#### **October 21, 2015 Math 6 Lesson 2.2**

Learning Objective: Students will be able to use a visual model and a formal rule to divide by a fraction.

# Warm Up

$$276 \times 150$$

# Warm Up Answers

705	183	625	276
× 156	× 515	× 208	× 150
4,230	915	5,000	0
35,250	1,830	0	13,800
70,500	91,500	125,000	27,600
109,980	94,245	130,000	41,400

9!	57	ļ	547		719		919
39	93	×	404	×	628	×	800
,8'	71	2,	188	5,	752		0
,13	30		0	14,	380		0
,1(	00	218,8	300	431,	400	735	,200
,1(	01	220,9	988	451,	532	735	,200

Lesson 2.2

October 21, 2015

## Essential Question:

How can you divide by a fraction?

Lesson 2.2 October 21, 2015

# Lesson Objective:

Students will be able to:

use a visual model and a formal rule to divide by a fraction.

## Self-Evaluation Scale

Score	Description		
4	I can teach other students how to use a visual model and a formal rule to divide by a fraction.		
3	I can use a visual model and a formal rule to divide by a fraction.		
2	I recognize, but still need help to use a visual model and a formal rule to divide by a fraction.		
1	I do not know how to use a visual model and a formal rule to divide by a fraction.		

### Homework Answers

#### 2.1 Record and Practice Journal

Multiply. Write the answer in simplest form.

1. 
$$\frac{1}{6} \times \frac{5}{8}$$

2. 
$$\frac{7}{9} \times 3$$

3. 
$$\frac{8}{9} \times \frac{3}{5}$$

$$\frac{5}{48}$$

$$2\frac{1}{3}$$

$$\frac{8}{15}$$

4. 
$$\frac{7}{8} \times 2\frac{1}{3}$$

5. 
$$7 \times 3\frac{9}{14}$$

6. 
$$5\frac{5}{9} \times 2\frac{7}{10}$$

$$2\frac{1}{24}$$

$$25\frac{1}{2}$$

- 7. You reserve  $\frac{2}{5}$  of the seats on a tour bus. You are able to fill  $\frac{5}{8}$  of the seats you reserve. What fraction of the seats on the bus are you able to fill?

8. A triangle has a base of  $5\frac{2}{3}$  inches and a height of 3 inches. What is the area of the triangle?

$$8\frac{1}{2}$$
 in.<sup>2</sup>

# Activity 1 & 2

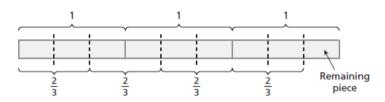
With a partner, work on Activity I & 2 on pages 35 & 36 of your Big Ideas Record and Practice Journal.

1 ACTIVITY: Dividing by a Fraction

Work with a partner. Write the division problem and solve it using a model.

a. How many two-thirds are in three?

The division problem is \_\_\_\_\_\_.



How many groups of  $\frac{2}{3}$  are in 3?

The remaining piece represents \_\_\_\_\_ of  $\frac{2}{3}$ .

So, there are \_\_\_\_\_ groups of  $\frac{2}{3}$  in 3.

So, \_\_\_\_\_ = \_\_\_\_

b. How many halves are in five halves?

1 1 1 2

c. How many four-fifths are in eight?

#### Work with a partner.

a. Complete each table.

#### **Division Table**

8 ÷ 16	$\frac{1}{2}$
8 ÷ 8	1
8 ÷ 4	2
8 ÷ 2	4
8 ÷ 1	8
$8 \div \frac{1}{2}$	
$8 \div \frac{1}{4}$	
$8 \div \frac{1}{8}$	

#### **Multiplication Table**

$8 \times \frac{1}{16}$	$\frac{1}{2}$
$8 \times \frac{1}{8}$	1
$8 \times \frac{1}{4}$	2
$8 \times \frac{1}{2}$	4
8 × 1	8
8 × 2	
8 × 4	
8 × 8	

Two numbers whose product is 1 are **reciprocals**. To write the reciprocal of a number, write the number as a fraction. Then invert the fraction. So, the reciprocal of a fraction  $\frac{a}{b}$  is  $\frac{b}{a}$ , where a and  $b \neq 0$ .

### The Meaning of a Word Invert

When you **invert** a glass, you turn it over.



### 1 Writing Reciprocals

	Original Number	Fraction	Reciprocal	Check
a.	$\frac{3}{5}$	$\frac{3}{5}$	$\frac{5}{3}$	$\frac{3}{5} \times \frac{5}{3} = 1$
b.	$\frac{9}{5}$	$\frac{9}{5}$	$\frac{5}{9}$	$\frac{9}{5} \times \frac{5}{9} = 1$
c.	2	$\frac{2}{1}$	$\frac{1}{2}$	$\frac{2}{1} \times \frac{1}{2} = 1$

## On Your Own

Write the reciprocal of the number.

1. 
$$\frac{3}{4}$$

3. 
$$\frac{7}{2}$$

**4**. 
$$\frac{4}{9}$$



### **Dividing Fractions**

**Words** To divide a number by a fraction, multiply the number by the reciprocal of the fraction.

**Numbers** 
$$\frac{1}{5} \div \frac{3}{4} = \frac{1}{5} \times \frac{4}{3} = \frac{1 \times 4}{5 \times 3}$$

**Algebra** 
$$\frac{a}{b} \div \frac{c}{d} = \frac{a}{b} \cdot \frac{d}{c} = \frac{a \cdot d}{b \cdot c}$$
, where *b*, *c*, and  $d \neq 0$ 

### 2 Dividing a Fraction by a Fraction

Find 
$$\frac{1}{6} \div \frac{2}{3}$$
.

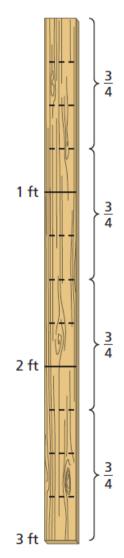
$$\frac{1}{6} \div \frac{2}{3} = \frac{1}{6} \times \frac{3}{2}$$
 Multiply by the reciprocal of  $\frac{2}{3}$ , which is  $\frac{3}{2}$ .

$$= \frac{1 \times 3}{8 \times 2}$$
 Multiple 2

Multiply fractions. Divide out the common factor 3.

$$\frac{1}{4}$$
 Simplify.

### **EXAMPLE** 3 Dividing a Whole Number by a Fraction



A piece of wood is 3 feet long. How many  $\frac{3}{4}$ -foot pieces can you cut from the piece of wood?

**Method 1:** Draw a diagram. Mark each foot on the diagram. Then divide each foot into  $\frac{1}{4}$ -foot sections.

Count the number of  $\frac{3}{4}$ -foot pieces of wood. There are four.

So, you can cut four  $\frac{3}{4}$ -foot pieces from the piece of wood.

**Method 2:** Divide 3 by  $\frac{3}{4}$  to find the number of  $\frac{3}{4}$ -foot pieces.

$$3 \div \frac{3}{4} = 3 \times \frac{4}{3}$$
 Multiply by the reciprocal of  $\frac{3}{4}$ , which is  $\frac{4}{3}$ .

$$= \frac{\cancel{3} \times 4}{\cancel{3}_{1}}$$
 Multiply. Divide out the common factor 3.

$$= 4$$
 Simplify.

So, you can cut four  $\frac{3}{4}$ -foot pieces from the piece of wood.

### On Your Own

Divide. Write the answer in simplest form.

**5.** 
$$\frac{2}{7} \div \frac{1}{3}$$

**6.** 
$$\frac{1}{2} \div \frac{1}{8}$$

7. 
$$\frac{3}{8} \div \frac{1}{4}$$

**5.** 
$$\frac{2}{7} \div \frac{1}{3}$$
 **6.**  $\frac{1}{2} \div \frac{1}{8}$  **7.**  $\frac{3}{8} \div \frac{1}{4}$  **8.**  $\frac{2}{5} \div \frac{3}{10}$ 

**9.** How many  $\frac{1}{2}$ -foot pieces can you cut from a 7-foot piece of wood?

### 4 Dividing a Fraction by a Whole Number

Find 
$$\frac{4}{5} \div 2$$
.

$$\frac{4}{5} \div 2 = \frac{4}{5} \div \frac{2}{1}$$
Write 2 as an improper fraction.
$$= \frac{4}{5} \times \frac{1}{2}$$
Multiply by the reciprocal of  $\frac{2}{1}$ , which is  $\frac{1}{2}$ .
$$= \frac{4 \times 1}{5 \times 10^{12}}$$
Multiply fractions. Divide out the common factor 2.

$$=\frac{2}{5}$$
 Simplify.

# Assignment

Complete problems 8, 9, 11, 13, 19, 21, 43, 48, & 51 on pages 67 & 68 in your Big Ideas Text Book.

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## Homework

In your Big Ideas Record and Practice Journal page 38.