

1) Find the area of $\triangle ABC$ if $a = 16$, $b = 25$, and $\angle C = 52^\circ$.

$$A = .5 * a * b * \sin C$$

$$A = .5 * 16 * 25 * \sin 52$$

$$A = 157.60 \text{ u}^2$$

2) The area of $\triangle ABC$ is 15. If $a = 12 \text{ cm}$, $b = 5 \text{ cm}$, find the measure of $\angle C$.

$$A = .5 * a * b * \sin C$$

$$15 = .5 * 12 * 5 * \sin C$$

$$A = 30^\circ$$

3) Find the area of a regular 12-sided polygon inscribed in a circle of radius 8 cm.

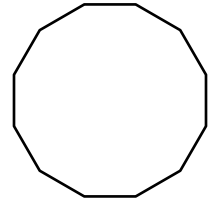
$$360^\circ / 12 = 30^\circ, 180^\circ - 30^\circ = 150^\circ / 2 = 75^\circ \Rightarrow \text{vertex} = 30^\circ$$

$$A = .5 * a * b * \sin C$$

$$A = .5 * 8 * 8 * \sin 30$$

$$A = 16 \text{ cm}^2 \text{ for each triangle}$$

$$16 * 12 = 192 \text{ cm}^2$$

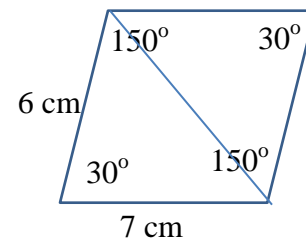


4) Adjacent sides of a parallelogram have lengths 6 cm and 7 cm, and the measure of the included angle is 30° . Find the area of the parallelogram.

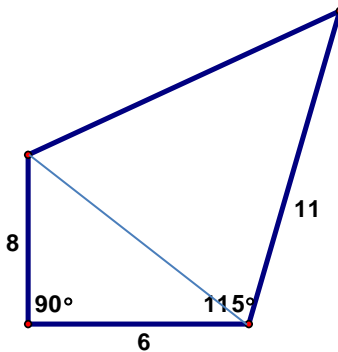
$$A = .5 * 7 * 6 * \sin 30^\circ$$

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$$A = 10.5 \text{ cm}^2 * 2 = 21 \text{ cm}^2$$



5) Find the area of the quadrilateral below to the nearest square unit.



$$A = .5 * 8 * 6$$

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$$A = 24 \text{ cm}^2, \text{ Diagonal} = 10$$

$$\tan^{-1}(8/6) = 53.1302^\circ$$

$$\text{Triangle angles} = 90^\circ, 53.1302^\circ, 36.8699^\circ$$

$$115^\circ - 53.1302^\circ = 61.8699^\circ$$

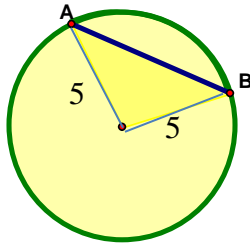
$$A = .5 * 10 * 11 * \sin(61.8699^\circ)$$

$$A = 48.5034 \text{ u}^2$$

$$24 + 48.5034 = 72.5034 \text{ u}^2$$

- 5) Find the area of a segment of a circle of radius 5 if the measure of the central angle of the segment is 2 radians.

$$A = \frac{1}{2} r^2 \cdot \theta$$



$$A = .5 * a * b * \sin C$$

$$A = .5 * 5 * 5 * \sin 2$$

$$A = 11.3662 \text{ u}^2$$

$$\frac{2}{2\pi} * \pi 5^2 = 25 \text{ u}^2$$

$$25 - 11.3662 = 13.6338 \text{ u}^2$$

- 6) Find the area of the segment formed by a chord 24 cm long in a circle of radius 13 cm.

$$A = \sqrt{s(s-a)(s-b)(s-c)}$$

$$(24 + 13 + 13)$$

$$s = \frac{2}{2} = 25$$

$$A = \sqrt{25(25-24)(25-13)(25-13)} = 60 \text{ cm}^2$$

$$24^2 = 13^2 + 13^2 - 2abc \cos(x)$$

$$X = 134.7603^\circ$$

$$\frac{134.7603}{360} * \pi 13^2 = 198.7449 \text{ cm}^2$$

$$198.7449 - 60 = 138.7449 \text{ cm}^2$$

- 7) Find the area of the Bermuda Triangle, if the sides have the approximate lengths 850 miles, 925 miles, and 1300 miles.

$$A = \sqrt{s(s-a)(s-b)(s-c)}$$

$$(850 + 925 + 1300)$$

$$s = \frac{2}{2} = 1537.5$$

A

$$= \sqrt{1537.5(1537.5-850)(1537.5-925)(1537.5-1300)}$$

$$= 392128.824 \text{ miles}^2$$

- 8) Find the area of a triangle in a rectangular coordinate plane whose vertices are (0,0), (3,4) and (-8,6) using Heron's area formula.

$$A(0,0) \text{ to } B(3,4) = 5$$

$$A \text{ to } C = 10$$

$$B \text{ to } C = 5\sqrt{5}$$

$$A = \sqrt{s(s-a)(s-b)(s-c)}$$

$$(5\sqrt{5} + 5 + 10)$$

$$s = \frac{2}{2} = 13.0902$$

$$A = \sqrt{13.0902(13.0902 - 5\sqrt{5})(13.0902 - 5)(13.0902 - 10)} = 25 \text{ u}^2$$