

1)  $x^2 + 1 + \frac{2}{x-3}$

2) quotient?  $x^2 + 1$  remainder?  $2$

3)  $f(3) = 2$

4)  $f(c)=r(c)$  if  $f(x)$  is divisible by  $(x-c)$

5)  $F(1)=3*1^5-2*1^4+7*1-5=3$  so the remainder = 3

$$(3x^4 + x^3 + x^2 + x + 8 + \frac{3}{x-1})$$

6)  $(-2)^3+2*(-2)^2+4*-2+8=0$

$$(x^2 + 4 + \frac{0}{x+2} \Rightarrow r(x)=0)$$

7) There is none.

8) Is  $(x - 2)$  a factor of  $f(x) = 2x^3 - 5x^2 - 4x + 12$ ?

$$2*2^3-5*2^2-4*2+12=0$$

$$(2x^2 - x - 6 + \frac{0}{x-2})$$

9)  $(2x + 3)(x - 2)^2$

10)  $(-2)^3+10*(-2)^2+31*(-2)+30=0$

$$x^2 + 8x + 15 + \frac{0}{x+2}$$

$$(x + 5)(x + 3)(x + 2)$$

11)  $\pm 20, 10, 5, 4, 2, 1$

$$(x - 1)(x^2 + 9x + 20) = (x - 1)(x + 4)(x + 5)$$

12)  $\pm 8, 4, 2, 1$

$$(x + 1)(x^3 - 2x^2 - 4x + 8) = (x + 1)(x - 2)(x^2 - 4) = (x + 1)(x - 2)^2(x + 2)$$

12)  $F(-1)=1-8-1+2=-6$ ;  $f(0)=2$ ; sign changes, it must cross the x-axis

13) Show that the equation  $x^3 + x^2 - 3 = 0$  has no rational roots, but that it does have an irrational root between  $x=1$  and  $x=2$ .

The possible rational roots are  $\pm 3, 1$ .  $f(3) \neq 0$ ,  $f(-3) \neq 0$ ,  $f(1) \neq 0$ ,  $f(-1) \neq 0$

$F(1)=-1$ ;  $f(2)=9$ ; sign changes, it must cross the x-axis