

Name _____

ANSWERS

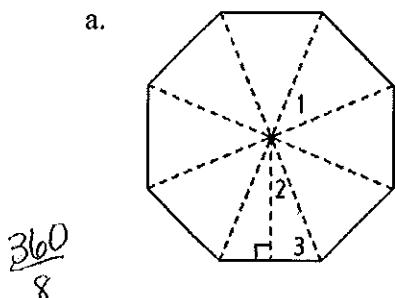
Period _____

Date _____

Geometry 22: 10.3 – Area of Regular Polygons Practice

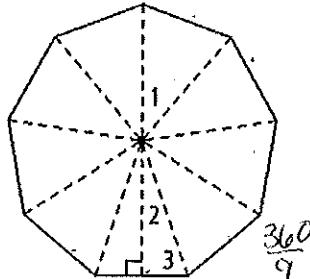
1. Each regular polygon has radii and apothem as shown. Find the measure of each numbered angle.

a.



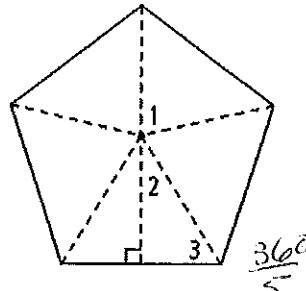
$$\frac{360}{8}$$

b.



$$\frac{360}{9}$$

c.



$$\frac{360}{5}$$

$$m\angle 1 = 45^\circ \quad m\angle 2 = 22.5^\circ \quad m\angle 3 = 67.5^\circ \quad m\angle 1 = 40^\circ \quad m\angle 2 = 20^\circ \quad m\angle 3 = 70^\circ \quad m\angle 1 = 72^\circ \quad m\angle 2 = 36^\circ \quad m\angle 3 = 54^\circ$$

2. Find the area of each regular polygon with the given apothem a and side length s .

- a. pentagon, $a = 4.9$ in., $s = 7.1$ in.

$$A = \frac{1}{2}ap \quad P = 7.1(5)$$

$$A = \frac{1}{2}(4.9)(35.5) \quad [86.975]_2$$

- c. dodecagon, $a = 40.6$ m, $s = 21.7$ m

$$P = (12)(21.7) \quad A = \frac{1}{2}(40.6)(260.4)$$

$$[5286.12]_2$$

- b. hexagon, $a = 12.1$ ft, $s = 14$ ft

$$A = \frac{1}{2}(12.1)(84)$$

$$P = 14(6)$$

$$[508.2]_2$$

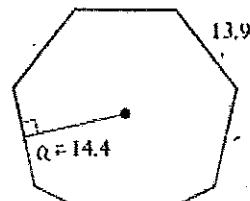
- d. nonagon, $a = 50.9$ m, $s = 37$ m

$$A = \frac{1}{2}(50.9)(333)$$

$$P = 9(37)$$

$$[8474.85]_2$$

e.

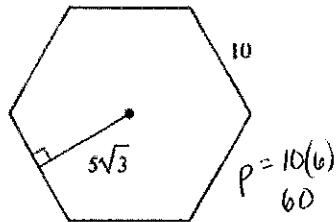


$$P = 13.9(7)$$

$$A = \frac{1}{2}(14.4)(97.3)$$

$$[700.56]_2$$

f.



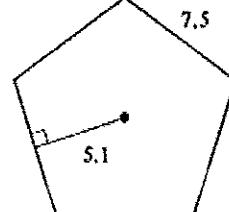
$$P = 10(6)$$

$$A = \frac{1}{2}(5\sqrt{3})(60)$$

$$A = 150\sqrt{3}$$

$$\text{or } (259.81)$$

g.



$$P = 7.5(5)$$

$$A = \frac{1}{2}(5.1)(37.5)$$

$$[95.625]$$

3. Find the approximate perimeter of a regular polygon if $a = 9$ m and $A = 259.2$ m².

$$A = \frac{1}{2}ap$$

$$259.2 = \frac{1}{2}(9)p$$

$$259.2 = 4.5p$$

$$P = 57.6 \text{ m}$$

4. Find the length of each side of a regular n-gon if $a = 80$ feet, $n = 20$, and $A = 20,000$ square feet.

$$A = \frac{1}{2}ap$$

$$20,000 = \frac{1}{2}(80)p$$

$$20,000 = 40p$$

$$500 = p$$

$$\text{perimeter} = \frac{500}{20 \text{ sides}}$$

$$= [25 \text{ ft each side}]$$

- 8
 5. A stop sign is a regular octagon. Each side of the sign is 12.6 in. long. The area of the stop sign is 770 in.².
 What is the length of the apothem to the nearest whole number?

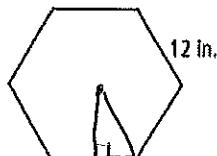
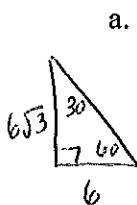
$$P = 8(12.6) \\ 100.8$$

$$A = \frac{1}{2}(a)P \\ 770 = \frac{1}{2}a(100.8)$$

$$770 = 50.4a$$

$$a = 15.27 \approx 15 \text{ in}$$

6. Find the area of each regular polygon. Round your answer to the nearest tenth.



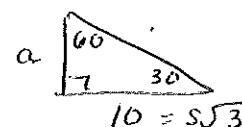
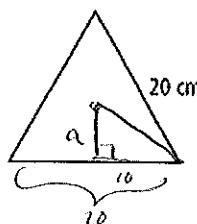
$$P = 12(6) \\ 72 \\ a = 6\sqrt{3}$$

$$A = \frac{1}{2}(6\sqrt{3})(72)$$

$$A = 216\sqrt{3} \approx$$

$$A \approx 374.12 \text{ in}^2$$

b.



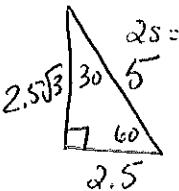
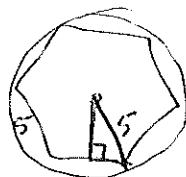
$$P = 20(3) \\ 60$$

$$s = \frac{10\sqrt{3}}{3} = a$$

$$A = \frac{1}{2}\left(\frac{10\sqrt{3}}{3}\right)(60)$$

$$\frac{300\sqrt{3}}{3} \approx 100\sqrt{3} \approx 173.2 \text{ cm}^2$$

7. Your math teacher draws a regular hexagon with a circle circumscribed around it. The radius of the circle is 5 m. To the nearest tenth, what is the area of the hexagon?



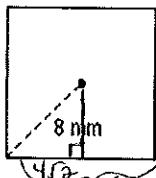
$$a = 2.5\sqrt{3} \\ P = 5(6) \\ 30$$

$$A = \frac{1}{2}(2.5\sqrt{3})(30) \\ 37.5\sqrt{3}$$

$$64.95 \approx 65.0 \text{ m}^2$$

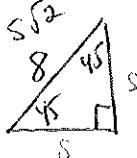
8. Find the area of each regular polygon with the given radius or apothem. If your answer is not an integer, leave it in simplest radical form.

a.



b.

$$8\sqrt{2} \\ P = 32\sqrt{2}$$



$$s\sqrt{2} = 8$$

$$s = \frac{8}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{8\sqrt{2}}{2}$$

$$s = 4\sqrt{2}$$

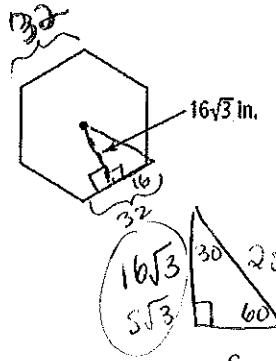
$$a = 4\sqrt{2}$$

$$P = 32\sqrt{2}$$

$$A = \frac{1}{2}(4\sqrt{2})(32\sqrt{2})$$

$$64 \cdot 2 = \\ 128 \text{ mm}^2$$

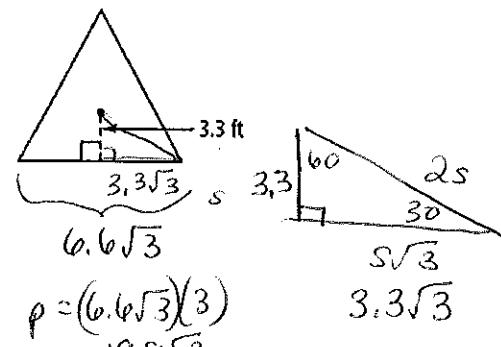
c.



$$s = 16$$

$$P = 32(6) \\ 192$$

$$A = \frac{1}{2}(16\sqrt{3})(192) \\ 1536\sqrt{3}$$



$$P = (6.45\sqrt{3})(3) \\ 19.8\sqrt{3}$$

$$A = \frac{1}{2}(3.3)(19.8\sqrt{3}) \\ 32.67\sqrt{3} \text{ ft}^2$$

$$(56.59)$$