

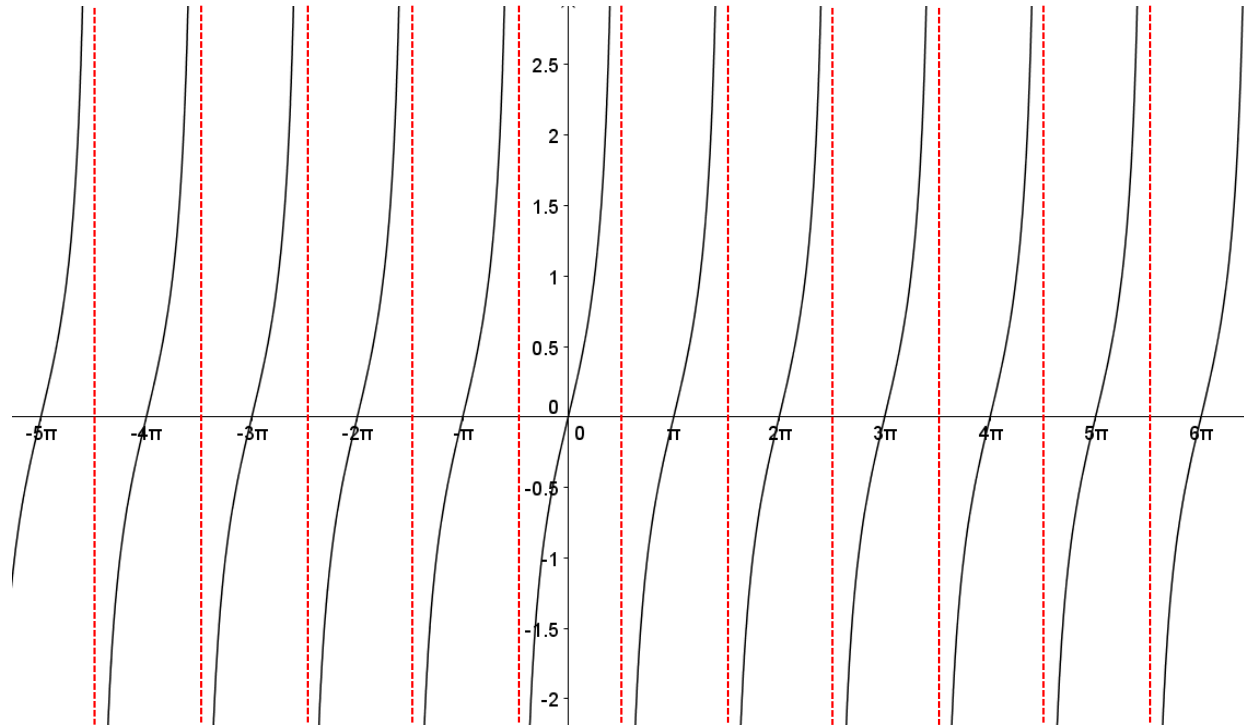
Know table of properties for six functions

Draw sin, cos for a transformed function with any combination of constants.

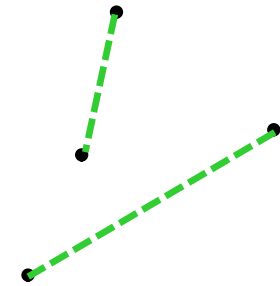
Write functions from pictures for sin, cos

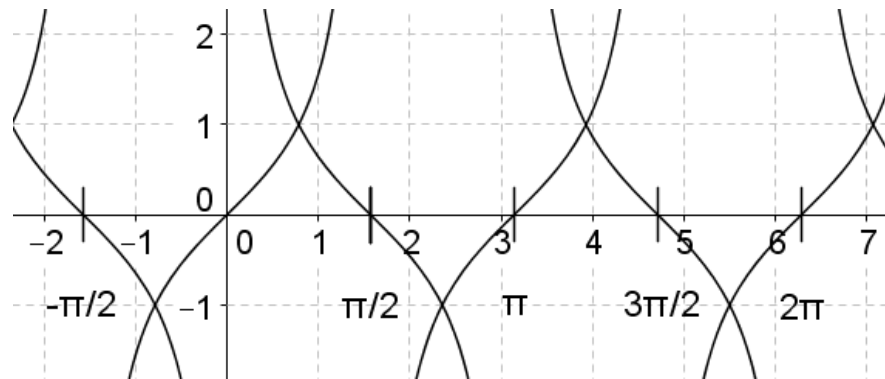
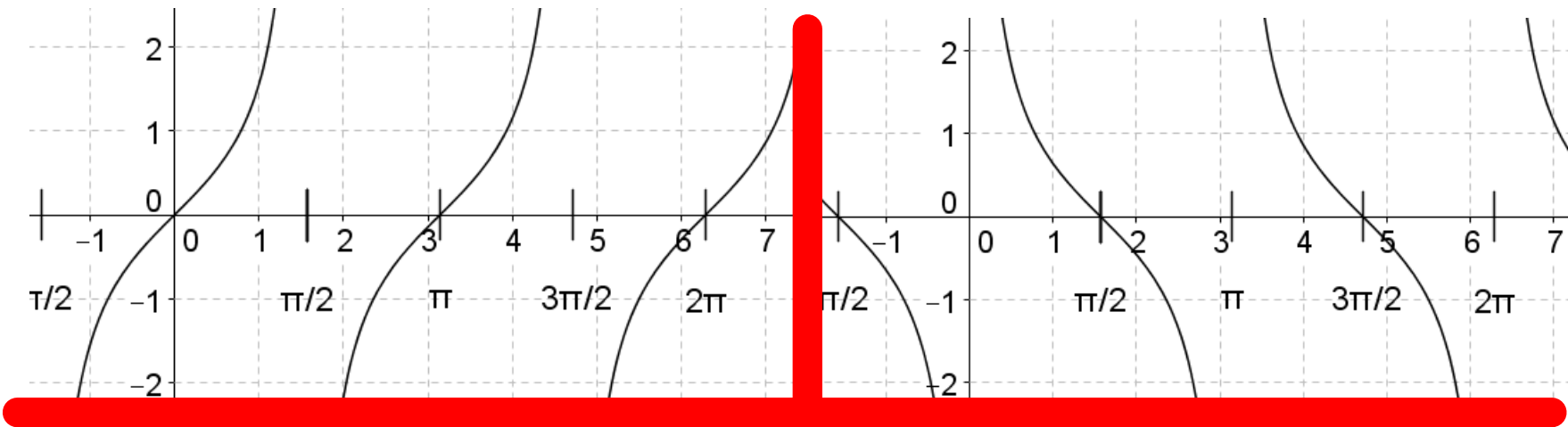
- Which ever you are told, or both.
- Any combination of constants

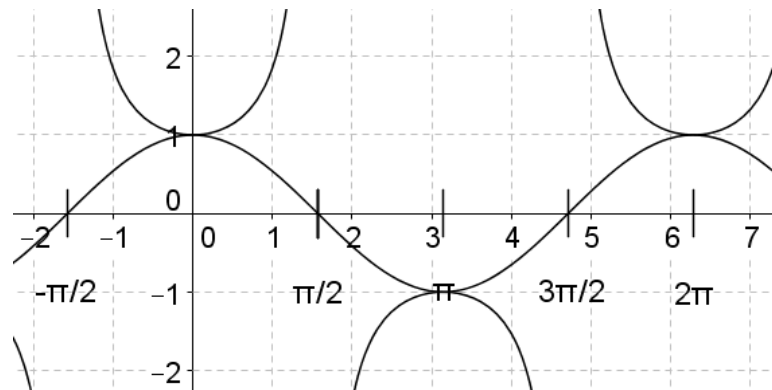
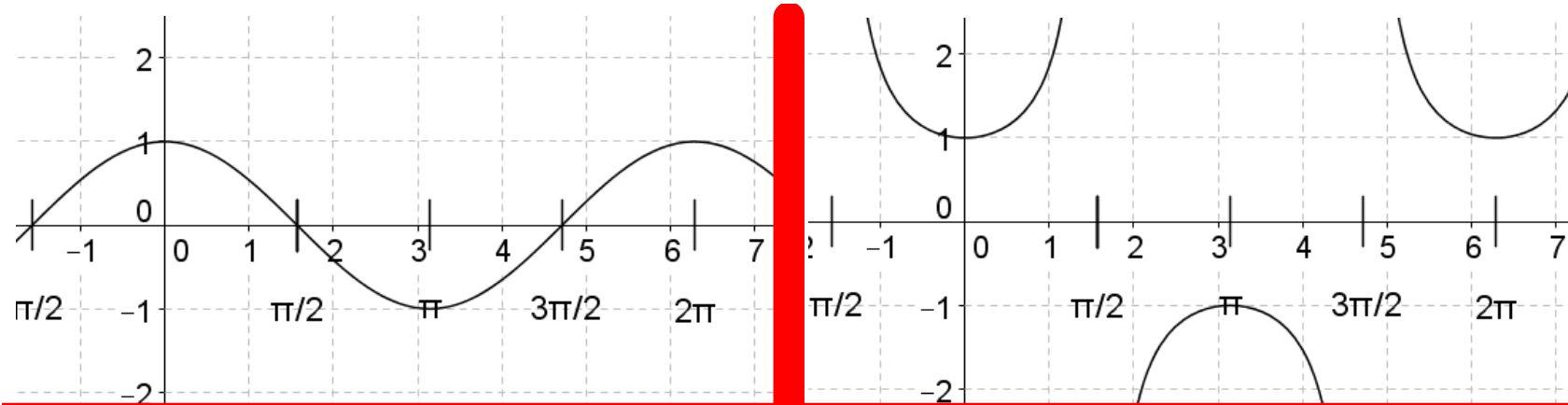
Draw tan, cot, sec, and csc with one or two transformations (never both horizontals)

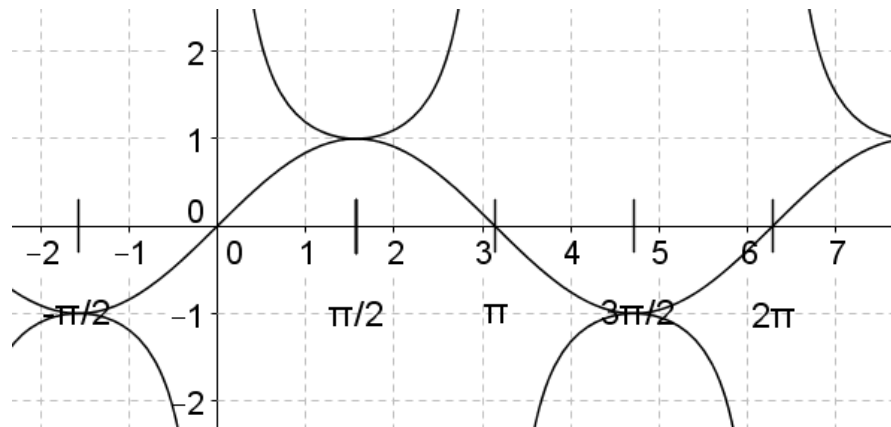
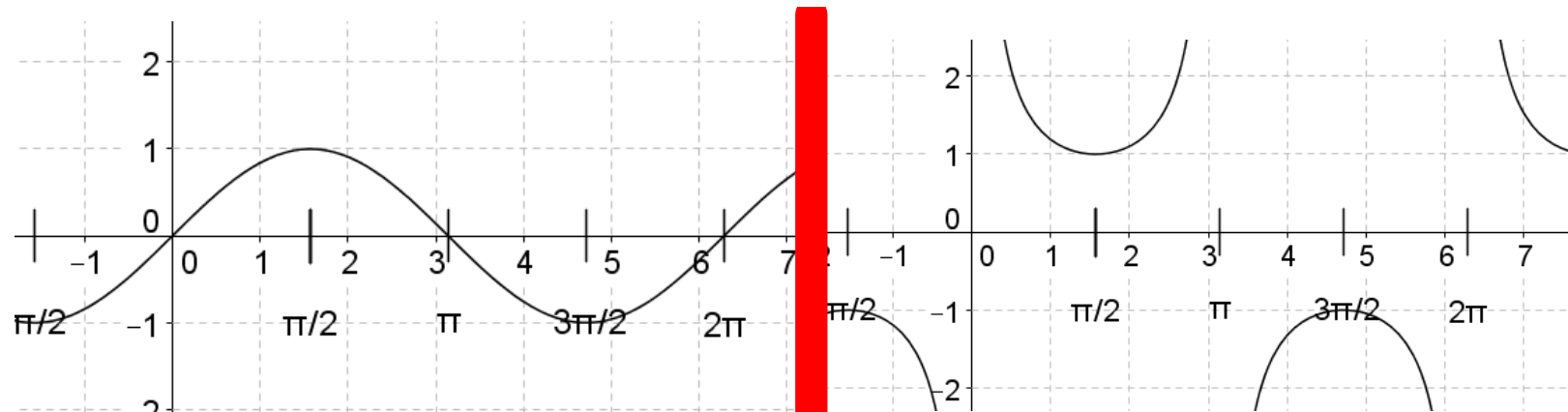


- Domain
- Range
- Odd or Even?
- Period?
- X intercepts?
- Y intercepts?
- Vertical asymptotes?









### *Properties of the Tangent Function*

1. The domain is the set of all real numbers, except odd multiples of  $\frac{\pi}{2}$ .
2. The range consists of all real numbers.
3. The tangent function is an odd function, as the symmetry of the graph with respect to the origin indicates.
4. The tangent function is periodic, with period  $\pi$ .
5. The  $x$ -intercepts are  $\dots, -2\pi, -\pi, 0, \pi, 2\pi, 3\pi, \dots$ ; the  $y$ -intercept is 0.
6. Vertical asymptotes occur at  $x = \dots, -\frac{3\pi}{2}, -\frac{\pi}{2}, \frac{\pi}{2}, \frac{3\pi}{2}, \dots$

Showing a transformation of tan, cotan, csc, sec.

$$y = A \tan(\omega x + \phi) + B$$

$$4 \tan(2x) \qquad y = A \sin\left(\omega \left(x + \frac{\phi}{\omega}\right)\right) + B$$

Show the 2 by:

- figuring out the new period  $\frac{\text{base period}}{\omega} = \text{new period} = \frac{\pi}{2}$

- plot new x intercepts and asymptotes.

- Asymptotes were every  $(\pi/2) + \pi x$  Now:  $(\pi/4) + (\pi/2) * x$

- X intercepts were  $\pi x$  now  $(\pi/2)x$

Show the 4 by taking the point  $(\pi/4, 1)$  and making it  $(\pi/8, 4)$

$(\pi/4, 1) \Rightarrow ((\pi/4)/2, 1*4) \Rightarrow (\pi/8, 4)$

$\csc(2x)$

