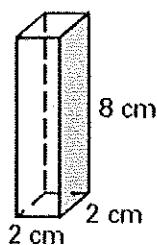


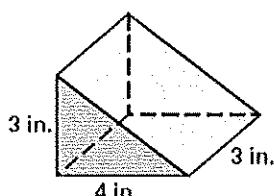
Find the Surface Area and Volume of each right prism. Round to the hundredth if necessary.

3) Find the Surface Area, Lateral Area, and Volume for the following solids. Give an exact answer.

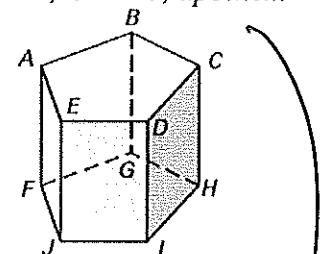
a.



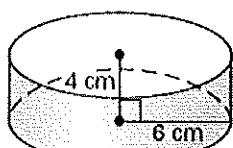
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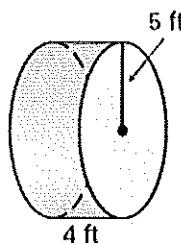
c.  $BC = 12$ ,  $CH = 5$ , apothem = 6.2



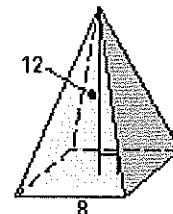
d.



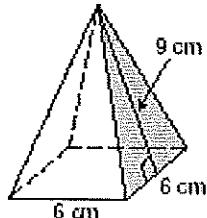
e.



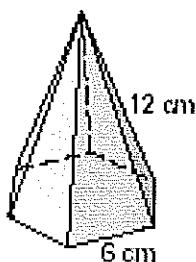
f.



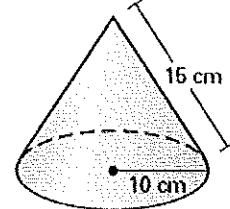
g.



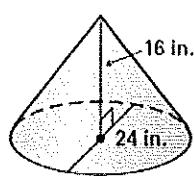
h. apothem = 5.2 cm



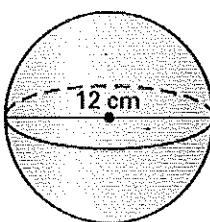
i.



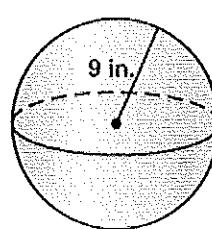
j.



k.

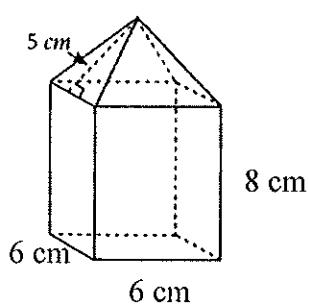


l.

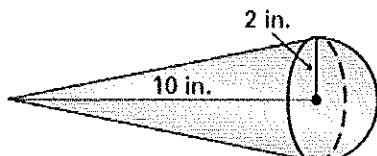


See  
next  
pages

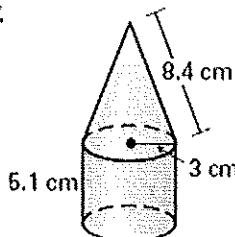
m.



n.



o.



a.)  $SA = 72 \text{ cm}^2$   
 $V = 32 \text{ cm}^3$

b.)  $SA = 48 \text{ in}^2$   
 $V = 18 \text{ in}^3$

c.)  $SA = 672 \text{ units}^2$   
 $V = 930 \text{ units}^3$

d.)  $SA = 376.99 \text{ cm}^2$   
 $V = 452.39 \text{ cm}^3$

e.)  $SA = 282.74 \text{ ft}^2$   
 $V = 314.16 \text{ ft}^3$

f.)  $SA = 266.4 \text{ units}^2$   
 $V = 256 \text{ units}^3$

g.)  $SA = 144 \text{ cm}^2$   
 $V = 101.88 \text{ cm}^3$

h.)  $SA = 258 \text{ cm}^2$   
 $V = 302.12 \text{ cm}^3$

i.)  $SA = 785.4 \text{ cm}^2$   
 $V = 1170.77 \text{ cm}^3$

j.)  $SA = 1206.37 \text{ in}^2$   
 $V = 2412.74 \text{ in}^3$

k.)  $SA = 452.39 \text{ cm}^2$   
 $V = 904.78 \text{ cm}^3$

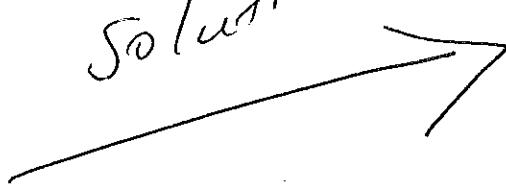
l.)  $SA = 1017.88 \text{ in}^2$   
 $V = 3053.63 \text{ in}^3$

Composites: ~~m~~  $SA = 296 \text{ cm}^2$   
 $V = 336 \text{ cm}^3$

~~n~~  $SA = 89.22 \text{ in}^2$   
 $V = 50.27 \text{ in}^3$

~~o~~  $SA = 203.58 \text{ cm}^2$   
 $V = 218.18 \text{ cm}^3$

See  
next  
pages for  
Surface Area & Volume  
Worked  
out  
Solutions



Geo 22 Final Review KEY

p. 12 SA and V.

a.) Rect. Prism

SA

$$SA = ph + 2B$$

$$p: 2(4) = 8$$

$$h: 8$$

$$B = s^2 = 2^2 = 4$$

$$SA = 8(8) + 2(4)$$

$$= 64 + 8$$

$$= \boxed{72 \text{ cm}^2}$$

V

$$V = Bh$$

$$B = 4$$

$$h = 8$$

$$V = 4(8)$$

$$= \boxed{32 \text{ cm}^3}$$

b.) Tri. Prism

SA

$$SA = ph + 2B$$

$$3^2 + 4^2 = c^2$$

$$\sqrt{25} = \sqrt{c^2}$$

$c = 5 \rightarrow 3^{\text{rd}}$  side  
of base

V

$$V = Bh$$

$$= 6(3)$$

$$= \boxed{18 \text{ in}^3}$$

$$p: 3+4+5 = 12$$

$$h: 3$$

$$B: \frac{3 \cdot 4}{2} = 6$$

$$SA = 12(3) + 2(6)$$

$$= \boxed{48 \text{ in}^2}$$

c.) Pent. Prism

SA

$$SA = ph + 2B$$

$$p: 12(5) = 60$$

$$h: 5$$

$$B = \frac{ap}{2} = \frac{6 \cdot 2 \cdot 60}{2}$$

$$= 180$$

V

$$V = Bh$$

$$= 180(5)$$

$$= \boxed{900 \text{ units}^3}$$

$$SA = 6a(5) + 2(180)$$

$$= 300 + 360$$

$$= \boxed{672 \text{ units}^2}$$

d.) Cylinder

SA

$$SA = 2\pi rh + 2\pi r^2$$

$$= 2\pi(6)(4) + 2\pi(6)^2$$

$$= 48\pi + 72\pi$$

$$= 120\pi = \boxed{376.99 \text{ cm}^2}$$

V

$$V = \pi r^2 h$$

$$= \pi(6)^2(4)$$

$$= 144\pi$$

$$= \boxed{452.39 \text{ cm}^3}$$

12a, b, c, d,

### e) Cylinder

SA

$$\begin{aligned} SA &= 2\pi(5)(4) + 2\pi(5)^2 \\ &= 40\pi + 50\pi \\ &= 90\pi = \boxed{282.74 \text{ ft}^2} \end{aligned}$$

V

$$\begin{aligned} V &= \pi r^2 h \\ &= \pi(5)^2(4) \\ &= 100\pi \\ &= \boxed{314.16 \text{ ft}^3} \end{aligned}$$

### f) Pyramid

SA

$$SA = \frac{P\ell}{2} + B$$

\* need slant height

$$4^2 + 12^2 = \ell^2$$

$$16 + 144 = \ell^2$$

$$\ell = \sqrt{12.65}$$

$$P = 8(4) = \boxed{32}$$

$$B = 8^2 = \boxed{64}$$

$$SA = \frac{32 \cdot 12.65}{2} + 64$$

$$= \boxed{266.4 \text{ units}^2}$$

V

$$V = \frac{Bh}{3}$$

$$= \frac{64 \cdot 12}{3}$$

$$= \boxed{256 \text{ units}^3}$$

### g.) Pyramid

$$SA = \frac{P\ell}{2} + B$$

$$P = 6(l) = \boxed{24}$$

$$l = \boxed{4}$$

$$B: 6^2 = \boxed{36}$$

$$SA = \frac{24 \cdot 4}{2} + 36$$

$$= \boxed{144 \text{ cm}^2}$$

$$V = \frac{Bh}{3}$$

\* need height

$$3^2 + h^2 = 9^2$$

$$9 + h^2 = 81$$

$$h = \boxed{8.49}$$

$$B = \boxed{36}$$

$$V = \frac{36 \cdot 8.49}{3}$$

$$= \boxed{101.88 \text{ cm}^3}$$

### h.) Hex Pyramid

$$SA$$

$$P: 6(l) = \boxed{36}$$

$$l = \boxed{12}$$

$$B: \frac{ap}{2} = \frac{5.2 \cdot 36}{2}$$

$$= \boxed{93.6}$$

$$SA = \frac{36 \cdot 12}{2} + 93.6$$

$$= \boxed{309.6 \text{ m}^2}$$

V

$$V = \frac{Bh}{3}$$

$$B = \boxed{93.6}$$

\* need height

$$3^2 + h^2 = 12^2$$

$$9 + h^2 = 144$$

$$h = \boxed{11.62}$$

$$V = 93.6(11.62) = \frac{362.51 \text{ m}^3}{3}$$

12 e, f, g, h

### i.) Cone

SA

$$\begin{aligned} SA &= \pi r l + \pi r^2 \\ &= \pi(10)(15) + \pi(10)^2 \\ &\approx 150\pi + 100\pi \\ &= 250\pi = 785.40 \text{ cm}^2 \end{aligned}$$

$$\left. \begin{aligned} V &= \frac{\pi r^2 h}{3} \\ &\text{* need height} \\ &10^2 + h^2 = 15^2 \\ &100 + h^2 = 225 \\ &h = 11.18 \\ &V = \frac{\pi(10)^2(11.18)}{3} \\ &\approx 372.67\pi \\ &= 1170.77 \text{ cm}^3 \end{aligned} \right\}$$

### k.) Sphere

SA

$$\begin{aligned} SA &= 4\pi r^2 \\ &= 4\pi(6)^2 \\ &= 144\pi = 452.39 \text{ cm}^2 \end{aligned}$$

$$\left. \begin{aligned} V &= \frac{4\pi r^3}{3} \\ &= \frac{4\pi(6)^3}{3} \\ &= 288\pi = 904.78 \text{ cm}^3 \end{aligned} \right\}$$

### j.) Cone

\* need slant height

$$12^2 + 16^2 = l^2$$

$$l = 20$$

$$SA = \pi(12)(20) + \pi(12)^2$$

$$= 240\pi + 144\pi$$

$$= 384\pi = 1206.37 \text{ in}^2$$

$$V = \frac{\pi(12)^2(16)}{3}$$

$$= 2304\pi = 2412.74 \text{ in}^3$$

### l.) Sphere

$$SA = 4\pi(a)^2$$

$$= 324\pi = 1017.88 \text{ in}^2$$

$$V = \frac{4\pi(a)^3}{3}$$

$$= 972\pi = 3053.63 \text{ in}^3$$

12. i, j, k, l

M.

## Composites

~~SA~~

### ① Rect. Prism

$$SA = ph + B$$

$$P: 6(4) = 24$$

$$h: 8$$

$$B = 6^2 = 36$$

$$SA = 24(8) + 36$$

$$= 228$$



### ② Pyramid

$$SA = \frac{Ph}{2}$$

$$= 24(5)$$

$$2$$

$$= 60$$

### Entire Figure

$$228 + 60 = 288 \text{ cm}^2$$

### ① Rect. Prism

$$V = Bh$$

$$= 36(8)$$

$$= 288$$

### ② Pyramid

$$V = \frac{Bh}{3}$$

\* height

$$3^2 + h^2 = 5^2$$

$$h = 4$$

$$V = \frac{36(4)}{3}$$

$$= 48$$

### Entire Figure

$$288 + 48 = 336 \text{ cm}^3$$

D.m

n.

Q) SA

① Cone

$$SA = \pi r l$$

\* need slant height

$$2^2 + 10^2 = l^2$$

$$l = \sqrt{10.20}$$

$$SA = \pi(2)(10.20)$$

$$= 64.09$$

V

② Hemisphere

$$SA = 2\pi r^2$$

$$= 2\pi(2)^2$$

$$= 25.13$$

Entire Figure

$$64.09 + 25.13 = 89.22 \text{ in}^2$$

① Cone

$$V = \frac{\pi r^2 h}{3}$$

$$= \pi(2)^2(10)$$

3

$$= -11.89$$

② Hemisphere

$$V = \frac{4}{3}\pi r^3$$

$$= \frac{4}{3}\pi(2)^3$$

3

$$= 16.76$$

Entire Figure

$$41.89 + 16.76 = 58.65 \text{ cm}^3$$

\* hen cut in half

Q) SA

① Cylinder

$$SA = 2\pi r h + 2\pi r^2$$

$$= 2\pi(3)(5.1) + \pi(3^2)$$

$$= 124.41$$

V

② Cone

$$SA = \pi r l$$

$$= \pi(3)(8.4)$$

$$= 79.17$$

Entire Figure

$$124.41 + 79.17 = 203.58 \text{ cm}^2$$

① Cylinder

$$V = \pi(3)^2(5.1)$$

$$= 144.2$$

$$= 45.9\pi$$

② Cone

$$V = \frac{\pi r^2 h}{3}$$

$$\rightarrow V = \frac{1}{3}\pi(3^2)(7.85)$$

3

\* need height

$$3^2 + h^2 = 8.4^2$$

$$= 73.98$$

$$h = 7.85$$

$$= 23.55\pi$$

Entire Figure

$$144.2 + 73.98$$

$$= 218.18 \text{ cm}^3$$

12 n, 128,

4) Find the unknown value for the right cylinder with radius  $r$ , height  $h$ , and surface area  $S$ .

a)  $r = \underline{1.038}$ ,  $h = 14$ ,  $S = 98$

b)  $r = 1.6$ ,  $h = \underline{1.95}$ ,  $S = 86$

$$98 = 2\pi r(14) + 2\pi r^2$$

$$98 = 28\pi r + 2\pi r^2$$

$$\frac{98}{2\pi} = \frac{2\pi(14r + r^2)}{2\pi}$$

$$r^2 + 14r - 15.6 = 0$$

5) Find the unknown value for the right cylinder with radius  $r$ , height  $h$ , and volume  $V$ .

a)  $r = 10$ ,  $h = \underline{4.0}$ ,  $V = 144$

$$V = \pi r^2 h$$

$$144 = \pi 10^2 h$$

$$\frac{144}{100\pi} = \frac{144\pi}{100\pi} h$$

6) The dimensions of Box A are 2" by 6" by 10" and the dimensions of Box B are 3" by 5" by 8".

a) Find the difference in volumes of A and B  $\underline{120 - 120}$ .

Both boxes have the same volume  
 $120 \text{ in}^3$

b) Find the difference in surface areas of A and B  $\underline{184 - 158}$

Box A has a SA that is  $26 \text{ in}^2$  larger

c) Find the ratio of Surface Areas of A to B  $\underline{92 : 79}$

7) If the ratio of Volumes of two prisms is  $\frac{8}{27}$  and the edge of the smaller prism is 20 inches, what is the length of the corresponding edge in the larger prism?  $\underline{x = 30 \text{ in.}}$

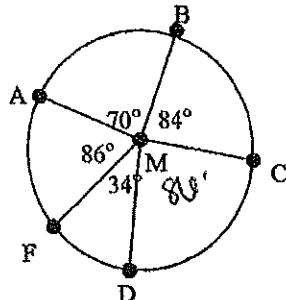
$$\frac{a}{b} = \frac{2}{3}$$

$$\frac{2}{3} = \frac{20}{x}$$

$$2x = 60$$

### Section 9

1) Find the degree measures of each arc or angle by using the central angle measures given in  $\odot M$



- |                     |                         |                     |                         |
|---------------------|-------------------------|---------------------|-------------------------|
| a) $m\widehat{AC}$  | $\underline{154^\circ}$ | b) $m\widehat{FA}$  | $\underline{810^\circ}$ |
| c) $m\widehat{CBF}$ | $\underline{240^\circ}$ | d) $m\widehat{DB}$  | $\underline{810^\circ}$ |
| e) $m\widehat{ADC}$ | $\underline{200^\circ}$ | f) $m\widehat{DCA}$ | $\underline{240^\circ}$ |
| g) $m\angle DMC$    | $\underline{810^\circ}$ |                     |                         |

2) Determine the missing value of an arc with length  $L$ , in a circle with radius  $r$ , and degree measure  $M$ .

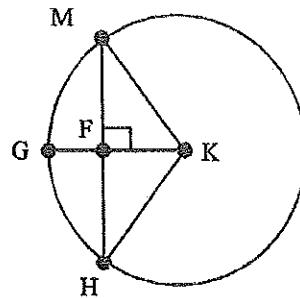
a)  $L = 15$ ,  $r = 12$ ,  $M = \underline{71.02^\circ}$

b)  $L = \frac{\frac{24}{3}\pi r}{\frac{114}{3}\pi}$ ,  $r = 8.5$ ,  $M = 240^\circ$

(13)

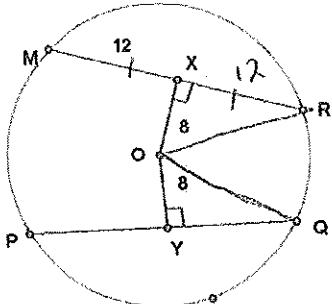
3) Refer to  $\odot K$ , in which  $\overline{KG} \perp \overline{MH}$  at F for the following.

- $\overline{MF} \cong \overline{FH}$  why? CHORD IS BISECTED
- $\overline{KG} \cong \overline{MK}$  and  $\overline{KH} \cong \overline{MH}$  why? ALL RADII  $\cong$
- If  $KH = 2$  and  $KF = 1$ , what is  $MF$ ?  $\sqrt{3}$  or 1.73
- If  $MK = 5$  and  $GF = 2$ , what is  $FH$ ? 4

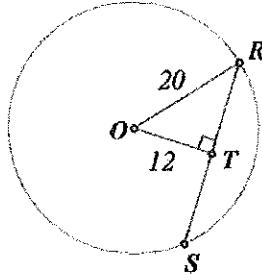


4) Find the indicated measure.

a)  $OQ = 14.42$   
(O is the center of the circle)



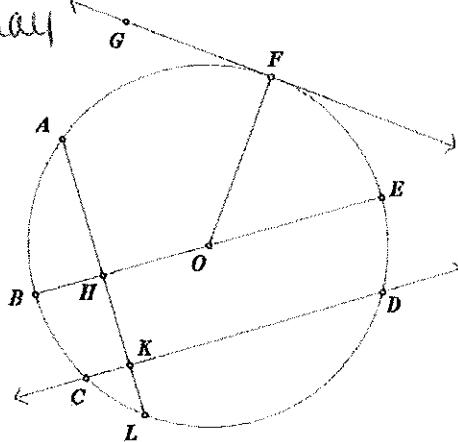
b)  $RS = 32$   
(O is the center of the circle)



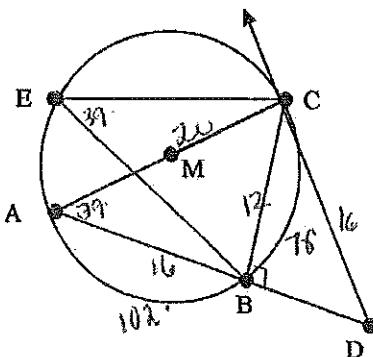
5) Using circle O below, name the following:

ANSWERS MAY VARY

- Chord  $\overline{AL}$ ,  $\overline{CD}$
- Diameter  $\overline{BZ}$
- Central Angle  $\angle FOE$ ,  $\angle BOF$
- Minor Arc  $\overarc{AF}$ ,  $\overarc{FE}$
- Major Arc  $\overarc{BZL}$
- Semicircle  $\overarc{BFE}$
- Radius  $\overline{OF}$
- Tangent  $\overline{GF}$
- Point of Tangency F



6) For the following, in  $\odot M$ ,  $\overline{AC}$  is the diameter,  $\overline{DC}$  is tangent to the circle at point C, and  $m\widehat{BC} = 78^\circ$ .



- $m\angle BAC$   $39^\circ$
- $m\angle BEC$   $39^\circ$
- $m\widehat{AB}$   $102^\circ$
- $m\angle ACB$   $51^\circ$
- $m\angle ABC$   $90^\circ$
- $m\angle ACD$   $90^\circ$

- $\overarc{EC}$  is a minor arc,  $\overarc{ACB}$  is a major arc
- $\overline{MA}$  is a radius,  $\overline{AC}$  is a diameter
- $\overline{CD}$  is a tangent,  $\overline{EC}$  is a chord

In  $\odot M$ , if  $BC = 12$ ,  $CD = 16$ , and  $AC = 20$ , find the following:

j)  $BD = 10.58$

k)  $AD = 24.58$

Find the measure of the arc or angle in  $\odot M$ .

7.  $m\angle QMP$   $60^\circ$

8.  $m\angle NMO$   $110^\circ$

9.  $m\angle PNO$   $35^\circ$

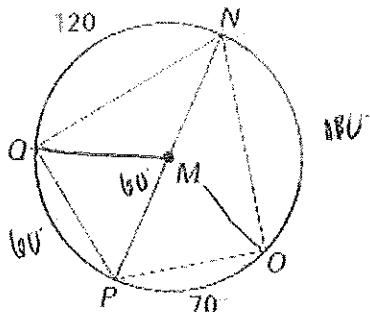
10.  $m\angle QNP$   $30^\circ$

11.  $m\angle QO$   $130^\circ$

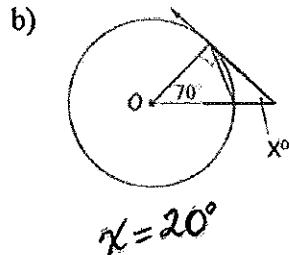
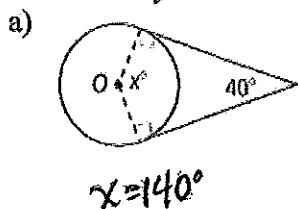
12.  $m\angle NOP$   $90^\circ$

13.  $m\angle P\bar{Q}$   $60^\circ$

14.  $m\angle QN$   $250^\circ$



- 15) What is the value of  $x$ ? Lines that appear to be tangent are tangent. Round to the nearest hundredth if necessary.

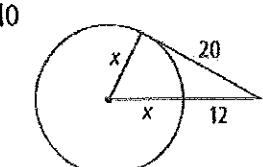


c)

$$x^2 + 9^2 = (x+6)^2$$

$$x^2 + 81 = x^2 + 12x + 36$$

$$x = 3.75$$



$$x^2 + 20^2 = (x+12)^2$$

$$x^2 + 400 = x^2 + 24x + 144$$

$$x \approx 10.67$$

- 16) Write the equation for the circle with center (2, 4) and radius = 7 in

$$(x-2)^2 + (y-4)^2 = 49$$

- 17) Write the equation for the circle with center (-3, 1) and diameter = 18 in  $r = 9$

$$(x+3)^2 + (y-1)^2 = 81$$

- 18) Find the center and radius of the circle:  $(x-7)^2 + (y+12)^2 = 144$

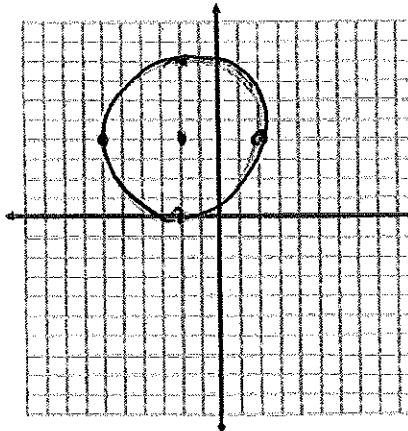
Center:  $(7, -12)$   $r = 12$

- 19) Find the center and radius of the circle:  $(x+5)^2 + (y+8)^2 = 225$

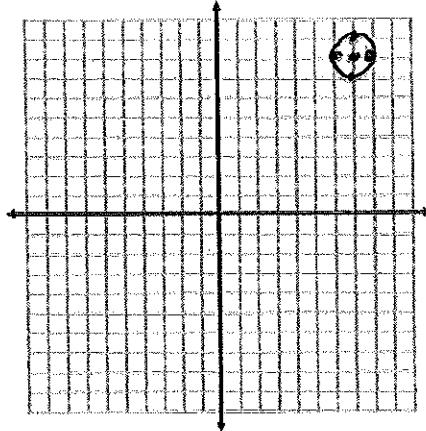
Center  $(-5, -8)$   $r = 15$

- 20) Graph the circle on the coordinate plane.

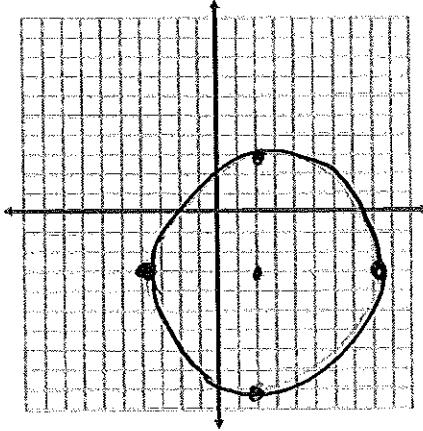
a.  $(x+2)^2 + (y-4)^2 = 16$



b.  $(x-7)^2 + (y-8)^2 = 1$



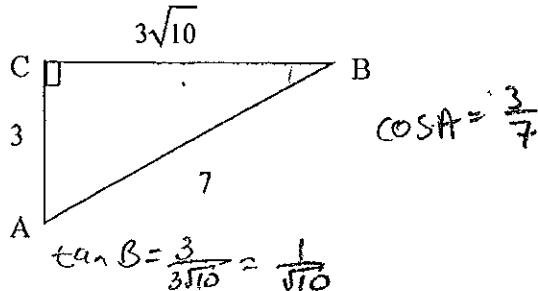
c.  $(x-2)^2 + (y+3)^2 = 36$



## Section 10

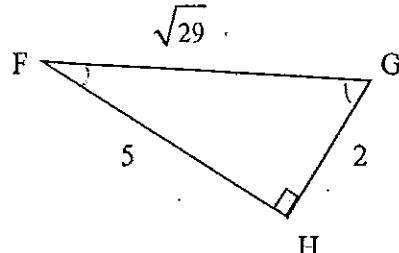
1) Determine the trigonometric ratio. Leave your answers as simplified fractions.

a)  $\tan B = \frac{1}{\sqrt{10}} = \frac{\sqrt{10}}{10}$  b)  $\cos A = \frac{3}{7}$



c)  $\sin F = \frac{2}{\sqrt{29}} = \frac{2\sqrt{29}}{29}$  d)  $\tan G = \frac{5}{2}$

$\sin F = \frac{2}{\sqrt{29}}$



2) Find the marked side of each of the following triangles.

a)  $32.3 \text{ m}$   $\cos(58^\circ) = \frac{y}{32.3}$

$y = 17.12$

b)  $17 \text{ mm}$   $\cos(20^\circ) = \frac{w}{17}$

$w = 16.09$

c)  $29 \text{ cm}$   $\sin(47^\circ) = \frac{x}{29}$

$x = 21.21$

d)  $0.39 \text{ m}$   $\tan(35^\circ) = \frac{b}{0.39}$

$b = 0.27$

3) Find the value for each of the marked angles.

a)  $6.2 \text{ m}$   $\tan(\theta) = \frac{3.6}{6.2}$

$\theta = 30^\circ$

b)  $56.0 \text{ cm}$   $\cos(\theta) = \frac{56}{72.9}$

$\theta = 40^\circ$

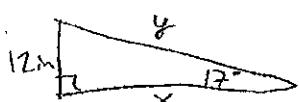
c)  $7.8 \text{ m}$   $\sin(\theta) = \frac{4.9}{7.8}$

$\theta = 39^\circ$

d)  $97 \text{ cm}$   $\tan(\theta) = \frac{97}{128}$

$\theta = 37^\circ$

4) A skateboarding ramp is 12 in. high and rises at an angle of  $17^\circ$ . How long is the base of the ramp? What is the length of the ramp? Round your answer to the nearest inch.



$\tan(17^\circ) = \frac{12}{x}$

$x = 39 \text{ in} \rightarrow \text{base}$

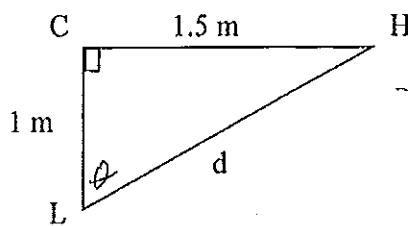
$\sin(17^\circ) = \frac{12}{y}$

$y = 41 \text{ in} \rightarrow \text{length}$

5) Joey is walking home from the library. He can walk for 1 mile along the street, then turn right and walk 1.5 miles along another street; or he can cut across a large field straight to his house. At what angle,  $\theta$ , should he head off from the library, and how far,  $d$ , should he cut across the field?

$\theta = 56^\circ$

$d = 1.8 \text{ m}$



$\tan(\theta) = \frac{1.5}{1}$

$\theta = 56^\circ$

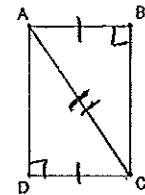
$\sin(56^\circ) = \frac{1.5}{d}$

$d = 1.8$

(16)

## Proofs

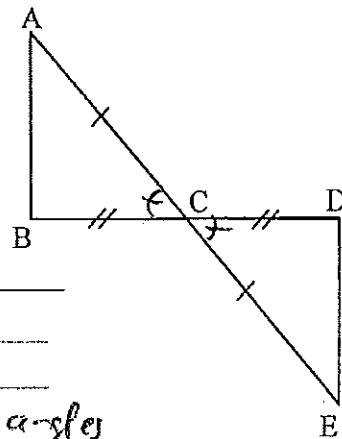
- 1) Given:  $\angle B$  and  $\angle D$  are right angles,  $\overline{AB} \cong \overline{CD}$   
 Prove:  $\triangle DAC \cong \triangle BCA$



Statements	Reasons
1. $\angle B$ and $\angle D$ are right angles, $\overline{AB} \cong \overline{CD}$	1. Given
2. $\triangle ADC$ and $\triangle CBA$ are right triangles	2. Definition of Right Triangles
3. $\overline{AC} \cong \overline{CA}$	3. Reflexive Property of Congruence
4. $\triangle ADC \cong \triangle CBA$	4. Hypotenuse Leg Theorem
5. $\angle DAC \cong \angle BCA$	5. Corresponding Parts of Congruent Triangles are Congruent

2)

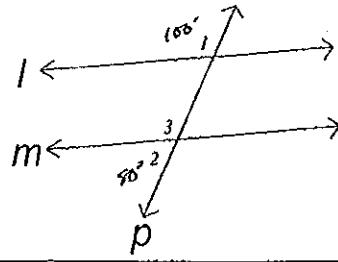
Fill in the blanks in the table below to prove  
 $\angle CBA \cong \angle CDE$



Statement	Reason
$\overline{CB} \cong \overline{DC}$	Given
$\overline{CA} \cong \overline{CE}$	Given
$\angle BCA \& \angle DCE$ are vertical angles	Definition of vertical angles
$\angle BCA \cong \angle DCE$	Vertical Angle Theorem
$\triangle BCA \cong \triangle DCE$	Side-Angle-Side Theorem
$\angle CBA \cong \angle CDE$	Corresponding Parts of congruent Triangles are congruent

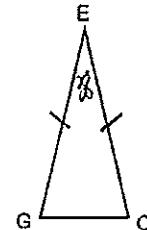
(7)

- 3) Given:  $m\angle 1 = 100^\circ$ ,  $m\angle 2 = 80^\circ$   
 Prove:  $l \parallel m$



Statements	Reasons
1. $m\angle 1 = 100^\circ$ , $m\angle 2 = 80^\circ$	1. Given
2. $\angle 2$ and $\angle 3$ form a linear pair	2. Definition of Linear Pair
3. $\angle 2$ and $\angle 3$ are supplementary	3. Linear Pair Property
4. $m\angle 2 + m\angle 3 = 180^\circ$	4. Definition of Supplementary angles
5. $80^\circ + m\angle 3 = 180^\circ$	5. Substitution Property of Equality
6. $m\angle 3 = 100^\circ$	6. Subtraction Property of Equality
7. $m\angle 1 = m\angle 3$	7. Substitution Property of Equality
8. $\angle 1 \cong \angle 3$	8. Definition of Angle Congruence
9. $\angle 1$ and $\angle 3$ are Corresponding Angles	9. Definition of Corresponding Angles
10. $l \parallel m$	10. Converse of Corresponding Angles Theorem

- 4)  
 Given:  $\overline{GE} \cong \overline{OE}$  ;  $m\angle E = 38^\circ$   
 Prove:  $m\angle G = 71^\circ$



Statements	Reasons
1. $\overline{GE} \cong \overline{OE}$	1. Given
2. $\angle G \cong \angle O$	2. Isosceles Triangle Theorem
3. $m\angle G = m\angle O$	3. Definition of Angle Congruence
4. $m\angle E = 38^\circ$	4. Given
5. $m\angle G + m\angle E + m\angle O = 180^\circ$	5. Triangle Sum Theorem
6. $m\angle G + 38^\circ + m\angle G = 180^\circ$	6. Substitution Property of Equality
7. $2 \cdot m\angle G + 38^\circ = 180^\circ$	7. Combine like terms
8. $2 \cdot m\angle G = 142^\circ$	8. Subtraction Property of Equality
9. $m\angle G = 71^\circ$	9. Division Property of Equality