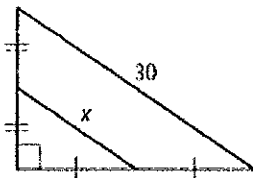
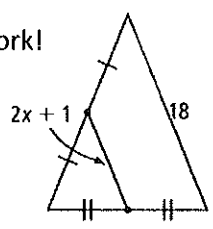
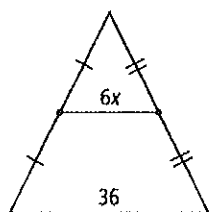
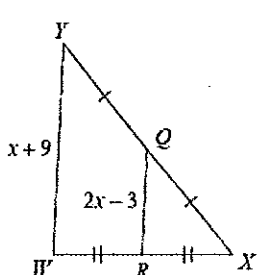


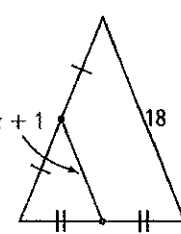
1 Find the value of x.

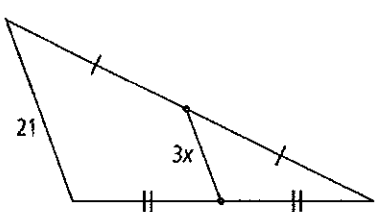
1)   $x = 15$

2) show work!   $2(2x + 1) = 18$   
 $x = 4$

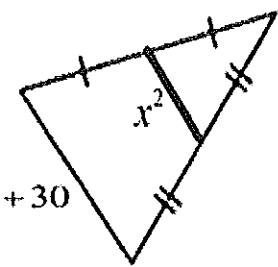
3.   $2(6x) = 36$   
 $x = 3$

4.   $2(2x - 3) = x + 9$   
 $x = 15$

5.   $2(2x + 1) = 18$   
 $x = 4$

6.   $2(3x) = 21$   
 $x = 3.5$

✓ Solve for x.



$2x^2 = -7x + 30$   
 $2x^2 + 7x - 30 = 0$   
 $(2x - 5)(x + 6) = 0$   
 $x = -6, 5/2$

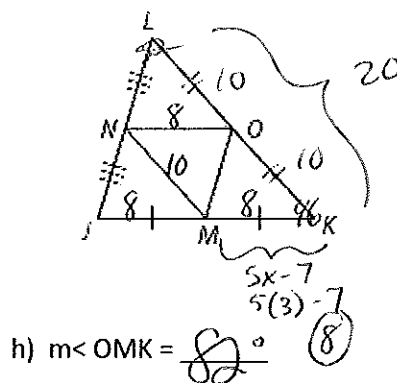
→ Use the diagram to the right and the following information...

LK =  $12x - 16$  cm, NM =  $3x + 1$ , MK =  $5x - 7$ , NO =  $2y$ ,  $m\angle L = 52^\circ$ ,  $m\angle K = 46^\circ$

a)  $x = 3$   $2(3x + 1) = 12x - 16$   
 $(3x + 1) = 12x - 16$  b)  $OK = 10$

c)  $MK = 8$   $18 = 6x$   
 $x = 3$  d)  $y = 4$  e)  $JK = 16$   
 $2y = 8$

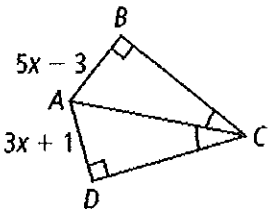
f)  $m\angle J = 82^\circ$  g)  $m\angle LNO = 82^\circ$



h)  $m\angle OMK = 82^\circ$

5.2

7) Solve for x.



$$5x - 3 = 3x + 1$$

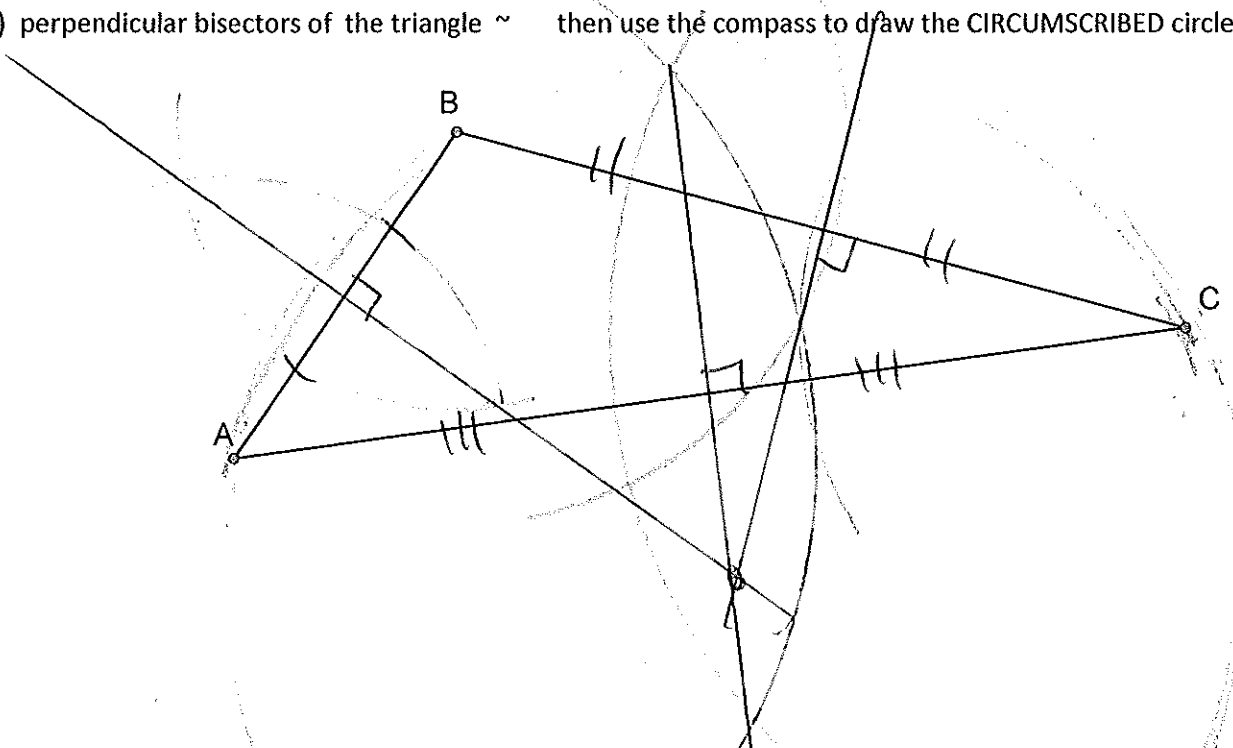
$$2x = 4$$

$$x = 2$$

$$x = \underline{2}$$

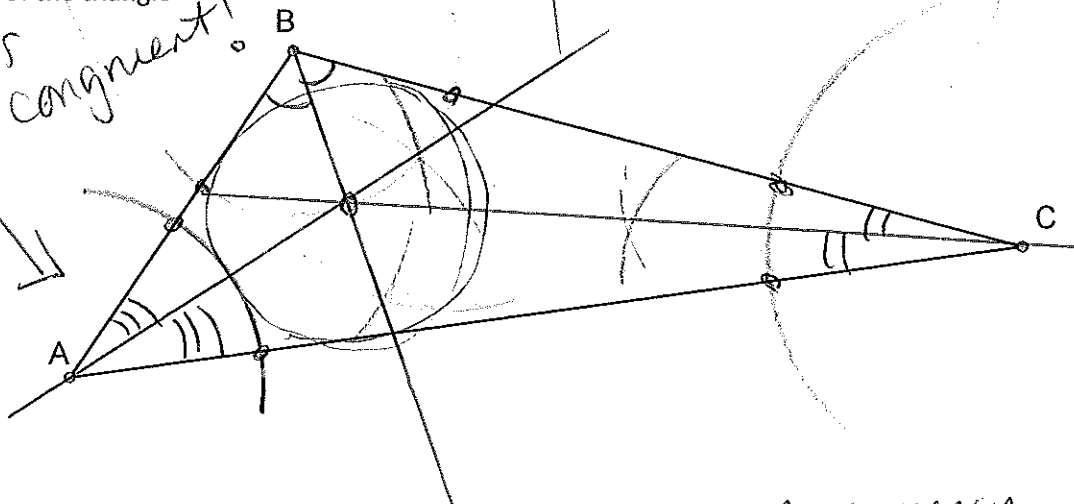
5.3 Use a compass to construct and label the following; **LABEL diagrams with appropriate congruent markings and/or perpendicular markings.**

8) perpendicular bisectors of the triangle ~ then use the compass to draw the CIRCUMSCRIBED circle of ABC



9) angle bisectors of the triangle

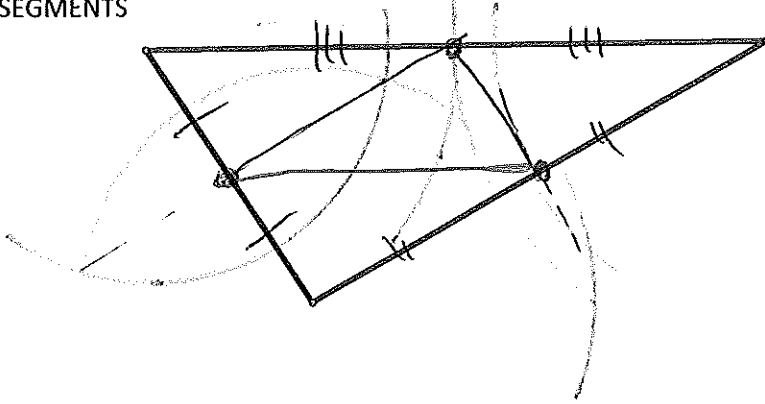
*mark  $\angle$ 's congruent!*



10. When the 3 bisectors all intersect at one point, that point is called a point of concurrency.

(still using a compass...)

11. MIDSEGMENTS



\* Find midpoint of each side

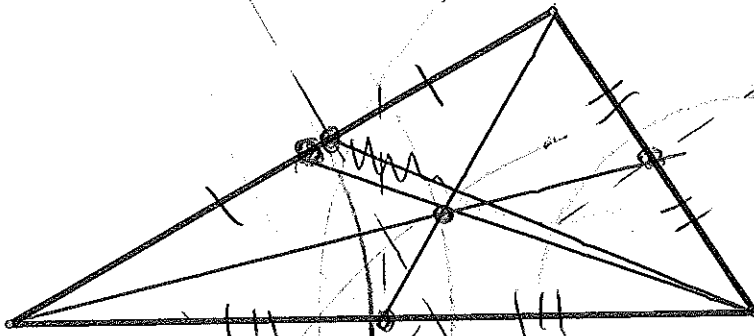
for both



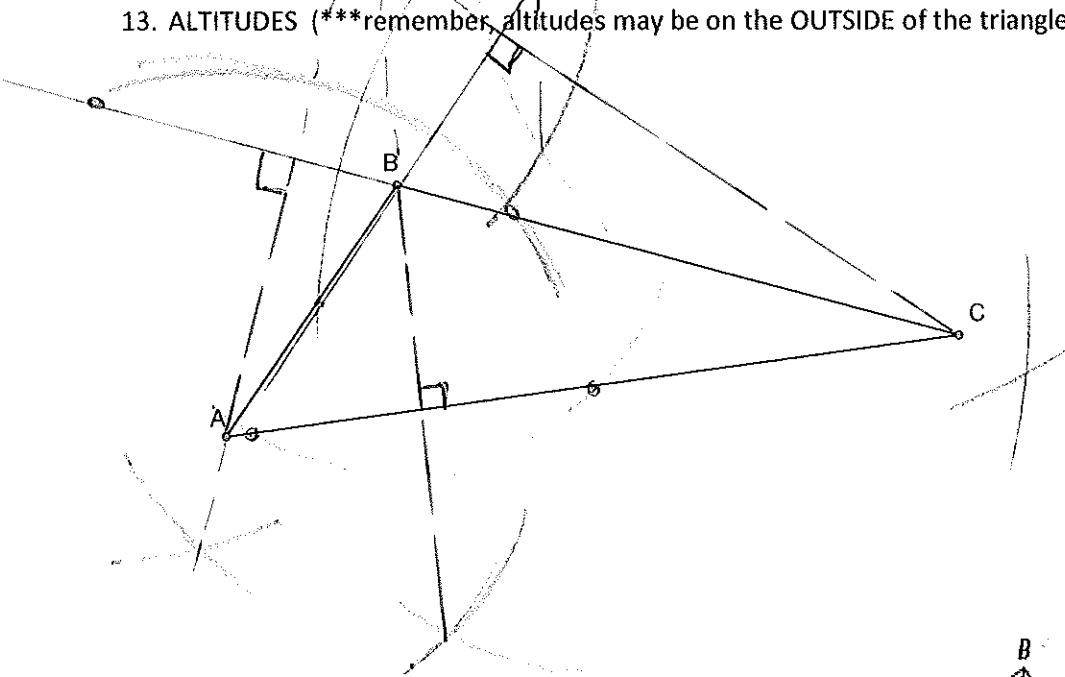
connect vertex to midpt



12. MEDIANS



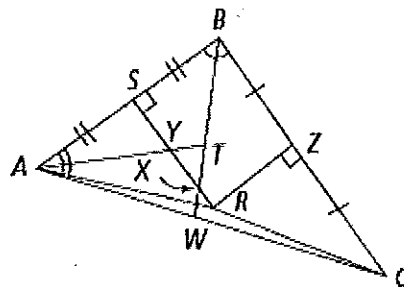
13. ALTITUDES (\*\*remember, altitudes may be on the OUTSIDE of the triangle!)



Use the diagram to the right...

14) Name a perpendicular bisector  $\overline{RZ}$  or  $\overline{YS}$

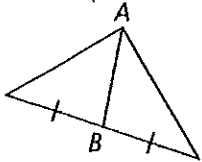
15) Name an angle bisector  $\overline{WB}$  or  $\overline{TA}$



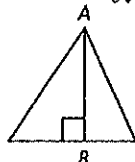
16) To find the point that is equidistant from the 3 vertices of the triangle, you would find the point where the 3 perpendicular bisectors intersect.

Is  $\overline{AB}$  a median, an altitude, a perpendicular bisector, angle bisector or none of these? How do you know?

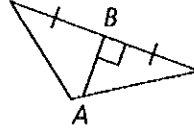
17. median



18. altitude

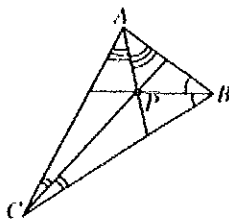


19. perp. bisector

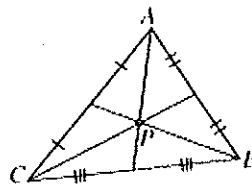


20. Which diagram shows a point P an equal distance from points A, B, and C?

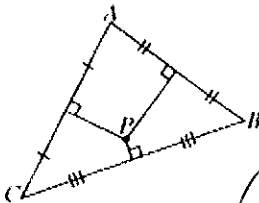
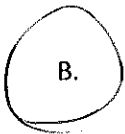
A.



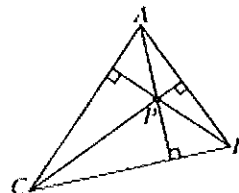
C.



B.



D.

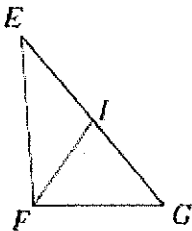


B  
+ bisectors

21) In each diagram, the segments drawn are **MEDIANS** of the triangle.

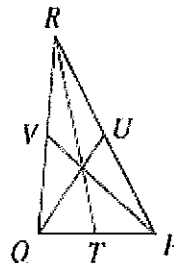
a) If  $GE = 3x + 5$ , and  $GI = 2x - 1$

b)  $QV = 32x - 12$ , and  $RV = 21x + 10$



$$3x + 5 = 2(2x - 1)$$

$x = \underline{7}$   $GI = \underline{13}$   $GE = \underline{26}$



$$32x - 12 = 2(21x + 10)$$

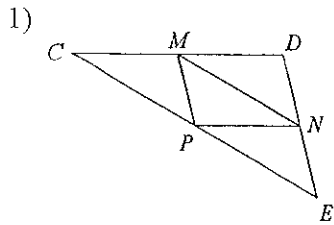
$x = \underline{2}$   $QV = \underline{52}$   $RV = \underline{52}$

22) Explain the similarities and differences between an triangle's altitude and median.

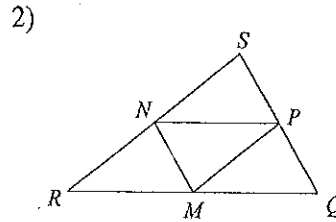
Altitudes are  $\perp$  to oppos. side, while medians go through midpt. of oppos. side,  
But both start at a vertex of the  $\Delta$ .

### Midsegment of a Triangle

In each triangle, M, N, and P are the midpoints of the sides. Name a segment parallel to the one given.



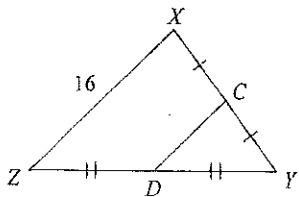
$\overline{CD} \parallel \overline{PN}$



$\overline{MN} \parallel \overline{QS}$

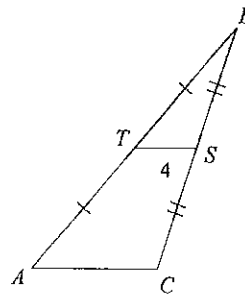
Find the missing length indicated.

3) Find  $CD$



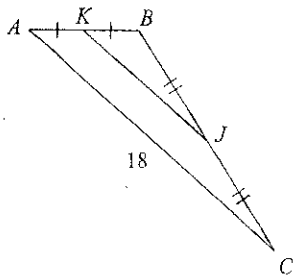
$CD = 8$

4) Find  $AC$



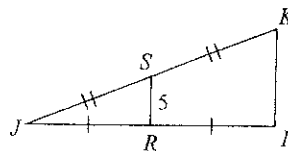
$AC = 8$

5) Find  $KJ$



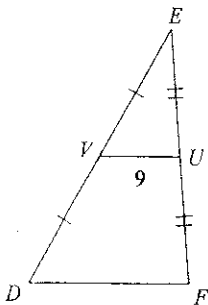
$KJ = 9$

6) Find  $IK$



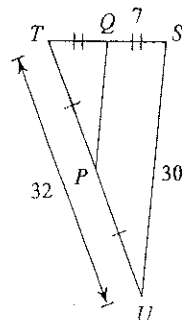
$IK = 10$

7) Find  $DF$



$DF = 18$

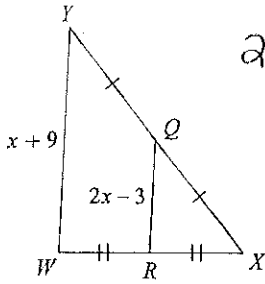
8) Find  $PQ$



$PQ = 15$

Solve for x.

9)



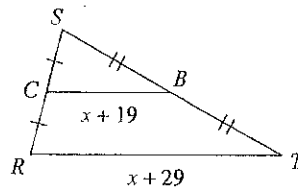
$$2(2x-3) = x+9$$

$$4x-6 = x+9$$

$$3x = 15$$

$$x = 5$$

10)

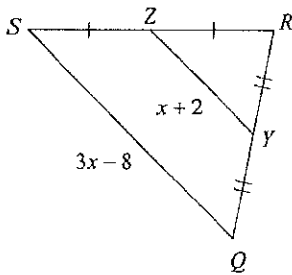


$$2(x+19) = x+29$$

$$2x+38 = x+29$$

$$x = -9$$

11)

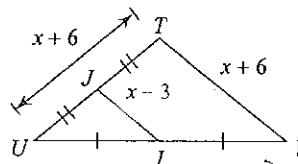


$$2(x+2) = 3x-8$$

$$2x+4 = 3x-8$$

$$12 = x$$

12)



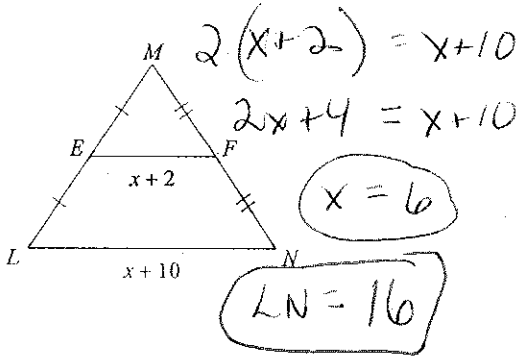
$$2(x-3) = x+6$$

$$2x-6 = x+6$$

$$x = 12$$

Find the missing length indicated.

13) Find LN



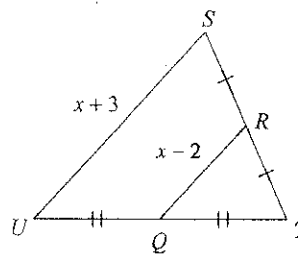
$$2(x+2) = x+10$$

$$2x+4 = x+10$$

$$x = 6$$

$$LN = 16$$

14) Find RQ



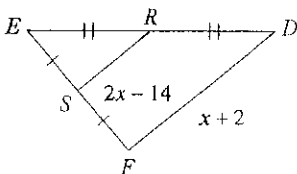
$$2(x-2) = x+3$$

$$2x-4 = x+3$$

$$x = 7$$

$$RQ = 7-2 = 5$$

15) Find SR



$$2(2x-14) = x+2$$

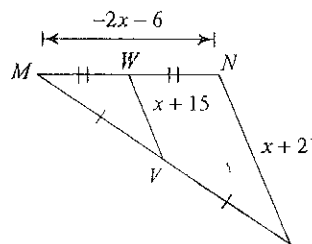
$$4x-28 = x+2$$

$$3x = 30$$

$$x = 10$$

$$SR = 2(10) - 14 = 6$$

16) Find VW



$$2(x+15) = x+21$$

$$2x+30 = x+21$$

$$x = -9$$

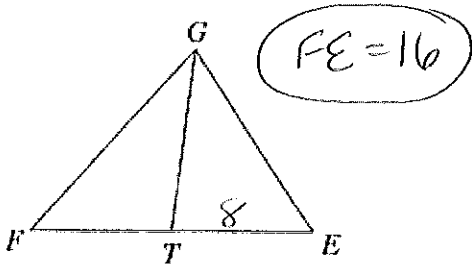
$$VW = 6$$

Practice using **MEDIANS** and **ANGLE BISECTORS** of **TRIANGLES**

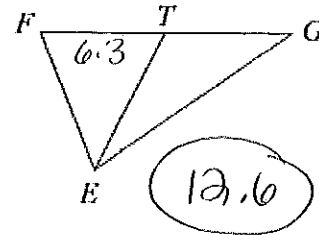
Name ANSWERS

Each figure shows a triangle with one or more of its medians.

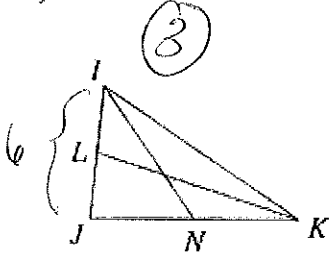
1) Find  $FE$  if  $TE = 8$



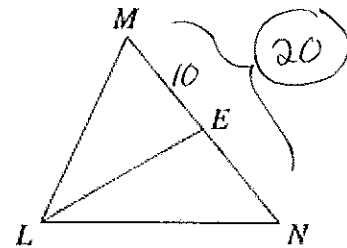
2) Find  $GF$  if  $TF = 6.3$



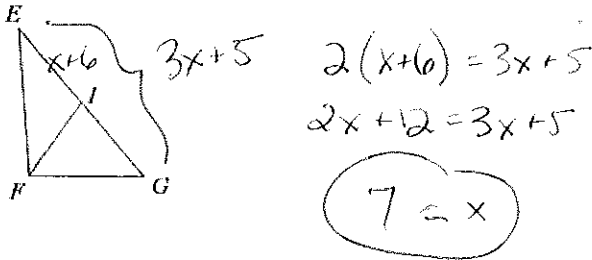
3) Find  $LJ$  if  $IJ = 6$



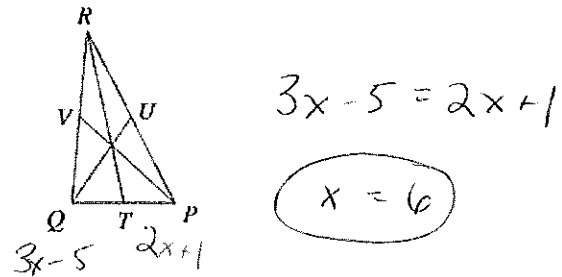
4) Find  $NM$  if  $EM = 10$



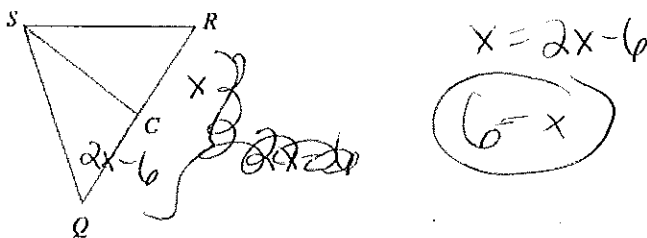
11) Find  $x$  if  $GE = 3x + 5$  and  $IE = x + 6$



12) Find  $x$  if  $TP = 2x + 1$  and  $TQ = 3x - 5$

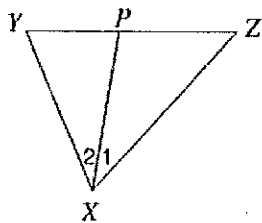


15) Find  $CQ$  if  $CR = x$  and  $CQ = 2x - 6$



Each figure shows a triangle with one of its angle bisectors.

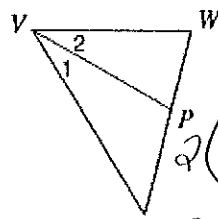
- 13) Find  $x$  if  $m\angle 2 = 4x + 5$  and  $m\angle 1 = 5x - 2$ .



$$4x + 5 = 5x - 2$$

$$7 = x$$

- 14) Find  $x$  if  $m\angle 2 = 1 + 28x$  and  $m\angle XVW = 59x - 1$ .



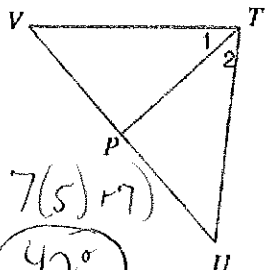
$$2(1 + 28x) = 59x - 1$$

$$2 + 56x = 59x - 1$$

$$x = 1$$

$$3 = 3x$$

- 15)  $m\angle 1 = 7x + 7$  and  $m\angle VTU = 16x + 4$ . Find  $m\angle 1$ .



$$2(7x + 7) = 16x + 4$$

$$14x + 14 = 16x + 4$$

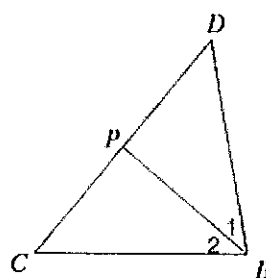
$$10 = 2x$$

$$m\angle 1 = 7(5) + 7$$

$$42^\circ$$

$$x = 5$$

- 16) Find  $m\angle 2$  if  $m\angle 2 = 7x + 5$  and  $m\angle 1 = 9x - 5$ .



$$7x + 5 = 9x - 5$$

$$10 = 2x$$

$$x = 5$$

$$m\angle 2 = 7(5) + 5$$

$$40^\circ$$

- 17) use a compass and straightedge for the following. If you don't have one, then just sketch and mark your diagram appropriately to show how you found the point that is equidistant from all of the schools.

Warde, Ludlowe, and Staples are playing in a tournament. The one requirement is that the tournament must be at a site that is equidistant from all schools. find the point on the map in which the event should be held.

Show all work!

Use the black dots as the school locations...

