

$$\cos(2\theta) = \cos^2 \theta - \sin^2 \theta$$

$$\cos(2\theta) = 1 - 2\sin^2 \theta$$

$$\cos(2\theta) = 2\cos^2 \theta - 1$$

$$\sin(2\theta) = 2\sin \theta \cos \theta$$

$$\tan(2\theta) = \frac{2\tan \theta}{1 - 2\tan \theta}$$

Derivation page 1 how double ange formulas come from sum/difference formulas
(something you could do):

$$\cos(\theta + \theta) = \cos(2\theta) = \cos\theta\cos\theta - \sin\theta\sin\theta = \cos^2\theta - \sin^2\theta$$

$$\cos^2 - \sin^2 \theta = 1 - \sin^2 \theta - \sin^2 \theta = 1 - 2\sin^2 \theta$$

$$\cos^2 - \sin^2 \theta = \cos^2 \theta - (1 - \cos^2 \theta) = 2\cos^2 \theta - 1$$

$$\sin(\theta + \theta) = \sin(2\theta) = \sin\theta\cos\theta + \cos\theta\sin\theta = 2\sin\theta\cos\theta$$

$$\tan(\theta + \theta) = \tan(2\theta) = \frac{\tan\theta + \tan\theta}{1 - \tan\theta\tan\theta} = \frac{2\tan\theta}{1 - 2\tan\theta}$$

Find $\sin(2\theta)$

$$\sin \theta = -\frac{\sqrt{3}}{3}, \quad \frac{3\pi}{2} < \theta < 2\pi$$

- Recognize the patterns of the formulas
- Use the substitution trick:

$$A=2\theta$$