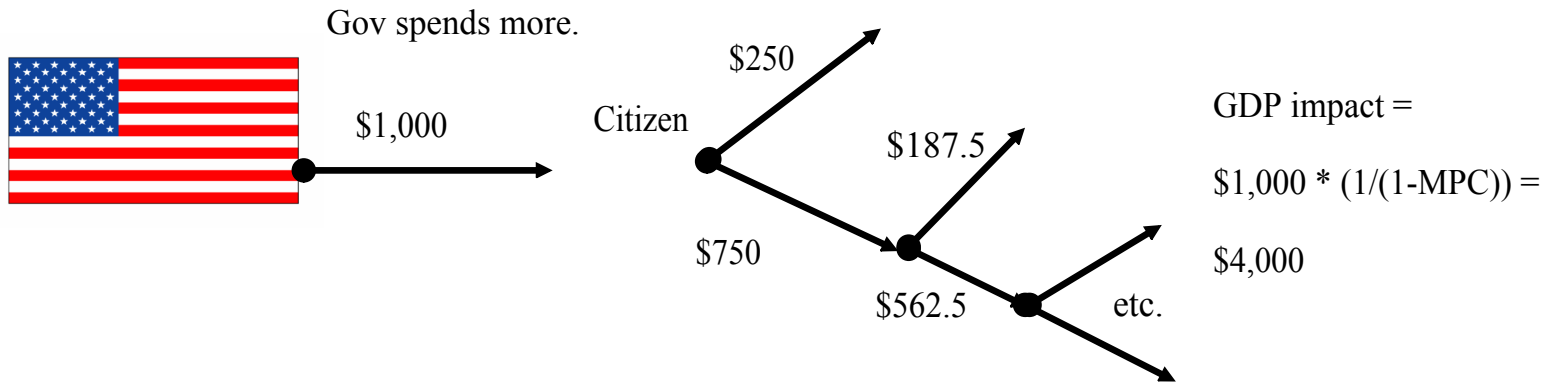
- Tax or spend

THEY DO NOT HAVE THE SAME EFFECT.

G is a direct insertion.

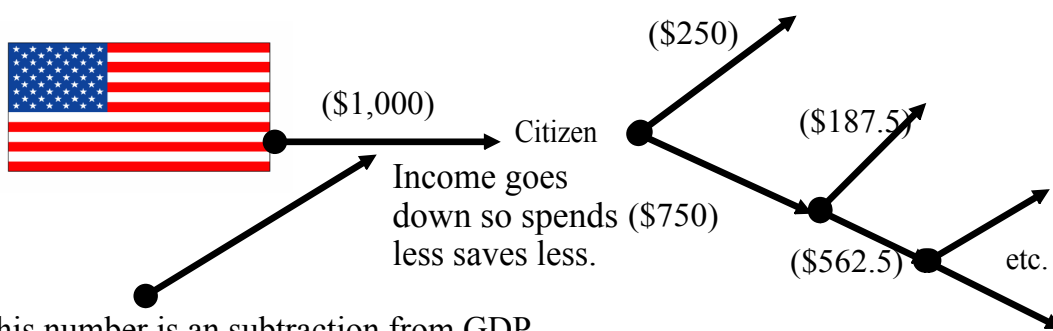
$$G * (1/(1-MPC)) = \text{GDP impact}$$

T is a DEDUCTION from income, not the same





Gov spends less



This number is a subtraction from GDP the rest follow. This is first round.

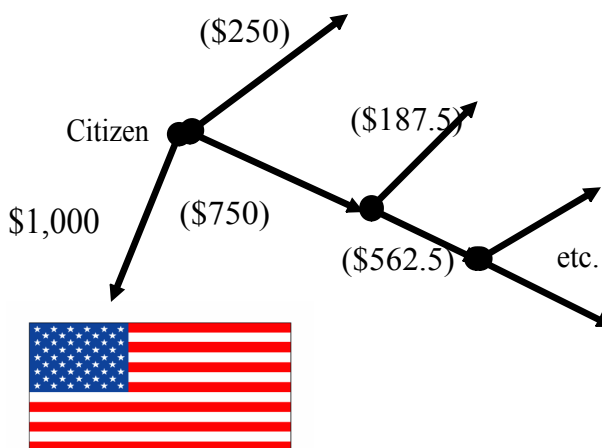
GDP impact =

$$-\$1,000 * (1/(1-MPC)) =$$

$$-\$4,000$$

With taxes, Citizen, takes from savings and spending budget and gives it to government.

There is no first round from government.



GDP impact, same as above EXCEPT there is no first round impact.

$$-\$1,000 * MPC * (1/(1-MPC)) =$$

$$-\$1,000 * MPC/(1-MPC) =$$

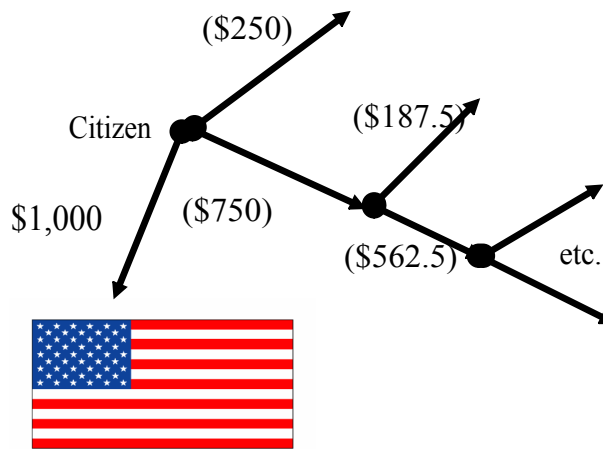
$$-\$1,000 * (3/4)/(1-(3/4))$$

$$-\$1,000 * 3 = -\$3,000$$

Tax increase

With taxes, Citizen, takes from savings and spending budget and gives it to government.

There is no first round from government.



GDP impact, same as above EXCEPT there is no first round impact.

$$-\$1,000 * MPC * (1/(1-MPC)) =$$

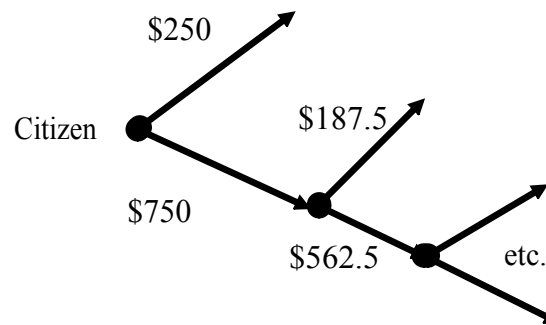
$$-\$1,000 * MPC/(1-MPC) =$$

$$-\$1,000 * (3/4)/(1-(3/4))$$

$$-\$1,000 * 3 = -\$3,000$$

Tax decrease

Citizen has \$250 more to save and spend, because he/she does not give it to the government.



GDP impact, same as above EXCEPT there is no first round impact.

$$\$1,000 * MPC * (1/(1-MPC)) =$$

$$\$1,000 * MPC/(1-MPC) =$$

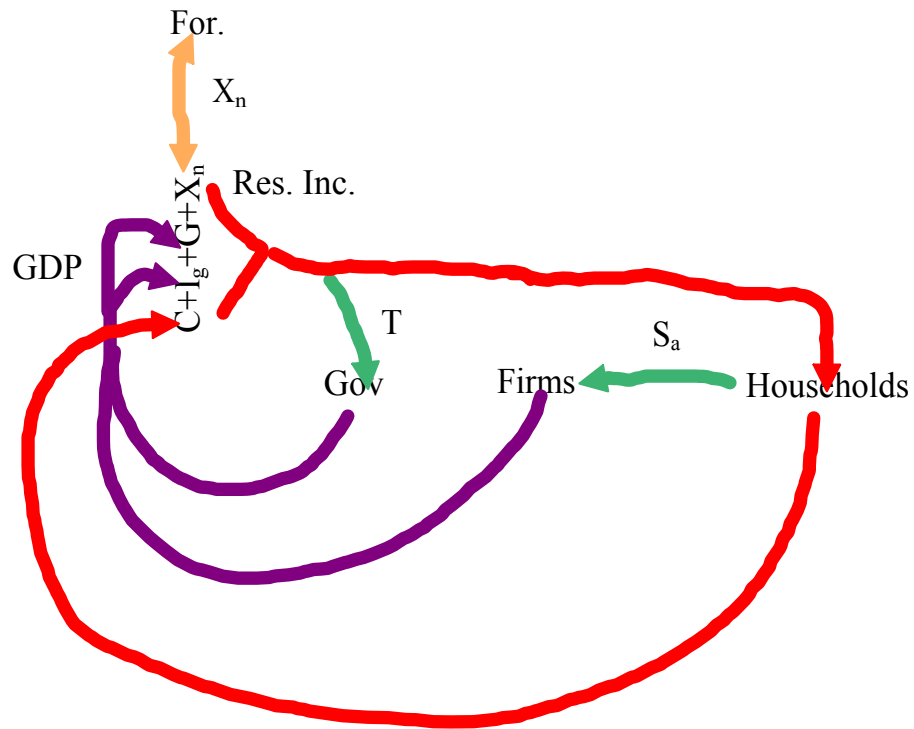
$$\$1,000 * (3/4)/(1-(3/4))$$

$$\$1,000 * 3 = \$3,000$$

Taxes can be an increased or decreased leakage,  
increasing GDP at multiplied values or decreasing GDP at multiplied values.

Government spending is an injection or a leakage,  
increasing GDP at multiplied values or decreasing GDP at multiplied values.

BUT, tax impacts effect the economy at Multiplier -1



$$C + I_g + G + X_n = \text{GDP}$$

$$(\text{Res. Inc.} - T - S_a) + I_g + G + (X - M) = \text{GDP}$$

$$(-T - S_a) + I_g + G + (X - M) = 0$$

$$I_g + G + X = T + S_a + M$$

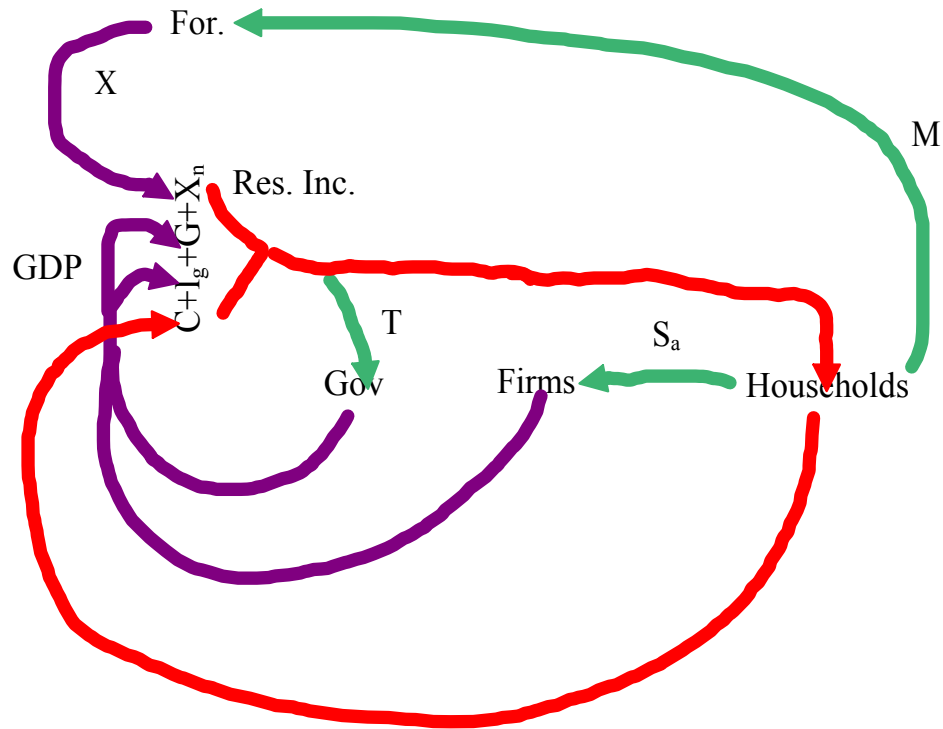
"Injections" "Leakages"

$$I_g + G + X = T + S_a + M$$

If you assume:

$$I_g + G = T + S_a$$

If savings does not support investment, or investment is less than savings, then the government can stabilize by taking up the slack.



The main artery is GDP provides resource income which should turn into C.

Everything else is a leakage or an injection.

$$C + I_g + G + X_n = \text{GDP}$$

$$(\text{Res. Inc.} - T - S_a) + I_g + G + (X - M) = \text{GDP}$$

$$(-T - S_a) + I_g + G + (X - M) = 0$$

$$I_g + G + X = T + S_a + M$$

"Injections"    "Leakages"

$$I_g + G + X = T + S_a + M$$

Equilibrium vs. Full employment

In this model equilibrium is determined by:

Desired level of investment by firms, government injections/leakages, imports and the mechanisms of consumers spending and saving preferences.

No real regard to price or Full employment.

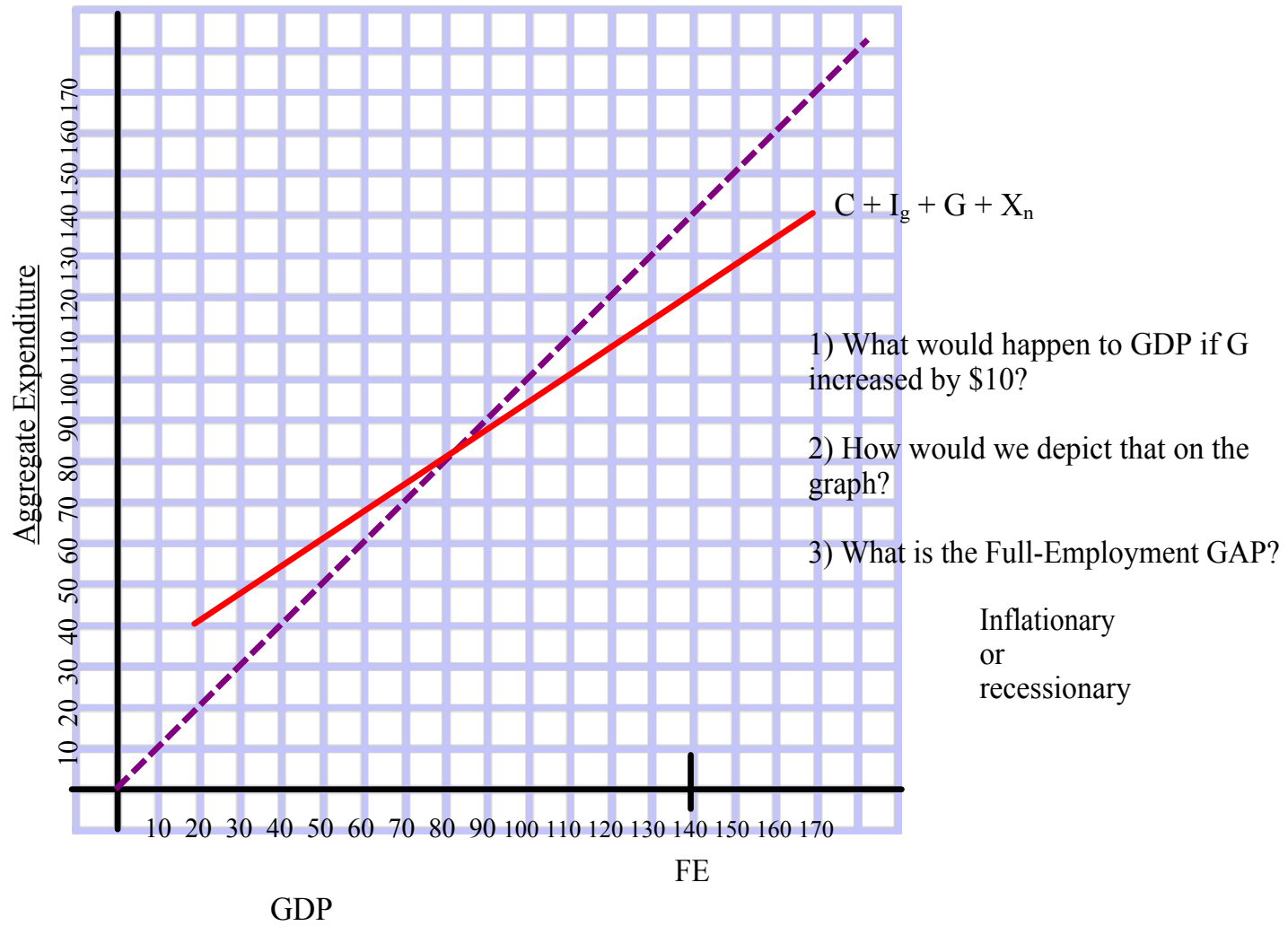
If the economy is equilibrating at somewhere other than full employment then there is a full employment gap.

It can be recessionary or inflationary.

The gap is the amount of an injection or leakage, the amount of extra expenditure required to get to full employment GDP.

(Full employment GDP - Actual GDP)

-----  
Multiplier



Points of value:

- Income = Expenditure
- Multiplier
- Leakages and injections (and multiplication)
- Involuntary disinvestment/investment mechanism
- The actors C, I, G, Foreigners and their leaks/inject.
- S supports I



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(Full employment GDP - Actual GDP)

-----  
Multiplier

Revisit my mispeak:

Slope on both graphs is MPC from which you can get the multiplier.

The Economy is at equilibrium at \$420 billion dollars.

$MPS = .1$

The full employment GDP is \$520.

What is the GDP gap?

Firms have unintended or planned investment

Trying to produce too little will result in unplanned disinvestment (inventories run down)

IF THEY WANT TO KEEP UP THEIR LEVEL OF INVESTMENT UP, they must produce more and end up back at the equilibrium level.

How much more?

They don't know because they will find it when disinvestment stops.

Sequence of events:

- 1) Firms choose product level and borrow to support a certain  $I_g$
- 2) That determines Resource income and  $DI$ .
- 3) Consumers decide their  $C$  and  $S$  choices
- 4) If firms made too little to support  $C$ , then customers take the extra out of inventory.
- 5) Inventories are lower than firms want, they replace.
- 6) This increases Resource income, which increase  $C$  and  $S$
- 7) Changes keep happening until
  - Inventories are what firms want.
  - They are borrowing the right amount for year to support  $I_g$

:

Goods wanted  $\Rightarrow DI = C_d + S_d$

Income generated by production  $GDP = C_p + I_p$

Stable when  $C + S = C + I$ ,  $S = I$