

1) 8th term is 4; 18th term is -96. Find the sum of the first 30 terms.

$$\frac{(-96-4)}{(18-8)} = -10 = d$$

$$a_n = a + d(n-1), a_8 = a + d(8-1), 4 = a - 10 * (8-1), 74 = a$$

$$a_{30} = 74 + (-10)(30-1) = -216$$

$$S_n = \frac{n}{2}(a + a_n) = S_{30} = \frac{30}{2}(74 - 216) = -2130$$

Find the sum of the following series:

2) 1+3+5+ ... +59

$$a=1, d=2$$

$$a_n = a + d(n-1), 59 = 1 + 2(n-1), n = 30$$

$$S_n = \frac{n}{2}(a + a_n), S_{30} = \frac{30}{2}(1 + 59) = 900$$

$$3) \frac{1}{16} + \frac{3}{64} + \frac{9}{256} + \dots + \frac{6561}{1048576}$$

$$a = \frac{1}{16}, d = \frac{\left(\frac{3}{4}\right)}{\left(\frac{1}{16}\right)} = \frac{3}{4}$$

$$a_n = a * r^{(n-1)} = \frac{1}{16} * \left(\frac{3}{4}\right)^{(n-1)} * \frac{\left(\frac{6561}{1048576}\right)}{\left(\frac{1}{16}\right)} = \left(\frac{3}{4}\right)^{(n-1)} * \frac{\ln\left(\frac{6561}{65536}\right)}{\ln\left(\frac{3}{4}\right)} = n - 1, n = 9$$

$$S_n = a \left(\frac{1-r^n}{1-r}\right), S_{59} = \frac{1}{16} * \left(\frac{1-\left(\frac{3}{4}\right)^9}{1-\frac{3}{4}}\right) = .23123$$

$$4) \sum_{k=1}^{\infty} 8\left(\frac{2}{3}\right)^{k-1}$$

$$S = \frac{a}{1-r} = \frac{8}{1-\frac{2}{3}} = 24$$