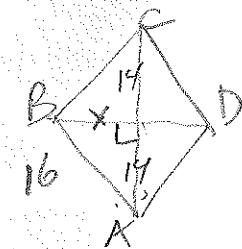


5. In rhombus ABCD,  $AB = 16$  and  $AC = 28$ . Find the area of the rhombus to the nearest tenth.



$$14^2 + x^2 = 16^2$$

$$x^2 = 256 - 196$$

$$x^2 = 60$$

$$x = \sqrt{60}$$

$$A = \frac{1}{2}(28)(\sqrt{60})^2$$

$$= 216.9 \text{ units}^2$$

6. The figure below is an overhead view of a deck surrounding a hot tub. What is the area of the deck to the nearest tenth?

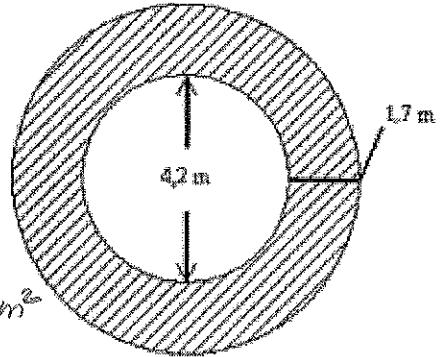
$$r_1 = 2.1$$

$$r_2 = 2.1 + 1.7 = 3.8$$

$$A_1 = \pi(2.1)^2 = 4.41\pi$$

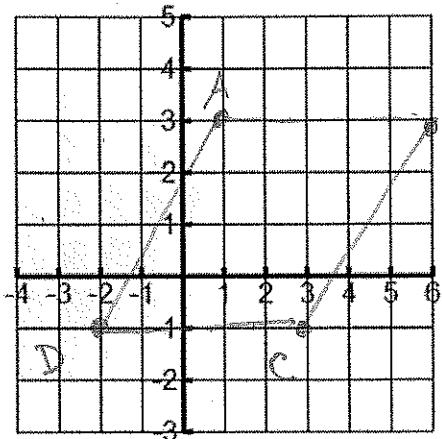
$$A_2 = \pi(3.8)^2 = 14.44\pi$$

$$A_2 - A_1 = 10.03\pi \approx 31.5 \text{ m}^2$$



7. Given A(1, 3) B(6, 3) C(3, -1) D(-2, -1).

Plot the points on the grid provided. Label your points, including coordinates.



- a) Find the slopes of the segments (in the subscripts). Show your work.

$$m_{AB} = 0$$

$$m_{BC} = \frac{4}{3}$$

$$m_{CD} = 0$$

$$m_{DA} = \frac{4}{3}$$

- b) Find the length of the segments indicated. Show your calculations.

$$AB = 5$$

$$BC = \sqrt{3^2 + 4^2} = \sqrt{25} = 5$$

$$CD = 5$$

$$AD = 5$$

- c) ABCD is a quadrilateral. How would you classify it? (What name would you give it?) Be as exact as you can.

rhombus

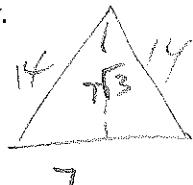
- d) Find the Area of quadrilateral ABCD

$$A = bh = 5(4) = 20 \text{ units}^2$$

8. Each of the following triples represents sides of a triangle. Determine whether the triangle is right, acute or obtuse.

a. 14, 48, 50	$\frac{50^2 \cancel{(?)} 14^2 + 48^2}{9^2 \cancel{(?)} 4^2 + 8^2}$	$2500 = 2500$ right
b. 4, 8, 9	$\frac{9^2 \cancel{(?)} 4^2 + 8^2}{6^2 \cancel{(?)} (2\sqrt{3})^2 + 4^2}$	$81 > 80$ obtuse
c. $2\sqrt{3}, 4, 6$	$\frac{6^2 \cancel{(?)} (2\sqrt{3})^2 + 4^2}{36 > 28}$	obtuse

9. Determine the area of an equilateral triangle whose side length is 14 in. Leave answer in simplified square roots if necessary.



$$A = \frac{1}{2}bh = \frac{1}{2}(14)(7\sqrt{3}) = 49\sqrt{3} \text{ in}^2$$

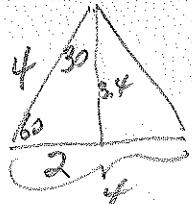
10. A regular hexagon has an apothem of 2cm and a side length of  $\frac{4\sqrt{3}}{3}$  cm. Determine its area exactly.

$$\begin{aligned} A &= \frac{1}{2}ap \\ &= \frac{1}{2}(2)(8\sqrt{3}) \\ &= 8\sqrt{3} \text{ cm}^2 \end{aligned}$$

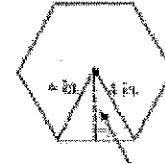


11. What is the perimeter of the regular hexagon to the nearest inch? (Radius is 4 in, apothem is 3.4 in)

$$P = 6(6) = 24 \text{ in}$$



$$\frac{362}{6} = 60$$



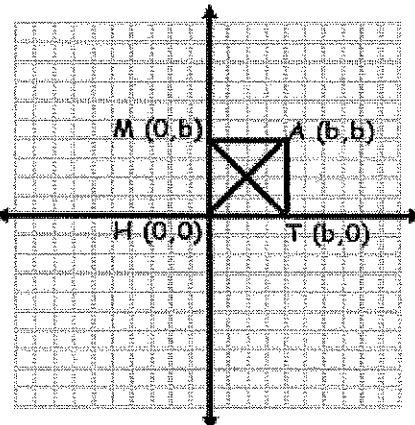
M(0,b) MATH is a square with diagonals  $\overline{AH}$  and  $\overline{MT}$ . Use distance, slope and/or midpoint formulas to prove each statement: Show all work

12. Diagonals are congruent.

distance

13. Diagonals bisect each other.

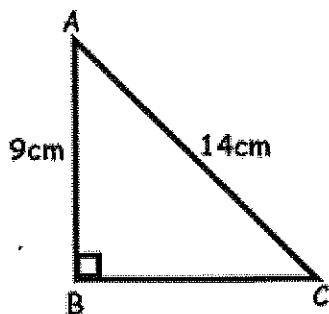
midpoint



14. Diagonals are perpendicular to each other.

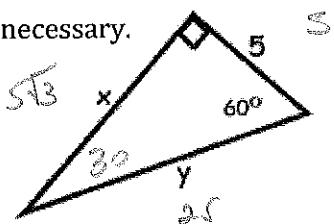
slope

15. In the triangle below, find BC when AB = 9cm and AC = 14cm. Leave answer to the nearest tenth.



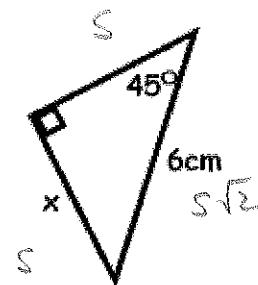
16. In the triangle below, find  $x$  and  $y$ . Leave answers as simplified square roots when necessary.

$$\begin{aligned} s &= 5 \\ x &= 5\sqrt{3} \\ y &= 2(5) = 10 \end{aligned}$$



17. Find  $x$ . Leave answers as simplified square roots when necessary.

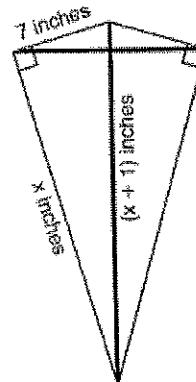
$$\begin{aligned} \sqrt{2} &= 6 \\ s &= \frac{6}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{6\sqrt{2}}{2} = 3\sqrt{2} \end{aligned}$$



ANSWER KEY

18. A kite needs a vertical and a horizontal support bar attached at opposite corners. The upper edges of the kite are 7 inches, the side edges are  $x$  inches and the vertical support bar is  $(x + 1)$  inches. What is the measure of the vertical support bar in inches?

$$\begin{aligned} x^2 + 7^2 &= (x+1)^2 \\ x^2 + 49 &= x^2 + 2x + 1 \\ 48 &= 2x \\ 24 &= x \\ x+1 &= 25 \quad \boxed{25 \text{ in.}} \end{aligned}$$



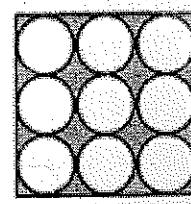
19. In the figure, each circle has a radius of 2 inches. What is the area of the shaded region rounded to the nearest hundredth?

$$A_s = (12)(12) = 144$$

$$A_c = \pi r^2 = 4\pi$$

$$9A_c = 36\pi$$

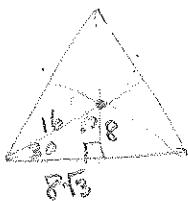
$$A_{\text{shaded}} = 144 - 36\pi \approx 32.96 \text{ in}^2$$



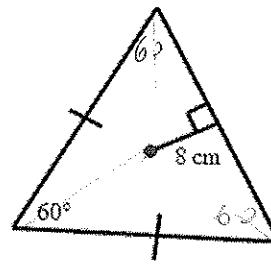
20. Find the area of the triangle if the length of the apothem is 8 cm.

$$h = (6+8) = 24$$

$$b = 2(8\sqrt{3}) = 16\sqrt{3}$$



$$A = \frac{1}{2}(16\sqrt{3})(24) = 192\sqrt{3} \text{ cm}^2$$



21. Find the area of the triangle if  $HW=6$  ft and  $DH$  is the apothem.

$$h = 6\sqrt{3}$$

$$b = 12$$

$$A = \frac{1}{2}(12)(6\sqrt{3}) = 36\sqrt{3} \text{ ft}^2$$

$HG$

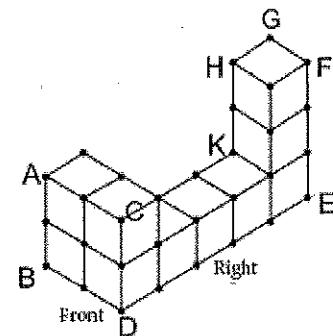
### Part 6

Use the diagram to answer the questions #1-5:

1) Name 2 pairs of skew lines  $AC + EF$   
 $CD + GH$

2). Name a plane that is perpendicular to line DE plane ABC

3) Name 2 pairs of parallel planes plane ABC // plane EFG  
plane CDE // plane ABH



### Part 7- Surface Area and Volume

Determine the surface area and volume of a right prism with the given base shape, base dimensions, and prism height, h. Round to the nearest tenth, if necessary.

$$SA = L + 2B \quad SA = hP + 2B$$

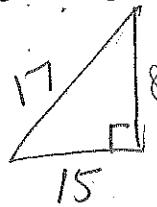
$$V = Bh$$

1. Square base whose side measures 3 meters;  $h = 14$  meters

2. Regular hexagon base whose sides measure 10 cm;  $h = 4$  cm

3. Equilateral triangle base whose sides measure 6 inches;  $h = 8$  in \_\_\_\_\_

4. A right triangle base whose hypotenuse is 17 in and one leg is 15 in;  $h = 5$  in



$$15^2 + x^2 = 17^2$$
$$x^2 = 64$$
$$x = 8$$
$$B = \frac{1}{2}(15)(8) = 60$$
$$SA = hP + 2B$$
$$= 5(40) + 2(60)$$
$$= 320 \text{ in}^2$$

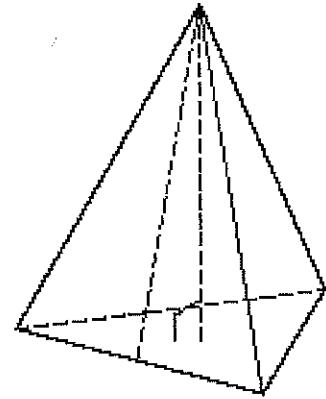
$$P = 40$$

$$V = Bh$$
$$= 60(5) = 300 \text{ in}^3$$

Use the pyramid at the right. The base of the pyramid is an equilateral triangle whose perimeter is 120 in. The volume of the pyramid is 3464.1 in<sup>3</sup>.

$$SA = L + B \quad SA = 3LP + B \quad V = \frac{1}{3}Bh$$

5. Determine the length of a side of the base \_\_\_\_\_



6. Determine the area of the base of the pyramid \_\_\_\_\_

7. Determine the height of the pyramid \_\_\_\_\_

8. The apothem of the triangular base is 11.547 in. Determine the slant height of the pyramid.

9. Determine the total surface area \_\_\_\_\_

$$SA = L + 2B \quad SA = 2\pi rh + 2\pi r^2 \quad V = Bh = \pi r^2 h$$

Determine the unknown value for a right cylinder with the given radius, r, height, h, surface area SA, and volume, V.

10.  $r = 26'$ ,  $h = 16'$

$SA = \underline{\hspace{2cm}}$

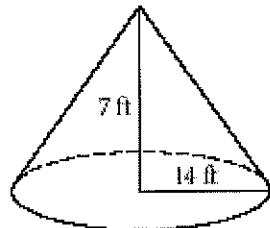
11.  $SA = 98 \text{ in}^2$ ,  $h = 14 \text{ in}$ ,  $r = \underline{\hspace{2cm}}$

12.  $V = 144 \text{ cm}^3$ ,  $r = 12 \text{ cm}$ ,  $h = \underline{\hspace{2cm}}$

13.  $V = 80 \text{ in}^3$ ,  $h = 16 \text{ in}$ ,  $r = \underline{\hspace{2cm}}$

Determine the surface area of each right cone.

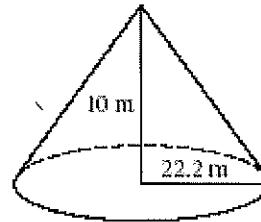
14.



$\underline{\hspace{2cm}}$

$$SA = L + B \quad SA = \pi r l + \pi r^2$$

15.

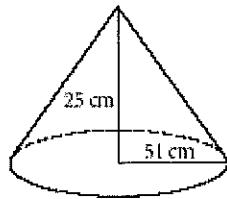


$\underline{\hspace{2cm}}$

16. A right cone has a surface area of  $152\pi$  square meters. The radius is 8 meters. Determine the slant height.

Determine the volume of each right cylinder.

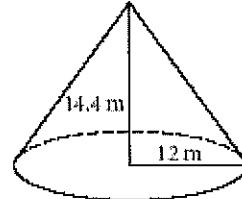
17.



$\underline{\hspace{2cm}}$

~~Cone~~ 
$$V = \frac{1}{3}Bh \quad V = \frac{1}{3}\pi r^2 h$$

18.



$\underline{\hspace{2cm}}$

19. The volume of a right cone is  $27\pi$  cubic inches. The height is the same as the radius. Determine the surface area of the cone to the nearest hundredth.

---

20. Determine the surface area of a sphere with a diameter of 4". Leave answer in terms of  $\pi$ .

$$SA = 4\pi r^2$$

---

21. Determine the length of a radius if the surface area of a sphere is  $36\pi \text{ cm}^2$ .

---

22. Determine the volume of a sphere with a radius of 14 cm.

$$V = \frac{4}{3}\pi r^3$$

---

23. Determine the volume of a sphere if the surface area is  $100 \text{ cm}^2$ .

---

24. Determine the volume of a sphere if the surface area is  $100\pi \text{ cm}^2$

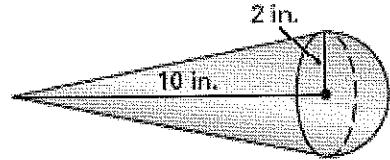
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Cone:  $SA = \pi dl + \pi r^2$        $V = \frac{1}{3}\pi r^2 h$

Determine the surface area and volume of each composite.

Sphere:  $SA = 4\pi r^2$        $V = \frac{4}{3}\pi r^3$

25.

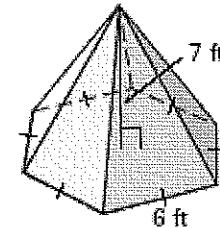


Cone:

$$SA = \underline{\hspace{2cm}}$$

$$\text{Volume} = \underline{\hspace{2cm}}$$

26.



Pyramid:  $SA = \frac{1}{2}lp + B$   
 $V = \frac{1}{3}Bh$

$$SA = \underline{\hspace{2cm}}$$

$$\text{Volume} = \underline{\hspace{2cm}}$$

### Part 8

#### Multiple-Choice

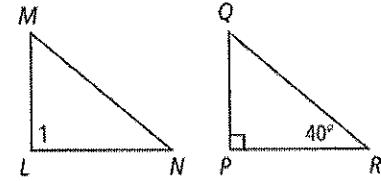
1. The pair of polygons below are similar. Determine the measure of angle 1.

a.  $90^\circ$

b.  $40^\circ$

c.  $50^\circ$

d.  $95^\circ$



2. Which of the following theorems/postulates is NOT a way to determine if triangles are similar?

a. SAS

b. ASA

c. AA

? d. SAA  
SSA

3. On a map of Florida, one-fourth of an inch represents 10 miles. If it is approximately 2 inches from Orlando to Ocala on the map, what is the actual distance in miles?

a. 16

b. 64

c. 80

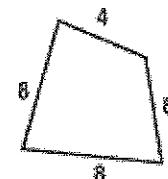
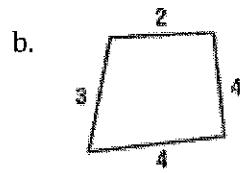
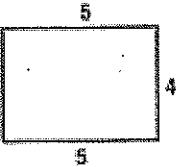
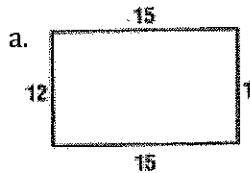
d. 20

$$\frac{.25}{10} = \frac{2}{x}$$

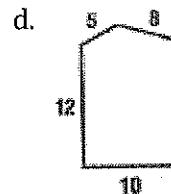
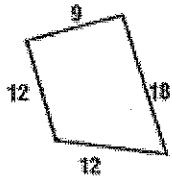
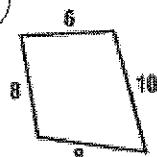
$$.25x = 20$$

$$x = 80$$

4. Which pair of polygons are definitely not similar?



c.



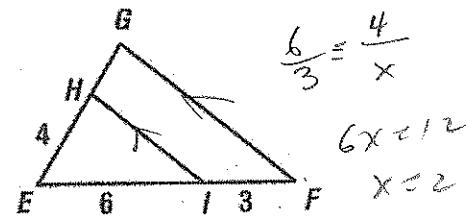
5. Given  $\triangle EGF$  with  $\overline{HI} \parallel \overline{GF}$ ,  $EI = 6$ ,  $IF = 3$ , and  $EH = 4$ , find  $HG$ .

a. 2

b. 3

c. 6

d. 10



6. Which proportion illustrates the Side-Splitting Theorem?

a.  $\frac{AD}{AB} = \frac{AL}{AE}$

b.  $\frac{AD}{EL} = \frac{AB}{AL}$

c.  $\frac{AD}{AE} = \frac{AL}{AB}$

d.  $\frac{AD}{DB} = \frac{AE}{EL}$

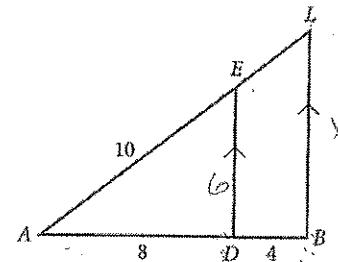
7. In  $\triangle ADE$ , if  $ED = 6$  what is  $BL$ ?

a. 3

b. 5

c. 9

d. 12



$$\frac{8}{6} = \frac{12}{x} \quad 8x = 72 \quad x = 9$$

8. The perimeter of  $\triangle GHI$  is 18, the perimeter of  $\triangle PQR$  is 30, and  $\triangle GHI \sim \triangle PQR$ . If  $GH$  is 10, what is  $PQ$ ?

a. 3.6

b. 6

c. 16.67

d. 27.78

$$\frac{18}{30} = \frac{10}{x} \quad 18x = 300 \quad x = 16.67$$

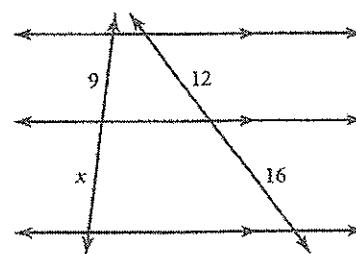
9. Suppose  $\triangle ABC$  is similar to a triangle whose sides have lengths 3, 7, and 6. Which of the following could be the perimeter of  $\triangle ABC$ ?

a. 8

b. 16

c. 32

d. any of these



10. What is the value of  $x$  in the figure at the right?

a. 8

b. 12

c. 14

d. 16

$$\frac{9}{x} = \frac{12}{16}$$

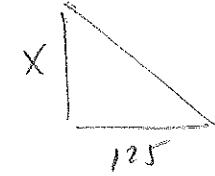
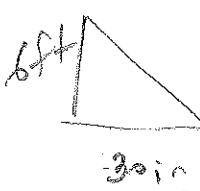
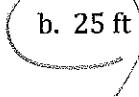
$$16x = 144$$

$$x = 9$$

11. The shadow of a man 6 feet tall is 30 inches long. At the same time of day, a building casts a shadow 125 inches long. How tall is the building?

- a. 15 ft      b. 25 ft      c. 30 ft

d. 50 ft



$$\frac{6}{30} = \frac{x}{125}$$

$$30x = 750$$

$$x = 25$$

12. It costs \$144 to refinish a floor that is 9 feet by 12 feet. At the same rate, how much will it cost to refinish a floor that is 12 feet by 16 feet?

- a. \$81      b. \$108      c. \$256

d. \$576



$$\frac{144}{108} = \frac{x}{192}$$

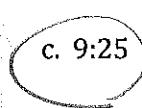
$$108x = 27648$$

$$x = 256$$

13. Two spheres have radii of 3 cm and 5 cm. What is the ratio between the areas of their great circles?

- a. 3:5      b. 6:10      c. 9:25

d. 27:125



$$\frac{3}{5}$$

$$\frac{9}{25}$$

$$\sqrt{\frac{9}{25}} = \frac{3}{5}$$

14. The area of one side of a cube is 36 ft<sup>2</sup>. If the edges of the cube are tripled, what is the volume of the new cube?

- a. 36 ft<sup>3</sup>      b. 196 ft<sup>3</sup>      c. 324 ft<sup>3</sup>

d. 5832 ft<sup>3</sup>

$$A = 36$$

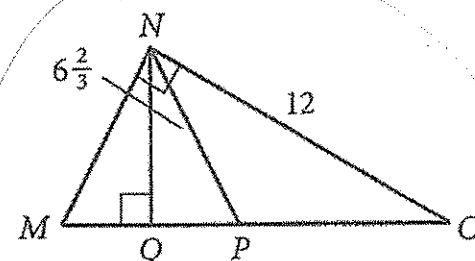
$$S = 6$$

$$3S = 18$$

$$V = 18^3$$

15. In the figure at the right,  $\triangle MNO \sim \triangle HIJ$ . What is the length of  $\overline{NQ}$ ?

- a. 6      b. 10      c. 12      d. 15



16.  $MN =$

- a.  $6\sqrt{7}$       b.  $4\sqrt{7}$       c.  $4\sqrt{3}$       d.  $6\sqrt{3}$

$$\frac{12}{18} = \frac{x}{6\sqrt{7}}$$

$$18x = 72\sqrt{7}$$

$$x = 4\sqrt{7}$$

$$\frac{12}{18} = \frac{NQ}{9}$$

$$NQ = 6$$

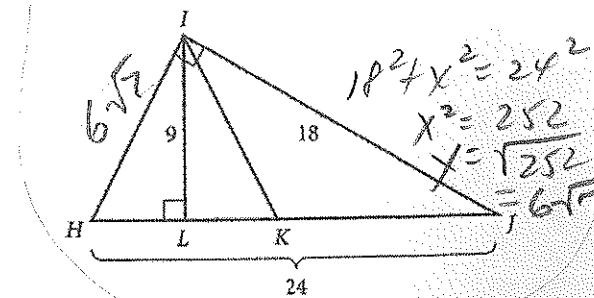
17. What is the length of  $\overline{IK}$ ?

- a. 9      b. 10      c. 12      d. 15

$$\frac{6\frac{2}{3}}{x} = \frac{12}{18}$$

$$12x = 120$$

$$x = 10$$



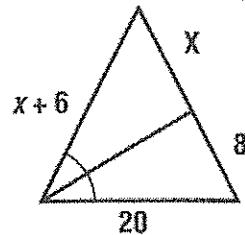
18. For the figure at the right, find the value of  $x$ .

a. 3

b. 4

c. 5

d. 6



$$\begin{array}{r} x+6 \\ \times 2 \\ \hline 2x+12 \\ -12 \\ \hline x \end{array}$$

19. Which polygon is similar to other polygons of its classification?

a. rectangle

b. rhombus

c. regular octagon

d. isosceles triangle

20. The measures of the angles of a triangle are in the extended ratio 2:4:9. Which is a measure of one of the angles?

a. 12

b. 36

c. 48

d. 105

$$2x + 4x + 9x = 180^\circ$$

$$15x = 180$$

$$x = 12$$

$$24, 48, 108$$

Complete each statement with the word *always*, *sometimes*, or *never*.

21. Two equilateral triangles are always similar.

22. Two similar triangles are sometimes congruent.

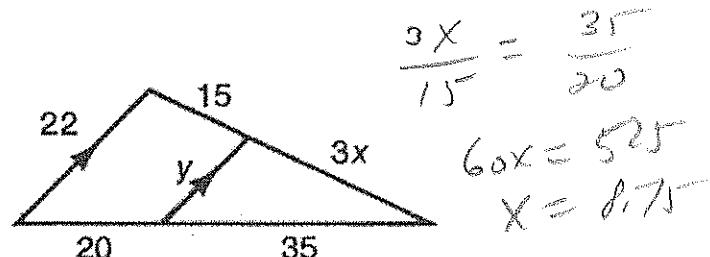
23. Two congruent triangles are always similar.

24. Two isosceles right triangles are always similar.

25. Find the values of  $x$  and  $y$ .

$$x = 8.75$$

$$y = 14$$



$$\frac{35}{22} = \frac{3x}{20}$$

$$60x = 525$$

$$x = 8.75$$

$$58y = 770$$

$$y = 14$$

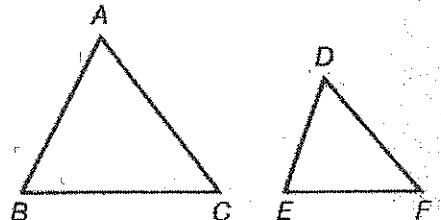
26. Using the given information, tell which triangles are similar. The diagram is not drawn to scale.

a.  $\frac{AB}{DF} = \frac{AC}{DE}$ ;  $\angle A \cong \angle D$

$\triangle ABC \sim \triangle DFE$  or  $\triangle BAC \sim \triangle FDE$

b.  $\frac{AB}{FD} = \frac{BC}{DE} = \frac{AC}{FE}$

$\triangle ABC \sim \triangle FDE$



ABC FDE

c.  $\angle A \cong \angle E$ ;  $\angle B \cong \angle F$

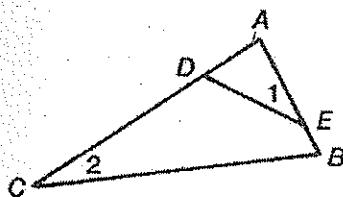
$\triangle ABC \sim \triangle EFD$

d.  $AB = AC$ ;  $DE = DF$ ;  $\angle A \cong \angle D$

$\triangle ABC \sim \triangle DEF$

27. Given:  $\angle 1 \cong \angle 2$

Prove:  $\frac{AD}{AB} = \frac{AE}{AC}$



Statements	Reasons

## Part 9:

Given  $\odot Q$ ,  $m\angle ABC = 72^\circ$  and  $m\widehat{CD} = 46^\circ$ .  $\overline{BD}$  is a diameter. Find the indicated measures.

$$1. \widehat{mCA} = 144$$

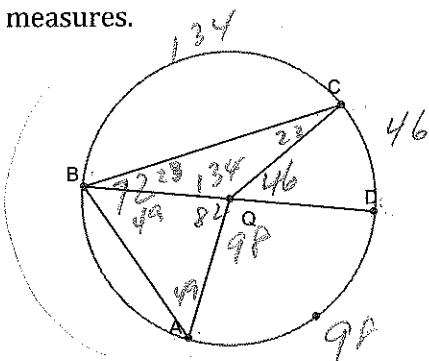
$$2. m\widehat{BC} = \underline{\hspace{2cm}134\hspace{2cm}}$$

$$3. m\widehat{AD} = \underline{\hspace{2cm}} 98$$

$$4. m\angle C = \underline{\hspace{2cm}}^{23}$$

$$5. m\angle ABD = \underline{\hspace{2cm}} 19$$

$$6. m\angle A = \underline{\hspace{2cm}} 49^{\circ} .$$



In the circle to the right,  $m\angle CAE = 60^\circ$ ,  $m\widehat{BC} = (10x - 36)^\circ$ ,  $m\widehat{BA} = (8x)^\circ$ ,  $m\widehat{AE} = (4x + 12)^\circ$ , and  $\overline{DE} \cong \overline{DC}$ . Find each of the following measures:

$$4x^2 + 72 + 8x + 10x - 36 + 120 = 360$$

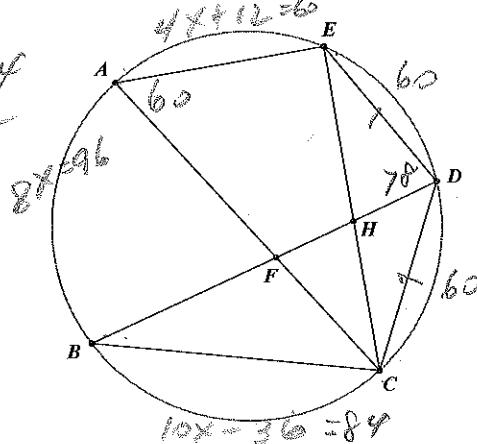
$$7. x = \underline{12}$$

$$8. m\angle BDE = \underline{78} \quad x = 12$$

$$9. \widehat{mECA} = 30.0$$

$$10. \ m\widehat{CD} = 60$$

$$11. m\angle BFC = \frac{60 + 60 + 184}{2} = 102$$



12. If the length of an arc on a circle is 26 cm and the radius of that circle is 10 cm, what is the degree measure of the arc? Leave your answer in exact, simplified terms.

$$\frac{L}{2\pi r} = \frac{M}{360} \quad \frac{26}{2\pi(10)} = \frac{M}{360} \quad 20\pi M = 9360$$

$$M = \frac{9360}{20\pi} = \left(\frac{468}{\pi}\right)^*$$

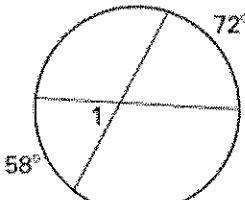
13. If the radius of a circle is 22 mm and the degree measure of one of the arcs on the circle is  $160^\circ$ , find the length of the arc.

$$\frac{162}{360} = \frac{L}{2\pi(21)} \quad 360L = 7248\pi$$

$$L = \frac{7248\pi}{360} = \frac{176\pi}{9} \text{ mm}$$

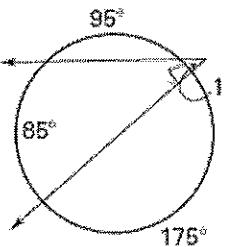
For each of the following problems, find the  $m_4$ .

14.



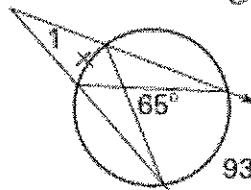
$$\begin{array}{r} 58 + 72 \\ \hline 130 \end{array}$$

15.



$$\frac{1}{2}(R=5)$$

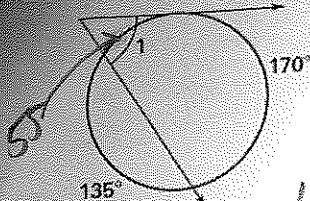
16.



$$m61 = \frac{93 - 37}{2} = 28$$

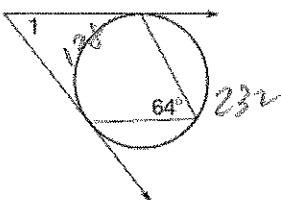
$$65 = \frac{1}{2}(x + 93)$$

17.



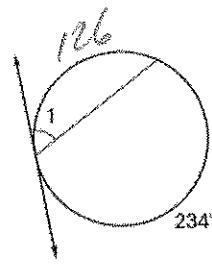
$$\frac{1}{2}(170 - 55) \\ 57.5$$

18.



$$\frac{1}{2}(232 - 128) \\ 52$$

19.

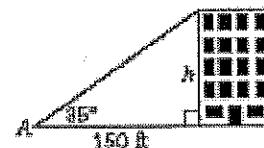


$$m\angle = \frac{126}{2} = 63^\circ$$

### Part 10

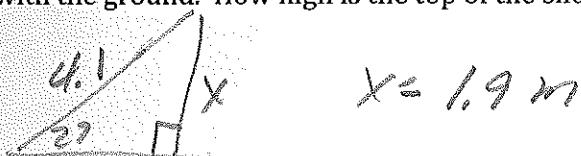
1. Determine the height of the building, to the nearest tenth, when  $\angle A = 35^\circ$

$$\tan 35 = \frac{h}{150} \quad h = 105.0 \text{ ft}$$



2. A slide 4.1 m long makes an angle of  $27^\circ$  with the ground. How high is the top of the slide above the ground? Round your answer to the nearest tenth.

$$\sin 27 = \frac{x}{4.1}$$



$$x = 1.9 \text{ m}$$

3. Tom drives 16 km up a hill that is at a grade of  $10^\circ$ . What horizontal distance, to the nearest tenth of a kilometer, has he covered?

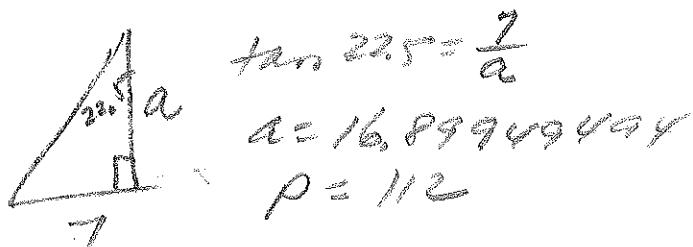


$$\cos 10 = \frac{x}{16}$$

$$x = 15.8 \text{ km}$$

4. Find the area of an octagon whose side length is 14 in.

$$A = \frac{1}{2}ap \\ = 946.3717 \text{ in}^2$$



$$\tan 22.5 = \frac{7}{a}$$

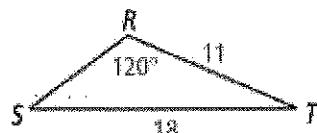
$$a = 16.89949494 \\ P = 112$$

5. In triangle RST, what is the measure of angle S to the nearest tenth?

$$\frac{\sin X}{11} = \frac{\sin 120}{18}$$

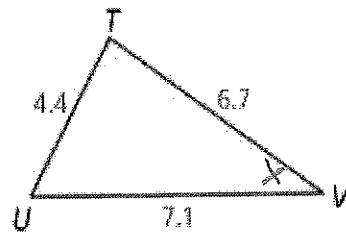
$$\frac{18 \sin X}{18} = \frac{11 \sin 120}{18}$$

$$\sin X = 31.953 \approx 32.0^\circ$$



the measure of angle V to the nearest tenth.

$$a^2 = a^2 + b^2 - 2ab \cos C$$
$$4.4^2 = 6.7^2 + 7.1^2 - 2(6.7)(7.1) \cos X$$
$$\frac{-75.94}{-2(6.7)(7.1)} = \cos X$$
$$.798192 = \cos X$$



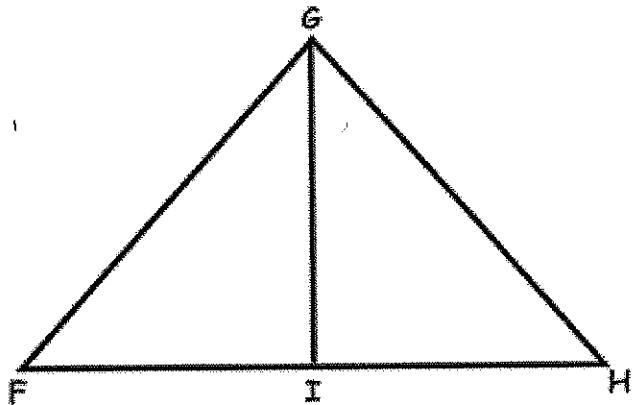
$$X = 37.0^\circ$$

### Part 11

1. Prove Indirectly:

Given:  $\triangle GHF$  is not isosceles;  $\angle GIF \cong \angle GIH$

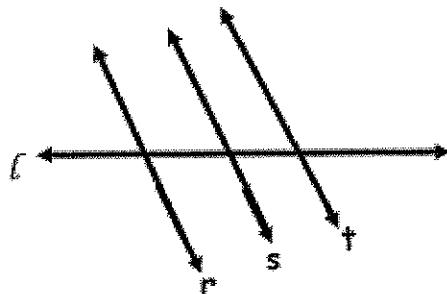
Prove:  $\overline{GI}$  is not a median



2. Prove indirectly.

Given:  $r \parallel s, s \nparallel t$

Prove:  $r \nparallel t$



GEOMETRY 21: Review for Final Exam ANSWER KEY

REV May 29, 2014

**Part 1**

- 1) F  
2) F  
3) ~~F~~ ✓ T  
4) F  
5) Point C  
6) Line AB  
7) Line CG  
8) Yes  
9) Segment EB  
10) Infinitely many  
11)  $x=7$ ,  $m\angle 3=52^\circ$   
12)  $180 - y$   
13)  $43$  and  $46$   
14)  $\triangle DGF$  and  $\triangle AGF$   
15) Parallel

16) Rotation

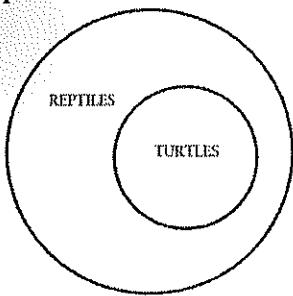
17) Reflection

18) Translation

- 19) incenter, inscribed  
20) circumcenter, circumscribed  
21) centroid  
22) orthocenter

**Part 2**

- 1) If an animal is a turtle, then it is a reptile.  
2) Hyp.: It is a turtle, Concl.: it is a reptile  
3)



- 4) If angles are a linear pair, then they are supplementary, adjacent angles

- 5) If angles are supplem, and adjacent, then they form a linear pair.  
6) Angles are a linear pair if and only if they are supplem. and adjacent.  
7) Yes, both conditional and converse are true.  
8)  $X=50^\circ$   
9)  $X=15^\circ$

- 10) F      15) E  
11) G      16) C  
12) D      17) B  
13) A      18) H

- 14)  $x = 4.08$       23) 149.72  
15) 47.56      24) 132.44  
16) 102.16      25) 30.28  
17) 30.28      26) 47.56

**Part 3**

- 1) C      4) C  
2) C      5) C  
3) B      6) A

- 7) c      11) c      15) d      19) a  
8) d      12) a      16) b      20) c  
9) c      13) d      ~~17) d~~      21) b  
10) b      14) c      18) b      22) a  
23) F      24) T      25) T      26) T  
27) T      28)  $65^\circ$       29)  $60^\circ$

- 1)  $\overline{MN} \parallel \overline{PO}$       1 - given  
2 -  $\angle P$  and  $\angle M$  sup      2 - same side int  $\angle$  thm  
3 -  $m\angle P + m\angle M = 180$       3 - defn sup  $\angle$ 's  
30) 4 -  $\angle M \cong \angle O$       4 - given  
5 -  $m\angle M = m\angle O$       5 - defn  $\cong$   
6 -  $m\angle P + m\angle O = 180$       6 - substitution  
7 -  $\angle P$  and  $\angle O$  sup      7 - defn sup  $\angle$ 's  
8 -  $\overline{MP} \parallel \overline{NO}$       8 - converse of SSI  $\angle$  thm

**Part 4**

- 1)  $x=15, y=38$  2)  $x=7/2$  or  $-3$  3)  
 $A=6, b=15$

- 7) no 8) yes AAS or ASA 9) yes, HL

- 4) Yes, AAS or ASA 6) yes, any AAS, ASA,  
5) No SAS or SSS

1-  $\angle D \cong \angle B$ ;  $\overline{CB} \parallel \overline{DA}$  1- given

- 10) 2-  $\angle BCA \cong \angle DAC$  2- Alt. Int.  $\angle$ 's thm  
3-  $\overline{AC} \cong \overline{CA}$  3- reflexive  
4-  $\triangle DCA \cong \triangle BAC$  4- AAS

1-  $\angle 1 \cong \angle 2$ ;  $\angle 3 \cong \angle 4$  1- given

- 11) 2-  $\overline{BA} \cong \overline{BC}$  2- converse of isos.  $\triangle$  thm  
3-  $\triangle BAE \cong \triangle BCD$  3- ASA  
4-  $\overline{BE} \cong \overline{BD}$  4- CPCTC  
5-  $\triangle BDE$  is isosceles 5- def isos.  $\triangle$

- 13) a.  $134^\circ$ ; b.  $x=7, y=4$

1- ABCD kite;  $\overline{AB} \cong \overline{BC}$ ;  $\overline{AD} \cong \overline{CD}$  1- given

- 2-  $\overline{BD} \cong \overline{BD}$  2- reflexive  
12) 3-  $\triangle ABD \cong \triangle CBD$  3- SSS  
4-  $\angle ABD \cong \angle CBD$  4- CPCTC  
5-  $\overline{BD}$  bisects  $\angle ABC$  5- def bisector  
6-  $\triangle ABC$  is isosceles 6- def isos.  $\triangle$   
7-  $\overline{BD}$  bisects  $\overline{AC}$

7 - the bisector of the vertex  
Angle of an isos  $\triangle$  is  $\perp$  bis. of base

7)

**Part 5**

- 1)  $966 \text{ u}^2$   
2)  $254 \text{ in}^2$   
3)  $160\sqrt{5} \text{ u}^2$   
4)  $12.5 \text{ u}^2$

- 5)  $216.9 \text{ u}^2$   
6)  $31.5 \text{ m}^2$   
7) a) right  
b) obtuse  
c) obtuse  
8) slopes  
 $\overline{AB} = \overline{CD} = 4/3$   
 $\overline{BC} = \overline{DA} = 0$   
Dist. Form.  
 $AB = BC = CD = AD = 5$   
Rhombus,  
Area =  $20 \text{ u}^2$

- 9)  $49\sqrt{3} \text{ in}^2$   
10)  $8\sqrt{3} \text{ cm}^2$   
11)  $p=24$   
12) dist. Form.  
 $MT = AH = b\sqrt{2}$

- 13) mdpts.  $\left(\frac{b}{2}, \frac{b}{2}\right)$   
14) slope of  $\overline{MT} = -1$   
 $AH = 1$  so  $\perp$   
15) 10.7  
16)  $x = 5\sqrt{3}, y = 10$

- 17)  $3\sqrt{2} \text{ cm}$   
18)  $x = 24 \text{ in}$  25)  
19) 30.90  
20)  $192\sqrt{3}$  or  
 $332.55 \text{ cm}^2$   
21)  $36\sqrt{3}$  or  
62.35 ft<sup>2</sup>

**Part 6**

- 1)  $\overrightarrow{AC}$  skew to  $\overrightarrow{FE}$ ,  $\overrightarrow{CD}$  skew to  $\overrightarrow{GH}$  2) plane ABC 3) plane ABC  $\parallel$  plane GFE, plane CDE  $\parallel$  plane ABH

- Part 7** \*all SA are in square units, all V in cubic units  
1) SA=186 V=126  
2) SA=759.6, V=1039.23  
3) SA=175.2, V=124.7  
4) SA=320, V=300

- 5) 40 in  
6) 692.8 in<sup>2</sup>  
7) 15 in  
8) 18.93 in  
9) SA= 1828.62  
10) SA=6861.2  
11) r = 1.04 in

- 12) .3 cm  
13) 1.3 in  
14) SA=1304.2  
15) SA=3246.4  
16) 11 m  
17) V= 68,094  
18) V= 2171

- 19) r=4.33, SA=142.15  
20) SA=16π  
21) r= 3 cm  
22) V=11,494.04  
23) V=94.03  
24) SA= 523.6

- 25) SA =  $28.4\pi$  ≈ 89.13  
V = 58.613  
26) SA= 250.45 V=  $126\sqrt{3}$  ≈ 218.24

### Part 8

- Leave as a  
fixed question ✓
- 1) a 2) d 3) c 4) c 5) a 6) d 7) c 8) c 9) d 10) b 11) b 12) c 13) c 14) d 15) a  
 16) b 17) b 18) b 19) c 20) c 21) always 22) sometimes 23) always 24) always  
 25)  $x = 35/4 \approx 8.75$ ,  $y = 14$  26) a)  $\triangle BAC \sim \triangle FDE$  b)  $\triangle ABC \sim \triangle FDE$  c)  $\triangle ABC \sim \triangle EFD$  d)  
 $\triangle ABC \sim \triangle DEF$

1- $<1 \leq <2$  1- given

2- $<A \cong <A$  2- reflexive

27) 3- $\triangle EAD \sim \triangle CAB$  3- AA similarity

4-  $\frac{AD}{AB} = \frac{AE}{AC}$  4- PSP (polygon similarity postulate)

### Part 9 \*all answers in degrees

- 1) 144  
2) 134  
3) 98

4) 23

5) 49

6) 49

7) 12

8) 78

9) 300

10) 60

11) 102

12)  $468/\pi$

13)  $176\pi/9$

14) 65

15) 40

16) 28

17) 57.5

18) 52

19) 63

mm

### Part 10

- 105.0 ft 2) 1.9 m 3) 15.8 km 4)  $946.37 \text{ in}^2$  5)  $32^\circ$  6)  $37^\circ$

### Part 11

- 1) If today is not Tuesday, then tomorrow is not Wednesday.

2) C

3)

S	q	$\sim q$	$\sim S$	$\sim q \rightarrow \sim S$
T	T	F	F	T
T	F	T	F	F
F	T	F	T	T
F	F	T	T	T

4) A

- 5) Assume  $\overline{GI}$  is a median, then I is midpoint of  $\overline{FH}$ ,  $FI \cong IH$  by defn. midpoint.  $\overline{FI} \cong \overline{IH}$  by defn congruent.  $\overline{GI} \cong \overline{GI}$  by reflexive. Given that  $\triangle GIF \cong \triangle GIH$ , then  $\triangle GIF \cong \triangle GIH$  by SAS. By CPCTC,  $\overline{GF} \cong \overline{GH}$ , so  $\triangle GHF$  is isosceles by defn of isosceles. But this contradicts the given which says  $\triangle GHF$  is not isosceles. So our assumption must be false and  $\overline{GI}$  is not a median.

- 6) Assume  $r \parallel t$ . Then  $\angle 3 \cong \angle 1$  by corresponding angles postulate. Since  $r \parallel s$ ,  $\angle 1 \cong \angle 2$  also by corresponding angles postulate.

So  $\angle 3 \cong \angle 2$  by transitive property. Therefore  $s \parallel t$  by converse of corresponding angles postulate. But this contradicts the given which says that line s is not parallel to line t. My assumption is false and line r is not parallel to line t.